

Package ‘BLR’

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Title Bayesian Linear Regression

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A *Pedigree info for the wheat dataset*

Description

Is a numerator relationship matrix (599 x 599) computed from a pedigree that traced back many generations. This relationship matrix was derived using the Browse application of the International Crop Information System (ICIS), as described in <http://repository.cimmyt.org/xmlui/bitstream/handle/10883/3488/72673.pdf> (McLaren *et al.* 2005).

Source

International Maize and Wheat Improvement Center (CIMMYT), Mexico.

References

McLaren, C. G., R. Bruskiewich, A.M. Portugal, and A.B. Cosico. 2005. The International Rice Information System. A platform for meta-analysis of rice crop data. *Plant Physiology* **139**: 637-642.

 BLR

Bayesian Linear Regression

Description

The BLR ('Bayesian Linear Regression') function was designed to fit parametric regression models using different types of shrinkage methods. An earlier version of this program was presented in de los Campos *et al.* (2009).

Usage

```
BLR(y, XF, XR, XL, GF, prior, nIter, burnIn, thin, thin2, saveAt,
    minAbsBeta, weights)
```

Arguments

y	(numeric, n) the data-vector (NAs allowed).
XF	(numeric, $n \times pF$) incidence matrix for β_F , may be NULL.
XR	(numeric, $n \times pR$) incidence matrix for β_R , may be NULL.
XL	(numeric, $n \times pL$) incidence matrix for β_L , may be NULL.
GF	(list) providing an \$ID (integer, n) linking observations to groups (e.g., lines or sires) and a (co)variance structure (\$A, numeric, $pU \times pU$) between effects of the grouping factor (e.g., line or sire effects). Note: ID must be an integer taking values from 1 to pU ; ID[i]= q indicates that the i th observation in \mathbf{y} belongs to cluster q whose (co)variance function is in the q th row (column) of \mathbf{A} . GF may be NULL.
weights	(numeric, n) a vector of weights, may be NULL.
nIter, burnIn, thin	(integer) the number of iterations, burn-in and thinning.
saveAt	(string) this may include a path and a pre-fix that will be added to the name of the files that are saved as the program runs.
prior	(list) containing the following elements, <ul style="list-style-type: none"> • prior\$varE, prior\$varBR, prior\$varU: (list) each providing degree of freedom (\$df) and scale (\$S). These are the parameters of the scaled inverse-χ^2 distributions assigned to variance components, see Eq. (2) below. In the parameterization used by BLR() the prior expectation of variance parameters is $S/(df - 2)$.

- `prior$lambda`: (list) providing `$value` (initial value for λ); `$type` ('random' or 'fixed') this argument specifies whether λ should be kept fixed at the value provided by `$value` or updated with samples from the posterior distribution; and, either `$shape` and `$rate` (this when a Gamma prior is desired on λ^2) or `$shape1`, `$shape2` and `$max`, in this case $p(\lambda | \max, \alpha_1, \alpha_2) \propto \text{Beta}\left(\frac{\lambda}{\max} | \alpha_1, \alpha_2\right)$. For detailed description of these priors see de los Campos *et al.* (2009).
- `thin2` This value controls whether the running means are saved to disk or not. If `thin2` is greater than `nIter` the running means are not saved (default, `thin2=1 \times 10^{10}`).
- `minAbsBeta` The minimum absolute value of the components of β_L to avoid numeric problems when sampling from τ^2 , default 1×10^{-9}

Details

The program runs a Gibbs sampler for the Bayesian regression model described below.

Likelihood. The equation for the data is:

$$\mathbf{y} = \mathbf{1}\mu + \mathbf{X}_F\beta_F + \mathbf{X}_R\beta_R + \mathbf{X}_L\beta_L + \mathbf{Z}\mathbf{u} + \boldsymbol{\varepsilon} \quad (1)$$

where \mathbf{y} , the response is a $n \times 1$ vector (NAs allowed); μ is an intercept; \mathbf{X}_F , \mathbf{X}_R , \mathbf{X}_L and \mathbf{Z} are incidence matrices used to accommodate different types of effects (see below), and; $\boldsymbol{\varepsilon}$ is a vector of model residuals assumed to be distributed as $\boldsymbol{\varepsilon} \sim N(\mathbf{0}, \text{Diag}(\sigma_\varepsilon^2/w_i^2))$, here σ_ε^2 is an (unknown) variance parameter and w_i are (known) weights that allow for heterogeneous-residual variances.

