

# Package ‘AnomalyScore’

May 6, 2026

**Title** Anomaly Scoring for Multivariate Time Series

**Version** 0.1

**Description** Compute an anomaly score for multivariate time series based on the k-nearest neighbors algorithm. Different computations of distances between time series are provided.

**License** GPL (>= 3)

**Imports** dtw, class, aetsa, transport, marima, TSA, RANN, MASS, mvLSW, stats

**Encoding** UTF-8

**RoxygenNote** 7.3.1

**NeedsCompilation** no

**Author** Guillermo Granados [aut, cre] (ORCID:  
<<https://orcid.org/0000-0003-4868-6163>>)

**Maintainer** Guillermo Granados <guillermo.granadosgarcia@outlook.com>

**Repository** CRAN

**Date/Publication** 2024-11-21 08:00:13 UTC

## Contents

all_bands . . . . .	2
Anomalyscoresframe . . . . .	3
Cort . . . . .	4
DEcort . . . . .	4
DEcortNorm . . . . .	5
distance_matrix_banddepth . . . . .	6
distance_matrix_CGCI . . . . .	7
distance_matrix_coherence . . . . .	8
distance_matrix_cort . . . . .	9
distance_matrix_cortNorm . . . . .	10
distance_matrix_dtw . . . . .	11
distance_matrix_mahalanobis . . . . .	12
distance_matrix_mvLWS . . . . .	12
distance_matrix_PDC . . . . .	13

distance_matrix_PMIME . . . . .	14
distance_matrix_RGPDC . . . . .	15
distance_matrix_wasserstein . . . . .	16
DTWcort . . . . .	16
dxy_bands . . . . .	17
informative_bands . . . . .	18
kneighbors_distance_docall . . . . .	19
matrix_PDC . . . . .	20
mBTS . . . . .	20
mBTSCGCI . . . . .	21
mBTSRGPDC . . . . .	22
mBTS_Af_mat . . . . .	22
multilagmatrix . . . . .	23
PMIME . . . . .	23
sqnorms . . . . .	25

## Index 26

---

all_bands	<i>Pairwise band generation in a multivariate time series</i>
-----------	---

---

### Description

takes all the pairs of series in a multivariate set and compute the band between each pair od series

### Usage

```
all_bands(series)
```

### Arguments

series	A matrix of n columns representing a multivariate time series, each column is a univariate time series
--------	--

### Value

a list with two elements the lowerbounds of all  $(n)(n-1)/2$  pairs and the upperbounds of the pairwise bands

### See Also

Band Depth Clustering for Nonstationary Time Series and Wind Speed Behavior (2018) Tupper et al

### Examples

```
X=matrix( rnorm(200), ncol=10 )
all_bands(X)
```

---

Anomalyscoresframe      *Anomaly score computation for a set of distances*

---

## Description

Computes anomaly scores for a selection of different distances for a single dataset.

## Usage

```
Anomalyscoresframe(unit, knn, measures, dparams)
```

## Arguments

unit	A matrix representing a multivariate time series where each column is a univariate time series.
knn	number of nearest neighbors to consider for the anomaly scores
measures	vector with the indexes of the selected measures 1=Cort, 2=Wasserstein, 3=Mahalanobis, 4=Normalized Cort, 5=Coherence, 6=PDC, 7=CGCI, 8=RGPDC, 9=PMIME, 10=mvLWS, 11=Band depth
dparams	a list where each element is a list with all the parameters necessary to compute the selected distances. If the distance does not need further parameters then define an empty list

## Value

A dataframe with the names of series in unit as a column called "series" and the corresponding scores computed for each distance. The rank is ordered with respect to the first measure in the measures index vector

## See Also

Guillermo Granados, and Idris Eckley. "Electricity Demand of Buildings Benchmarked via Regression Trees on Nearest Neighbors Anomaly Scores"

## Examples

```
unit=matrix( rnorm(500), ncol=5 )
measures= c(1,5,11 ) # Cort, Coherence and Band depth
knn=3
dparams=list(
  list(k=2),
  list( span1=2, span2=2, period = 5),
  list( )
)
Anomalyscoresframe(unit, knn,measures, dparams)
```

Cort

*Temporal correlation coefficient*

---

**Description**

Return the temporal correlations of two time series by first taking the lag one differences of each series and the computing the correlation coefficient.

