

# Package ‘BootPR’

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**Type** Package

**Title** Bootstrap Prediction Intervals and Bias-Corrected Forecasting

**Version** 1.0

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**Author** Jae. H. Kim <jaekim8080@gmail.com>

**Maintainer** Jae H. Kim <jaekim8080@gmail.com>

**Description** Contains functions for bias-Corrected Forecasting and Bootstrap Prediction Intervals for Autoregressive Time Series.

**License** GPL-2

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BootPR-package

*Bootstrap Prediction Intervals and Bias-Corrected Forecasting*

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### Description

The package provides alternative bias-correction methods for univariate autoregressive model parameters; and generate point forecasts and prediction intervals for economic time series.

A future version will include the case of vector AR models.

### Details

Package: BootPR  
Type: Package  
Version: 1.0  
Date: 2023-08-31  
License: GPL version 2 or newer

### Author(s)

Jae H. Kim

Maintainer: Jae H. Kim <J.Kim@latrobe.edu.au>

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Andrews.Chen

*Andrews-Chen median-unbiased estimation for AR models*

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### Description

This function returns the Andrews-Chen estimates for AR coefficients, residuals, and AR forecasts generated using the Andrews-Chen estimates

### Usage

```
Andrews.Chen(x, p, h, type)
```

### Arguments

x	a time series data set
p	AR order
h	the number of forecast periods
type	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend

**Value**

coef	Andrews-Chen median-unbiased estimates
ecm.coef	the coefficients in the ADF form
resid	residuals
forecast	point forecasts from Andrews-Chen estimates

**Note**

The Andrew-Chen estimator may break down when the AR order is very high. I recommend that AR order be kept low

**Author(s)**

Jae H. Kim

**References**

Kim, J.H., 2003, Forecasting Autoregressive Time Series with Bias-Corrected Parameter Estimators, *International Journal of Forecasting*, 19, 493-502.

Andrews, D.W. K. (1993). Exactly median-unbiased estimation of first order autoregressive / unit root models. *Econometrica*, 61, 139-165.

Andrews, D.W. K., & Chen, H. -Y. (1994). Approximate median unbiased estimation of autoregressive models. *Journal of Business & Economic Statistics*, 12, 187-204.

**Examples**

```
data(IPdata)
BootBC(IPdata,p=1,h=10,nboot=200,type="const+trend")
```

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ARorder	<i>AR model order selection</i>
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**Description**

AR model selection using AIC, BIC, HQ

**Usage**

```
ARorder(x, pmax, type)
```

**Arguments**

x	a time series data set
pmax	the maximum AR order
type	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend

**Value**

ARorder	AR orders selected by AIC, BIC and HQ
Criteria	the values of AIC, BIC and HQ

**Author(s)**

Jae H. Kim

**Examples**

```
data(IPdata)
ARorder(IPdata, pmax=12, type="const+trend")
```

---

BootAfterBootPI

*Bootstrap-after-Bootstrap Prediction*

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**Description**

This function calculates bootstrap-after-bootstrap prediction intervals and bootstrap bias-corrected point forecasts

**Usage**

```
BootAfterBootPI(x, p, h, nboot, prob, type)
```

**Arguments**

x	a time series data set
p	AR order
h	the number of forecast periods
nboot	number of bootstrap iterations
prob	a vector of probabilities
type	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend

**Value**

PI	prediction intervals
forecast	bias-corrected point forecasts

**Author(s)**

Jae H. Kim

**References**

- Kim, J.H., 2001, Bootstrap-after-Bootstrap Prediction Intervals for Autoregressive Models, *Journal of Business & Economic Statistics* 19, 117-128
- Kilian, L. (1998). Small sample confidence intervals for impulse response functions. *The Review of Economics and Statistics*, 80,218-230.

**Examples**

```
data(IPdata)
BootAfterBootPI(IPdata,p=1,h=10,nboot=100,prob=c(0.05,0.95),type="const+trend")
```

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BootBC	<i>Bootstrap bias-corrected estimation and forecasting for AR models</i>
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**Description**

This function returns bias-corrected parameter estimates and forecasts for univariate AR models.