Any of the elements in the right-hand side of the linear predictor, except μ and $\boldsymbol{\varepsilon}$, can be omitted; by default the program runs an intercept model.

Prior. The residual variance is assigned a scaled inverse- χ^2 prior with degree of freedom and scale parameter provided by the user, that is, $\sigma_\varepsilon^2 \sim \chi^{-2}(\sigma_\varepsilon^2 | df_\varepsilon, S_\varepsilon)$. The regression coefficients $\{\mu, \beta_F, \beta_R, \beta_L, \mathbf{u}\}$ are assigned priors that yield different type of shrinkage. The intercept and the vector of regression coefficients β_F are assigned flat priors (i.e., estimates are not shrunk). The vector of regression coefficients β_R is assigned a Gaussian prior with variance common to all effects, that is, $\beta_{R,j} \stackrel{iid}{\sim} N(0, \sigma_{\beta_R}^2)$. This prior is the Bayesian counterpart of Ridge Regression. The variance parameter $\sigma_{\beta_R}^2$, is treated as unknown and it is assigned a scaled inverse- χ^2 prior, that is, $\sigma_{\beta_R}^2 \sim \chi^{-2}(\sigma_{\beta_R}^2 | df_{\beta_R}, S_{\beta_R})$ with degrees of freedom df_{β_R} , and scale S_{β_R} provided by the user.

The vector of regression coefficients β_L is treated as in the Bayesian LASSO of Park and Casella (2008). Specifically,

$$p(\beta_L, \tau^2, \lambda | \sigma_\varepsilon^2) = \left\{ \prod_k N(\beta_{L,k} | 0, \sigma_\varepsilon^2 \tau_k^2) \text{Exp}(\tau_k^2 | \lambda^2) \right\} p(\lambda),$$

where, $\text{Exp}(\cdot)$ is an exponential prior and $p(\lambda)$ can either be: (a) a mass-point at some value (i.e., fixed λ); (b) $p(\lambda^2) \sim \text{Gamma}(r, \delta)$ this is the prior suggested by Park and Casella (2008); or, (c) $p(\lambda | \max, \alpha_1, \alpha_2) \propto \text{Beta}\left(\frac{\lambda}{\max} | \alpha_1, \alpha_2\right)$, see de los Campos *et al.* (2009) for details. It can be shown that the marginal prior of regression coefficients $\beta_{L,k}$, $\int N(\beta_{L,k} | 0, \sigma_\varepsilon^2 \tau_k^2) \text{Exp}(\tau_k^2 | \lambda^2) \partial \tau_k^2$, is Double-Exponential. This prior has thicker tails and higher peak of mass at zero than the Gaussian prior used for β_R , inducing a different type of shrinkage.

The vector \mathbf{u} is used to model the so called ‘infinitesimal effects’, and is assigned a prior $\mathbf{u} \sim N(\mathbf{0}, \mathbf{A}\sigma_{\mathbf{u}}^2)$, where, \mathbf{A} is a positive-definite matrix (usually a relationship matrix computed from a pedigree) and $\sigma_{\mathbf{u}}^2$ is an unknown variance, whose prior is $\sigma_{\mathbf{u}}^2 \sim \chi^{-2}(\sigma_{\mathbf{u}}^2 | df_{\mathbf{u}}, S_{\mathbf{u}})$.

Collecting the above mentioned assumptions, the posterior distribution of model unknowns, $\boldsymbol{\theta} = \{\mu, \beta_F, \beta_R, \sigma_{\beta_R}^2, \beta_L, \tau^2, \lambda, \mathbf{u}, \sigma_{\mathbf{u}}^2, \sigma_{\varepsilon}^2\}$, is,