**Usage**

```
Cort(S1, S2)
```

**Arguments**

S1                    A vector representing a univariate time series  
S2                    A second vector representing a univariate time series

**Value**

A coefficient in the interval  $[-1, 1]$  representing the lag 1 correlation

**See Also**

Douzal-Chouakria, Ahlame, and Cecile Amblard. "Classification Trees for Time Series." Pattern Recognition 45, no. 3 (March 2012): 1076-91. doi:[10.1016/j.patcog.2011.08.018](https://doi.org/10.1016/j.patcog.2011.08.018)

**Examples**

```
S1=rnorm(100)  
S2=rnorm(100)  
Cort(S1, S2)
```

---

DEcort

*Distance based on value and behavior of the time series*

---

**Description**

Return a weighted distance based on a weighted sum of the Euclidean norm and the temporal correlation coefficient. The distance is inflated in the presence of NA compensating for the lack of information.

**Usage**

```
DEcort(k, S1, S2)
```

**Arguments**

k	The parameter $k$ controls the contribution of the sum of squares comparison as a value-based metric and the $Cort$ quantity as a behavioral metric; when $k=0$ , then the distance is equal to the value-based metric, on the other hand, when $k=6$ the distance is mainly determined by the value of the temporal correlation $Cort$ .
S1	A vector representing a univariate time series
S2	A second vector representing a univariate time series

**Value**

a non-zero value

**See Also**

Douzal-Chouakria, Ahlame, and Cecile Amblard. "Classification Trees for Time Series." Pattern Recognition 45, no. 3 (March 2012): 1076-91. doi:[10.1016/j.patcog.2011.08.018](https://doi.org/10.1016/j.patcog.2011.08.018)

**Examples**

```
S1=rnorm(100)
S2=rnorm(100)
k=1
DEcort(k,S1, S2)
```

---

DEcortNorm	<i>Normalized version of the Cort distance the modification is based on using the coefficient of variation rather than euclidean distance, performed by normalizing by the absolute value of the total differences of the series.</i>
------------	---

---

**Description**

Normalized version of the Cort distance the modification is based on using the coefficient of variation rather than euclidean distance, performed by normalizing by the absolute value of the total differences of the series.

**Usage**

```
DEcortNorm(k, S1, S2)
```

**Arguments**

k	The parameter $k$ controls the contribution of the sum of squares comparison as a value-based metric and the $Cort$ quantity as a behavioral metric; when $k=0$ , then the distance is equal to the value-based metric, on the other hand, when $k=6$ the distance is mainly determined by the value of the temporal correlation $Cort$ .
S1	A vector representing a univariate time series
S2	A second vector representing a univariate time series

**Value**

a non-zero value

**See Also**

Granados-Garcia, and Idris Eckley. "Building Electricity Demand Benchmarking via a Regression Trees on Anomaly Scores"

**Examples**

```
S1=rnorm(100)
S2=rnorm(100)
k=1
DEcortNorm(k,S1, S2)
```

---

distance\_matrix\_banddepth

*Pairwise distance matrix based on the band depth distance*

---

**Description**

Pairwise distance matrix based on the band depth distance

**Usage**

```
distance_matrix_banddepth(unit)
```

**Arguments**

unit	A matrix representing a multivariate time series where each column is a univariate time series.
------	---

**Value**

a matrix with pairwise distances

**See Also**

Band Depth Clustering for Nonstationary Time Series and Wind Speed Behavior (2018) Tupper et al

**Examples**

```
X=matrix( rnorm(2000), ncol=10 )
distance_matrix_banddepth(unit=X)
```

---

distance\_matrix\_CGCI *Pairwise distance matrix based on the conditional Granger causality index*

---

**Description**

Pairwise distance matrix of a multivariate time series based on the the conditional Granger causality index distance between two series

**Usage**

```
distance_matrix_CGCI(unit, pmax)
```

**Arguments**

unit	A matrix representing a multivariate time series where each column is a univariate time series.
pmax	maximum order(lag) of the VAR model to be considered