**Usage**

```
BootBC(x, p, h, nboot, type)
```

**Arguments**

x	a time series data set
p	AR order
h	the number of forecast period
nboot	number of bootstrap iterations
type	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend

**Value**

coef	Bootstrap bias-corrected parameter estimates
resid	residuals
forecast	point forecasts from bootstrap bias-corrected parameter estimates

**Author(s)**

Jae H. Kim

**References**

- Kim, J.H., 2003, Forecasting Autoregressive Time Series with Bias-Corrected Parameter Estimators, *International Journal of Forecasting*, 19, 493-502.
- Kilian, L. (1998a). Small sample confidence intervals for impulse response functions. *The Review of Economics and Statistics*, 80,218-230.

**Examples**

```
data(IPdata)
BootBC(IPdata,p=1,h=10,nboot=100,type="const+trend")
```

---

BootPI	<i>Bootstrap prediction intervals and point forecasts with no bias-correction</i>
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---

**Description**

This function returns bootstrap forecasts and prediction intervals with no bias-correction

**Usage**

```
BootPI(x, p, h, nboot, prob, type)
```

**Arguments**

x	a time series data set
p	AR order
h	the number of forecast periods
nboot	number of bootstrap iterations
prob	a vector of probabilities
type	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend

**Value**

PI	prediction intervals
forecast	bias-corrected point forecasts

**Author(s)**

Jae H. Kim

**References**

Thombs, L. A., & Schucany, W. R. (1990). Bootstrap prediction intervals for autoregression. *Journal of the American Statistical Association*, 85, 486-492.

**Examples**

```
data(IPdata)
BootPI(IPdata,p=1,h=10,nboot=100,prob=c(0.05,0.95),type="const+trend")
```

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IPdata	<i>US industrial production data</i>
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**Description**

From Extended Nelson-Plosser data set, annual, 1860-1988

**Usage**

```
data(IPdata)
```

**References**

Andrews, D.W. K., & Chen, H. -Y. (1994). Approximate median-unbiased estimation of autoregressive models. *Journal of Business & Economic Statistics*, 12, 187-204.

**Examples**

```
data(IPdata)
```

---

LS.AR	<i>OLS parameter estimates and forecasts, no bias-correction</i>
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**Description**

The function returns parameter estimates and forecasts from OLS estimation for AR models

**Usage**

```
LS.AR(x, p, h, type, prob)
```

**Arguments**

x	a time series data set
p	AR order
h	the number of forecast period
prob	a vector of probabilities
type	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend

**Value**

coef	OLS parameter estimates
resid	OLS residuals
forecast	point forecasts from OLS parameter estimates
PI	Prediction Intervals based on OLS parameter estimates based on normal approximation

**Author(s)**

Jae H. Kim

**Examples**

```
data(IPdata)
LS.AR(IPdata,p=6,h=10,type="const+trend", prob=c(0.05,0.95))
```

---

Plot.Fore	<i>Plotting point forecasts</i>
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**Description**

The function returns plots the point forecasts

**Usage**

```
Plot.Fore(x, fore, start, end, frequency)
```

**Arguments**

x	a time series data set
fore	point forecasts
start	starting date
end	ending date
frequency	data frequency

**Details**

frequency=1 for annual data, 4 for quarterly data, 12 for monthly data

start=c(1980,4) indicates April 1980 if frequency=12

end = c(2000,1) indicates 1st quarter of 2000 if frequency = 4

**Value**

plot

**Author(s)**

Jae H. Kim

**Examples**

```
data(IPdata)
BootF <- BootBC(IPdata,p=1,h=10,nboot=100,type="const+trend")
Plot.Fore(IPdata,BootF$forecast,start=1860,end=1988,frequency=1)
```

---

`Plot.PI`*Plotting prediction intervals and point forecasts*

---

**Description**

The function returns plots the point forecasts and prediction intervals

**Usage**

```
Plot.PI(x, fore, Interval, start, end, frequency)
```

**Arguments**

<code>x</code>	a time series data set
<code>fore</code>	point forecasts
<code>Interval</code>	Prediction Intervals
<code>start</code>	starting date
<code>end</code>	ending date
<code>frequency</code>	data frequency