$$\begin{aligned}
 p(\boldsymbol{\theta}|\mathbf{y}) &\propto N\left(\mathbf{y}|\mathbf{1}\mu + \mathbf{X}_F\beta_F + \mathbf{X}_R\beta_R + \mathbf{X}_L\beta_L + \mathbf{Z}\mathbf{u}; \text{Diag}\left\{\frac{\sigma_{\varepsilon}^2}{w_i}\right\}\right) \\
 &\times \left\{ \prod_j N(\beta_{R,j}|0, \sigma_{\beta_R}^2) \right\} \chi^{-2}(\sigma_{\beta_R}^2 | df_{\beta_R}, S_{\beta_R}) \\
 &\times \left\{ \prod_k N(\beta_{L,k}|0, \sigma_{\varepsilon}^2\tau_k^2) \text{Exp}(\tau_k^2|\lambda^2) \right\} p(\lambda) \\
 &\times N(\mathbf{u}|\mathbf{0}, \mathbf{A}\sigma_{\mathbf{u}}^2) \chi^{-2}(\sigma_{\mathbf{u}}^2 | df_{\mathbf{u}}, S_{\mathbf{u}}) \chi^{-2}(\sigma_{\varepsilon}^2 | df_{\varepsilon}, S_{\varepsilon})
 \end{aligned} \tag{2}$$

Value

A list with posterior means, posterior standard deviations, and the parameters used to fit the model:

<code>\$yHat</code>	the posterior mean of $\mathbf{1}\mu + \mathbf{X}_F\beta_F + \mathbf{X}_R\beta_R + \mathbf{X}_L\beta_L + \mathbf{Z}\mathbf{u} + \varepsilon$.
<code>\$SD.yHat</code>	the corresponding posterior standard deviation.
<code>\$mu</code>	the posterior mean of the intercept.
<code>\$varE</code>	the posterior mean of σ_{ε}^2 .
<code>\$bR</code>	the posterior mean of β_R .
<code>\$SD.bR</code>	the corresponding posterior standard deviation.
<code>\$varBr</code>	the posterior mean of $\sigma_{\beta_R}^2$.
<code>\$bL</code>	the posterior mean of β_L .
<code>\$SD.bL</code>	the corresponding posterior standard deviation.
<code>\$tau2</code>	the posterior mean of τ^2 .
<code>\$lambda</code>	the posterior mean of λ .
<code>\$u</code>	the posterior mean of \mathbf{u} .
<code>\$SD.u</code>	the corresponding posterior standard deviation.
<code>\$varU</code>	the posterior mean of $\sigma_{\mathbf{u}}^2$.
<code>\$fit</code>	a list with evaluations of effective number of parameters and DIC (Spiegelhalter <i>et al.</i> , 2002).
<code>\$whichNa</code>	a vector indicating which entries in \mathbf{y} were missing.
<code>\$prior</code>	a list containing the priors used during the analysis.
<code>\$weights</code>	vector of weights.
<code>\$fit</code>	list containing the following elements, <ul style="list-style-type: none"> • <code>\$logLikAtPostMean</code>: log-likelihood evaluated at posterior mean. • <code>\$postMeanLogLik</code>: the posterior mean of the Log-Likelihood. • <code>\$pD</code>: estimated effective number of parameters, Spiegelhalter <i>et al.</i> (2002). • <code>\$DIC</code>: the deviance information criterion, Spiegelhalter <i>et al.</i> (2002).


```

nIter=5500, burnIn=500, thin=1,
saveAt="example_")

MSE.tst<-mean((fm$yHat[whichNa]-y[whichNa])^2)
MSE.tst
MSE.trn<-mean((fm$yHat[-whichNa]-y[-whichNa])^2)
MSE.trn
COR.tst<-cor(fm$yHat[whichNa],y[whichNa])
COR.tst
COR.trn<-cor(fm$yHat[-whichNa],y[-whichNa])
COR.trn

plot(fm$yHat~y,xlab="Phenotype",
      ylab="Pred. Gen. Value" ,cex=.8)
points(x=y[whichNa],y=fm$yHat[whichNa],col=2,cex=.8,pch=19)

x11()
plot(scan('example_varE.dat'),type="o",
      ylab=expression(paste(sigma[epsilon]^2)))
}
#####
#Example 2: Ten fold, Cross validation, environment 1,
#####
if(FALSE){
rm(list=ls())
library(BLR)
data(wheat) #Loads the wheat dataset
nIter<-1500 #For real data sets more samples are needed
burnIn<-500
thin<-10
folds<-10
y<-Y[,1]
priorBL<-list(
  varE=list(df=3,S=2.5),
  varU=list(df=3,S=0.63),
  lambda = list(shape=0.52,rate=1e-5,value=20,type='random')
)

set.seed(123) #Set seed for the random number generator
sets<-rep(1:10,60)[-1]
sets<-sets[order(runif(nrow(A)))]
COR.CV<-rep(NA,times=(folds+1))
names(COR.CV)<-c(paste('fold=',1:folds,sep=''),'Pooled')
w<-rep(1/nrow(A),folds) ## weights for pooled correlations and MSE
yHatCV<-numeric()

for(fold in 1:folds)
{
  yNa<-y
  whichNa<-which(sets==fold)
  yNa[whichNa]<-NA
  prefix<-paste('PM_BL','_fold_',fold,'_',sep='')
  fm<-BLR(y=yNa,XL=X,GF=list(ID=(1:nrow(A)),A=A),prior=priorBL,