**Value**

a matrix with pairwise distances

**See Also**

Siggiridou, Elsa, and Dimitris Kugiumtzis. "Granger Causality in Multivariate Time Series Using a Time-Ordered Restricted Vector Autoregressive Model." IEEE Transactions on Signal Processing 64, no. 7 (April 2016): 1759-73. doi:[10.1109/TSP.2015.2500893](https://doi.org/10.1109/TSP.2015.2500893)

**Examples**

```
X=matrix( rnorm(2000), ncol=10 )
pmax=4
distance_matrix_CGCI(unit=X, pmax)
```

---

distance\_matrix\_coherence

*Distance matrix from a coherence measure*

---

## Description

Pairwise distance matrix of a multivariate time series based on computing the squared coherence and transformed it to represent a distance at a specific frequency

## Usage

```
distance_matrix_coherence(unit, span1, span2, period)
```

## Arguments

unit	A matrix representing a multivariate time series where each column is a univariate time series.
span1	Odd integer giving the widths of modified Daniell smoothers to be used to smooth the periodogram. Refers to the bandwidth of the smoothing process.
span2	Odd integer giving the widths of modified Daniell smoothers to be used to smooth the periodogram. Control another level of smoothing to the spectral density estimation without altering the peaks
period	Integer referencing the index of the frequency to use for the distance. It gives the Hertz or periods per unit of time; i.e., if the sampling is per minute, and each hour cycle is the period of interest

## Value

a matrix with pairwise distances

## See Also

For more details, check the `astsa` package documentation on CRAN or visit the GitHub repository <https://github.com/nickpoison/astsa>.

## Examples

```
X=matrix( rnorm(2000), ncol=10 )
span1=2
span2=2
period=3
distance_matrix_coherence(unit=X, span1, span2, period )
```

---

distance\_matrix\_cort *Distance matrix from a pattern recognition distance*

---

### Description

pairwise distance matrix of a multivariate time series based on a value (Euclidean distance) and behavior (temporal correlation) measures

### Usage

```
distance_matrix_cort(k, unit)
```

### Arguments

- |      |  |
|------|--|
| k    | The parameter <code>k</code> controls the contribution of the sum of squares comparison as a value-based metric and the <code>Cort</code> quantity as a behavioral metric; when <code>k=0</code> , then the distance is equal to the value-based metric, on the other hand, when <code>k=6</code> the distance is mainly determined by the value of the temporal correlation <code>Cort</code> . |
| unit | A matrix representing a multivariate time series where each column is a univariate time series.  |

### Value

a matrix with pairwise distances

### See Also

Douzal-Chouakria, Ahlame, and Cecile Amblard. "Classification Trees for Time Series." *Pattern Recognition* 45, no. 3 (March 2012): 1076-91. doi:[10.1016/j.patcog.2011.08.018](https://doi.org/10.1016/j.patcog.2011.08.018)

### Examples

```
X=matrix( rnorm(200), ncol=10 )
k=2
distance_matrix_cort(k,X)
```

---

`distance_matrix_cortNorm`*Normalized distance matrix from a pattern recognition distance*

---

### Description

pairwise distance matrix of a multivariate time series based on a value (Coefficient of variation) and behavior (temporal correlation) measures

### Usage

```
distance_matrix_cortNorm(k, unit)
```

### Arguments

<code>k</code>	The parameter <code>k</code> controls the contribution of the sum of squares comparison as a value-based metric and the <code>Cort</code> quantity as a behavioral metric; when <code>k=0</code> , then the distance is equal to the value-based metric, on the other hand, when <code>k=6</code> the distance is mainly determined by the value of the temporal correlation <code>Cort</code> .
<code>unit</code>	A matrix representing a multivariate time series where each column is a univariate time series.

### Value

a matrix with pairwise distances

### See Also

Guillermo Granados, and Idris Eckley. "Electricity Demand of Buildings Benchmarked via Regression Trees on Nearest Neighbors Anomaly Scores"

### Examples

```
X=matrix( rnorm(200), ncol=10 )
k=2
distance_matrix_cortNorm(k,X)
```

---

distance\_matrix\_dtw    *Normalized distance matrix from dynamic time-warping distance*

---

## Description

pairwise distance matrix of a multivariate time series based on a minimal mapping between two time series weighted by temporal correlation

## Usage

```
distance_matrix_dtw(k, unit, maxwindow)
```

## Arguments

k	The parameter $k$ controls the contribution of the sum of squares comparison as a value-based metric and the $Cort$ quantity as a behavioral metric; when $k=0$ , then the distance is equal to the value-based metric, on the other hand, when $k=6$ the distance is mainly determined by the value of the temporal correlation $Cort$ .
unit	A matrix representing a multivariate time series where each column is a univariate time series.
maxwindow	the maximum shift allowed between time series points.

## Value

a matrix with pairwise distances

## See Also

For more details, check the dtw package documentation on CRAN

## Examples

```
X=matrix( rnorm(200), ncol=10 )
k=2
maxwindow=10
distance_matrix_dtw(k,X,maxwindow)
```

---

distance\_matrix\_mahalanobis

*Pairwise distance matrix based on the mahalanobis distance*

---

### Description

Pairwise distance matrix of a multivariate time series based on the Mahalanobis distance between two series, modified to consider the different scales of series

### Usage

```
distance_matrix_mahalanobis(unit)
```

### Arguments

`unit`            A matrix representing a multivariate time series where each column is a univariate time series.

### Value

a matrix with pairwise distances

### See Also

Prekopcsak, Zoltan, and Daniel Lemire. "Time Series Classification by Class-Specific Mahalanobis Distance Measures." *Advances in Data Analysis and Classification* 6, no. 3 (October 2012): 185-200. doi:[10.1007/s1163401201106](https://doi.org/10.1007/s1163401201106)

### Examples

```
X=matrix( rnorm(2000), ncol=10 )
distance_matrix_mahalanobis(unit=X )
```

---

distance\_matrix\_mvLWS *Pairwise distance matrix based on the multivariate locally wavelet partial coherence*

---

### Description

Pairwise distance matrix based on the multivariate locally wavelet partial coherence

### Usage

```
distance_matrix_mvLWS(unit)
```

**Arguments**

`unit`            A matrix representing a multivariate time series where each column is a univariate time series.

**Value**

a matrix with pairwise distances

**See Also**

Park, Timothy, Idris A. Eckley, and Hernando C. Ombao. "Estimating Time-Evolving Partial Coherence Between Signals via Multivariate Locally Stationary Wavelet Processes." *IEEE Transactions on Signal Processing* 62, no. 20 (October 2014): 5240-50. doi:10.1109/TSP.2014.2343937

**Examples**

```
X=matrix( rnorm(2000), ncol=10 )
distance_matrix_mvLWS(unit=X)
```

---

distance\_matrix\_PDC    *Distance matrix from a partial directed coherence measure (PDC)*

---

**Description**

Pairwise distance matrix of a multivariate time series based on the partial directed coherence among two series. The distance considers both directions of causality and transform it to give 0 in absence of causality between the series.

**Usage**

```
distance_matrix_PDC(unit, ar, period)
```

**Arguments**

`unit`            A matrix representing a multivariate time series where each column is a univariate time series.

`ar`              Integer vector containing all the lags considered for the vector autoregressive model

`period`         Integer referencing the index of the frequency to use for the distance. It gives the Hertz or periods per unit of time; i.e., if the sampling is per minute, and each hour cycle is the period of interest

**Value**

a matrix with pairwise distances

**See Also**

Guillermo Granados, and Idris Eckley. "Electricity Demand of Buildings Benchmarked via Regression Trees on Nearest Neighbors Anomaly Scores"

**Examples**

```
X=matrix( rnorm(2000), ncol=10 )
ar=c(1, 2)
period=10
distance_matrix_PDC( unit=X, ar, period )
```

---

distance\_matrix\_PMIME *Pairwise distance matrix based on the partial mutual information of mixed embeddings (PMIME) method*

---

**Description**

Pairwise distance matrix based on the partial mutual information of mixed embeddings (PMIME) method

**Usage**

```
distance_matrix_PMIME(unit, Lmax, Tl, nnei, A)
```

**Arguments**

unit	A matrix representing a multivariate time series where each column is a univariate time series.
Lmax	: the maximum delay to search for X and Y components for the mixed embedding vector ,default is 5.
Tl	: Tl steps ahead that the mixed embedding vector has to explain. Note that if Tl>1 the future vector is of length Tl and contains the samples at times t+1,...,t+Tl ,default is 1.
nnei	: number of nearest neighbors for density estimation ,default is 5
A	: the threshold for the ratio of CMI over MI of the lagged variables for the termination criterion.