```

```

      nIter=nIter, burnIn=burnIn, thin=thin)
    yHatCV[whichNa]<-fm$yHat[fm$whichNa]
    w[fold]<-w[fold]*length(fm$whichNa)
    COR.CV[fold]<-cor(fm$yHat[fm$whichNa],y[whichNa])
  }

COR.CV[11]<-mean(COR.CV[1:10])
COR.CV
}
#####

```

sets

*Sets for cross validation (CV)***Description**

Is a vector (599 x 1) that assigns observations to 10 disjoint sets; the assignment was generated at random. This is used later to conduct a 10-fold CV.

Source

International Maize and Wheat Improvement Center (CIMMYT), Mexico.

wheat

*wheat dataset***Description**

Information from a collection of 599 historical CIMMYT wheat lines. The wheat data set is from CIMMYT's Global Wheat Program. Historically, this program has conducted numerous international trials across a wide variety of wheat-producing environments. The environments represented in these trials were grouped into four basic target sets of environments comprising four main agroclimatic regions previously defined and widely used by CIMMYT's Global Wheat Breeding Program. The phenotypic trait considered here was the average grain yield (GY) of the 599 wheat lines evaluated in each of these four mega-environments.

A pedigree tracing back many generations was available, and the Browse application of the International Crop Information System (ICIS), as described in <http://repository.cimmyt.org/xmlui/bitstream/handle/10883/3488/72673.pdf> (McLaren *et al.* 2005), was used for deriving the relationship matrix A among the 599 lines; it accounts for selection and inbreeding.

Wheat lines were recently genotyped using 1447 Diversity Array Technology (DArT) generated by Tritcarte Pty. Ltd. (Canberra, Australia). The DArT markers may take on two values, denoted by their presence or absence. Markers with a minor allele frequency lower than 0.05 were removed, and missing genotypes were imputed with samples from the marginal distribution of marker genotypes, that is, $x_{ij} = \text{Bernoulli}(\hat{p}_j)$, where \hat{p}_j is the estimated allele frequency computed from the non-missing genotypes. The number of DArT MMs after edition was 1279.

Usage

data(wheat)

Format

Matrix Y contains the average grain yield, column 1: Grain yield for environment 1 and so on. The matrix A contains additive relationship computed from the pedigree and matrix X contains the markers information.

Source

International Maize and Wheat Improvement Center (CIMMYT), Mexico.

References

McLaren, C. G., R. Bruskiewich, A.M. Portugal, and A.B. Cosico. 2005. The International Rice Information System. A platform for meta-analysis of rice crop data. *Plant Physiology* **139**: 637-642.

X *Molecular markers*

Description

Is a matrix (599 x 1279) with DArT genotypes; data are from pure lines and genotypes were coded as 0/1 denoting the absence/presence of the DArT. Markers with a minor allele frequency lower than 0.05 were removed, and missing genotypes were imputed with samples from the marginal distribution of marker genotypes, that is, $x_{ij} = \text{Bernoulli}(\hat{p}_j)$, where \hat{p}_j is the estimated allele frequency computed from the non-missing genotypes. The number of DArT MMs after edition was 1279.

Source

International Maize and Wheat Improvement Center (CIMMYT), Mexico.

Y *Grain yield*

Description

A matrix (599 x 4) containing the 2-yr average grain yield of each of these lines in each of the four environments (phenotypes were standardized to a unit variance within each environment).

Source

International Maize and Wheat Improvement Center (CIMMYT), Mexico.

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