**Value**

a matrix with pairwise distances

**See Also**

Kugiumtzis, D. "Direct-Coupling Information Measure from Nonuniform Embedding." Physical Review E 87, no. 6 (June 25, 2013): 062918. doi:[10.1103/PhysRevE.87.062918](https://doi.org/10.1103/PhysRevE.87.062918)

**Examples**

```
X=matrix( rnorm(300), ncol=3 )
Lmax=2
Tl=1
nnei=5
A=.95
distance_matrix_PMIME(unit=X, Lmax, Tl, nnei, A )
```

---

distance\_matrix\_RGPDC *Pairwise distance matrix based on the restricted generalized partial directed coherence*

---

**Description**

Pairwise distance matrix of a multivariate time series based on the the restricted generalized partial directed coherence distance between two series

**Usage**

```
distance_matrix_RGPDC(unit, pmax, period)
```

**Arguments**

unit	A matrix representing a multivariate time series where each column is a univariate time series.
pmax	maximum order(lag) of the VAR model to be considered
period	Integer referencing the index of the frequency to use for the distance. It gives the Hertz or periods per unit of time; i.e., if the sampling is per minute, and each hour cycle is the period of interest

**Value**

a matrix with pairwise distances

**See Also**

Siggiridou, Elsa, Vasilios K. Kimiskidis, and Dimitris Kugiumtzis. "Dimension Reduction of Frequency-Based Direct Granger Causality Measures on Short Time Series." *Journal of Neuroscience Methods* 289 (September 2017) : 64-74. doi:[10.1016/j.jneumeth.2017.06.021](https://doi.org/10.1016/j.jneumeth.2017.06.021)

**Examples**

```
X=matrix( rnorm(2000), ncol=10 )
pmax=4
period=3
distance_matrix_RGPDC(unit=X, pmax, period)
```

distance\_matrix\_wasserstein

*Distance matrix from based on the Wasserstein distance*

---

### Description

Pairwise distance matrix of a multivariate time series based on the Wasserstein distance between the empirical distribution of the series

### Usage

```
distance_matrix_wasserstein(unit)
```

### Arguments

`unit`            A matrix representing a multivariate time series where each column is a univariate time series.

### Value

a matrix with pairwise distances

### See Also

For more details, check the transport package documentation on CRAN

### Examples

```
X=matrix( rnorm(2000), ncol=10 )
distance_matrix_wasserstein(unit=X)
```

---

DTWcort

*Extention of the dynamic time warping distance*

---

### Description

This function uses the `dtw()` function from the `dtw` R package to compute a distance based on the mapping that minimizes the distance between two sets of points, the parameters chosen are the "Manhattan" distance to compute the differences between points and the "sakoechiba" window type. Important note: the `dtw` function does not accept NA values, therefore these types of values are removed.

### Usage

```
DTWcort(k, S1, S2, maxwindow)
```

**Arguments**

k	The parameter $k$ controls the contribution of the sum of squares comparison as a value-based metric and the $Cort$ quantity as a behavioral metric; when $k=0$ , then the distance is equal to the value-based metric, on the other hand, when $k=6$ the distance is mainly determined by the value of the temporal correlation $Cort$ .
S1	A vector representing a univariate time series
S2	A second vector representing a univariate time series
maxwindow	the maximum shift allowed between time series points.

**Value**

A non-negative value representing the distance between two time series

**See Also**

Douzal-Chouakria, Ahlame, and Cecile Amblard. "Classification Trees for Time Series." *Pattern Recognition* 45, no. 3 (March 2012): 1076-91. doi:10.1016/j.patcog.2011.08.018

**Examples**

```
S1=rnorm(100)
S2=rnorm(100)
k=1
maxwindow=20
DTWcort(k,S1, S2,maxwindow)
```

---

dxy\_bands

*Band depth distance between 2 time series given a set of bands*


---

**Description**

Distance based on a depth concept, given a set of bands a modified Jaccard measure is compute between the sets of indices that two series share, the Jaccard distances then are averaged over all informative bands.

**Usage**

```
dxy_bands(allbands, x, y)
```

**Arguments**

allbands	a list with two elements the lowerbounds of all $(n)(n-1)/2$ pairs and the upperbounds of the pairwise bands.
x	A vector representing a univariate time series
y	A vector representing a univariate time series

**Value**

A non-negative value representing the distance between two time series, based on the concept of band depth.

**See Also**

Band Depth Clustering for Nonstationary Time Series and Wind Speed Behavior (2018) Tupper et al

**Examples**

```
X=matrix( rnorm(200), ncol=10 )
M=all_bands(X)
dxy_bands(M,X[,1],X[,2] )
```

---

informative_bands	<i>indexes where a series is within a specific band</i>
-------------------	---

---

**Description**

Return the indicies in which the values of a series  $x$  are located within a band  $b$ , called the informative bands.

**Usage**

```
informative_bands(allbands, x)
```

**Arguments**

allbands	a list with two elements the lowerbounds of all $(n)(n-1)/2$ pairs and the upperbounds of the pairwise bands. Result of the function all_bands
x	A vector representing a univariate time series

**Value**

A vector with indices

**See Also**

Band Depth Clustering for Nonstationary Time Series and Wind Speed Behavior (2018) Tupper et al

**Examples**

```
X=matrix( rnorm(200), ncol=10 )
M=all_bands(X)
informative_bands(M,X[,1] )
```

---

`kneighbors_distance_docal1`*K-Nearest neighbors algorithm to compute an anomaly score*

---

## Description

The method obtain a distance matrix and find the K-nearest neighbors of each series and sum their distances in the neighborhood. The sum is defined as the anomaly score, the series with higher scores implies their neighbors are far away and such a series is a potential outlier

## Usage

```
kneighbors_distance_docal1(knn, distance, dparams)
```

## Arguments

<code>knn</code>	number of nearest neighbors to consider for the anomaly score
<code>distance</code>	function name of the available distance matrices
<code>dparams</code>	a list with all the parameters for the distance matrix

## Value

A list of two elements with the anomaly scores and the distance matrix

## See Also

Guillermo Granados, and Idris Eckley. "Electricity Demand of Buildings Benchmarked via Regression Trees on Nearest Neighbors Anomaly Scores"

## Examples

```
X=matrix( rnorm(2000), ncol=10 )
distance=distance_matrix_coherence
dparams=list(unit=X, span1=2, span2=2, period = 5 )
knn=5
kneighbors_distance_docal1(knn,distance, dparams)
```

---

matrix_PDC	<i>Partial directed coherence matrix</i>
------------	--

---

**Description**

Partial directed coherence matrix

**Usage**

```
matrix_PDC(unit, ar)
```

**Arguments**

unit	A Matrix containing the multivariate time series. Each column represents a univariate time series.
ar	Integer vector containing all the lags considered for the vector autoregressive model

**Value**

An real array of dimensions, ncol(unit), ncol(unit), n, where n is the number of frequencies at which the PDC is estimated.

**Examples**

```
X=matrix( rnorm(2000), ncol=10 )
ar=c(1, 2)
matrix_PDC(X, ar)
```

---

mBTS	<i>modified Back-in-time Selection for vector AR parameters estimation</i>
------	--

---

**Description**

modified Back-in-time Selection for vector AR parameters estimation

**Usage**

```
mBTS(xM, responseindex, pmax)
```

**Arguments**

xM	the matrix of K time series (variables in columns)
responseindex	the index of the response variable in $\{1, \dots, K\}$
pmax	maximum order(lag) of the VAR model to be considered

**Value**

the matrix of all explanatory lagged variables in the DR model. The sequence of the lagged variables in 'lagM'

**See Also**

I. Vlachos and D. Kugiumtzis, "Backward-in-time selection of the order of dynamic regression prediction model," J. Forecast., vol. 32, pp. 685-701, 2013.

---

mBTSCGCI

*computation of the conditional Granger causality index*


---

**Description**

computation of the conditional Granger causality index

**Usage**

mBTSCGCI(xM, responseindex, pmax)

**Arguments**

xM	the matrix of K time series (variables in columns)
responseindex	the index of the response variable in $\{1, \dots, K\}$
pmax	maximum order(lag) of the VAR model to be considered

**Value**

the matrix of all the conditional Granger causality index across the series of a multivariate set.

**See Also**

Siggiridou, Elsa, and Dimitris Kugiumtzis. "Granger Causality in Multivariate Time Series Using a Time-Ordered Restricted Vector Autoregressive Model." IEEE Transactions on Signal Processing 64, no. 7 (April 2016): 1759-73. doi:[10.1109/TSP.2015.2500893](https://doi.org/10.1109/TSP.2015.2500893)

---

mBTSRGPDC

*Restricted Generalized Partial Directed Coherence*


---

**Description**

partial directed coherence matrix values based on the mBTS algorithm for estimation of the VAR parameters

**Usage**

```
mBTSRGPDC(xM, pmax, freqs)
```

**Arguments**

xM	the matrix of K time series (variables in columns)
pmax	maximum order(lag) of the VAR model to be considered
freqs	frequencies at which the spectral density is estimated

**Value**

the matrix of all the Restricted Generalized Partial Directed Coherence index across the series of a multivariate set. #'

---

mBTS\_Af\_mat

*mBTS Vector Autoregressive coefficients fourier transform*


---

**Description**

DFT Vector Autoregressive coefficients matrix using the mBTS algorithm. This matrix is the base to compute the generalized partial directed coherence

**Usage**

```
mBTS_Af_mat(xM, responseindex, pmax, freqs)
```

**Arguments**

xM	the matrix of K time series (variables in columns)
responseindex	the index of the response variable in $\{1, \dots, K\}$
pmax	maximum order(lag) of the VAR model to be considered
freqs	frequencies at which the spectral density is estimated

**Value**

the matrix of all the Restricted Generalized Partial Directed Coherence index across the series of a multivariate set.

multilagmatrix                      *multilagmatrix*

**Description**

multilagmatrix builds the set of explanatory variables for the dynamic regression model.

**Usage**

multilagmatrix(xM, responseindex, ordersV, indexV)

**Arguments**

- xM                      the matrix of K time series (variables in columns)
- responseindex      the index of the response variable in  $\{1, \dots, K\}$
- ordersV              vector of size 1xK of the maximum order for each of the K variables.
- indexV                the vector of size 1 x K *pmax of zeros and ones e.g. if the component in position 2pmax+3 is one, the third variable, lag 3, X3(t-3), is selected.*

**Value**

the matrix of all explanatory lagged variables in the DR model. The sequence of the lagged variables in 'lagM'

**See Also**

Kugiumtzis, D. "Direct-Coupling Information Measure from Nonuniform Embedding." Physical Review E 87, no. 6 (June 25, 2013): 062918. doi:[10.1103/PhysRevE.87.062918](https://doi.org/10.1103/PhysRevE.87.062918)

PMIME                                      *PMIME Partial mutual information from mixed embedding*

**Description**

computes the measure  $R_{X \rightarrow Y|Z}$  for all combinations of X and Y time series from the multivariate time series given in matrix 'allM', of size  $N \times K$ , where Z contains the rest  $K - 2$  time series. The components of X, Y, and Z, are found from a mixed embedding aiming at explaining Y. The mixed embedding is formed by using the progressive embedding algorithm based on conditional mutual information (CMI). CMI is estimated by the method of nearest neighbors (Kraskov's method). The function is the same as PMIMEsig.m but defines the stopping criterion differently, using a fixed rather than adjusted threshold. Specifically, the algorithm terminates if the contribution of the selected lagged variable in explaining the future response state is small enough, as compared to a threshold 'A'. Concretely, the algorithm terminates if  $I(x^F; w|wemb)/I(x^F; w, wemb) \leq A$  where  $I(x^F; w|wemb)$  is the CMI of the selected lagged variable w and the future response state  $x^F$  given the current mixed embedding vector, and  $I(x^F; w, wemb)$  is the MI between  $x^F$  and the

augmented mixed embedding vector  $wemb, w$ . We experienced that in rare cases the termination condition is not satisfied and the algorithm does not terminate. Therefore we included a second condition for termination of the algorithm when the ratio  $I(x^F; w|wemb)/I(x^F; w, wemb)$  increases in the last two embedding cycles. The derived  $R$  measure indicates the information flow of time series  $X$  to time series  $Y$  conditioned on the rest time series in  $Z$ . The measure values are stored in a  $K \times K$  matrix 'RM' and given to the output, where the value at position  $(i, j)$  indicates the effect from  $i$  to  $j$  (row to col), and the  $(i, i)$  components are zero. The library RANN was used for the nearest neighbor estimation of the mutual information

### Usage

```
PMIME(allM, Lmax = 5, T1 = 1, nnei = 5, A = 0.03, showtxt = 1)
```

### Arguments

allM	the $N \times K$ matrix of the $K$ time series of length $N$ .
Lmax	the maximum delay to search for $X$ and $Y$ components for the mixed embedding vector ,default is 5.
T1	$T1$ steps ahead that the mixed embedding vector has to explain. Note that if $T > 1$ the future vector is of length $T$ and contains the samples at times $t+1, \dots, t+T$ ,default is 1.
nnei	number of nearest neighbors for density estimation ,default is 5
A	the threshold for the ratio of CMI over MI of the lagged variables for the termination criterion.
showtxt	: if 0 or negative do not print out anything, if 1 print out the response variable index at each run, if 2 or larger print also info for each embedding cycle ,default is 1.

### Value

$RM$ : A  $K \times K$  matrix containing the  $R$  values computed by PMIME using the surrogates for setting the stopping criterion.  $ecC$ : cell array of  $K$  components, where each component is a matrix of size  $E \times 5$ , and  $E$  is the number of embedding cycles. For each embedding cycle the following 5 results are stored: 1. variable index, 2. lag index, 3. CMI of the selected lagged variable  $w$  and the future response state  $x^F$  given the current mixed embedding vector,  $I(x^F; w|wemb)$ . 4. MI between  $x^F$  and the augmented mixed embedding vector  $wemb, w$ ,  $I(x^F; w, wemb)$ . 5. The ration of 3. and 4.:  $I(x^F; w|wemb)/I(x^F; w, wemb)$

### See Also

Kugiumtzis, D. "Direct-Coupling Information Measure from Nonuniform Embedding." Physical Review E 87, no. 6 (June 25, 2013): 062918. doi:10.1103/PhysRevE.87.062918

---

sqnorms	<i>Quadratic multiplication of a matrix M with respect to a matrix A: Conj(M) A M, where Conj() is the complex conjugate function</i>
---------	---

---

**Description**

Quadratic multiplication of a matrix M with respect to a matrix A:  $\text{Conj}(M) A M$ , where  $\text{Conj}()$  is the complex conjugate function

**Usage**

```
sqnorms(M, A)
```

**Arguments**

M	A Matrix of dimension P by P
A	A squared Matrix of dimension P by P

**Value**

The squared root of the absolute values of the matrix result of the operation  $\text{Conj}(M) A M$

**Examples**

```
M=matrix( rnorm(100), ncol=10 )  
A=matrix( rnorm(100), ncol=10 )  
sqnorms(M, A)
```

# Index

[all\\_bands](#), [2](#)  
[Anomalyscoresframe](#), [3](#)

[Cort](#), [4](#)

[DEcort](#), [4](#)  
[DEcortNorm](#), [5](#)  
[distance\\_matrix\\_banddepth](#), [6](#)  
[distance\\_matrix\\_CGCI](#), [7](#)  
[distance\\_matrix\\_coherence](#), [8](#)  
[distance\\_matrix\\_cort](#), [9](#)  
[distance\\_matrix\\_cortNorm](#), [10](#)  
[distance\\_matrix\\_dtw](#), [11](#)  
[distance\\_matrix\\_mahalanobis](#), [12](#)  
[distance\\_matrix\\_mvLWS](#), [12](#)  
[distance\\_matrix\\_PDC](#), [13](#)  
[distance\\_matrix\\_PMIME](#), [14](#)  
[distance\\_matrix\\_RGPDC](#), [15](#)  
[distance\\_matrix\\_wasserstein](#), [16](#)  
[DTWcort](#), [16](#)  
[dxy\\_bands](#), [17](#)

[informative\\_bands](#), [18](#)

[kneighbors\\_distance\\_docal1](#), [19](#)

[matrix\\_PDC](#), [20](#)  
[mBTS](#), [20](#)  
[mBTS\\_Af\\_mat](#), [22](#)  
[mBTSCGCI](#), [21](#)  
[mBTSRGPDC](#), [22](#)  
[multilagmatrix](#), [23](#)

[PMIME](#), [23](#)

[sqnorms](#), [25](#)