**Details**

`frequency=1` for annual data, 4 for quarterly data, 12 for monthly data  
`start=c(1980,4)` indicates April 1980 if `frequency=12`  
`end = c(2000,1)` indicates 1st quarter of 2000 if `frequency = 4`

**Value**

plot

**Author(s)**

Jae H. Kim

**Examples**

```
data(IPdata)
PI <- ShamanStine.PI(IPdata,p=1,h=10,nboot=100,prob=c(0.025,0.05,0.95,0.975),type="const+trend",0)
Plot.PI(IPdata,PI$forecast,PI$PI,start=1860,end=1988,frequency=1)
```

---

`Roy.Fuller`*Roy-Fuller median-unbiased estimation*

---

**Description**

This function returns parameter estimates and forecasts based on Roy-Fuller median-unbiased estimator for AR models

**Usage**

```
Roy.Fuller(x, p, h, type)
```

**Arguments**

<code>x</code>	a time series data set
<code>p</code>	AR order
<code>h</code>	the number of forecast period
<code>type</code>	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend

**Value**

<code>coef</code>	Roy-Fuller parameter estimates
<code>resid</code>	residuals
<code>forecast</code>	point forecasts from Roy-Fuller parameter estimates

**Author(s)**

Jae H. Kim

**References**

Kim, J.H., 2003, Forecasting Autoregressive Time Series with Bias-Corrected Parameter Estimators, *International Journal of Forecasting*, 19, 493-502.

Roy, A., & Fuller, W. A. (2001). Estimation for autoregressive time series with a root near one. *Journal of Business & Economic Statistics*, 19(4), 482-493.

**Examples**

```
data(IPdata)
Roy.Fuller(IPdata, p=6, h=10, type="const+trend")
```

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ShamanStine.PI                      *Bootstrap prediction interval using Shaman and Stine bias formula*

---

### Description

The function returns bias-corrected forecasts and bootstrap prediction intervals using Shaman and Stine bias formula for univariate AR models

### Usage

```
ShamanStine.PI(x, p, h, nboot, prob, type, pmax)
```

### Arguments

x	a time series data set
p	AR order
h	the number of forecast periods
nboot	number of bootstrap iterations
prob	a vector of probability values
type	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend
pmax	for exogenous lag order algorithm, pmax = 0, for endogenous lag order algorithm, pmax is an integer greater than 0

### Value

PI	prediction intervals
forecast	bias-corrected point forecasts

### Author(s)

Jae H. Kim

### References

- Kim, J.H., 2004, Bootstrap Prediction Intervals for Autoregression using Asymptotically Mean-Unbiased Parameter Estimators, *International Journal of Forecasting*, 20, 85-97.
- Kim, J.H., 2003, Forecasting Autoregressive Time Series with Bias-Corrected Parameter Estimators, *International Journal of Forecasting*, 19, 493-502.
- Shaman, P., & Stine, R. A. (1988). The bias of autoregressive coefficient estimators. *Journal of the American Statistical Association*, 83, 842-848.
- Stine, R. A., & Shaman, P. (1989). A fixed point characterization for bias of autoregressive estimators. *The Annals of Statistics*, 17, 1275-1284.
- Kilian, L. (1998a). Small sample confidence intervals for impulse response functions. *The Review of Economics and Statistics*, 80, 218-230.

**Examples**

```
data(IPdata)
ShamanStine.PI(IPdata,p=1,h=10,nboot=100,prob=c(0.05,0.95),type="const+trend",pmax=0)
```

---

 Stine.Shaman

*bias-corrected estimation based on Shaman-Stine formula*


---

**Description**

The function returns parameter estimates and bias-corrected forecasts using Shaman and Stine bias formula for univariate AR models

**Usage**

```
Stine.Shaman(x, p, h, type)
```

**Arguments**

x	a time series data set
p	AR order
h	the number of forecast period
type	"const" for the AR model with intercept only, "const+trend" for the AR model with intercept and trend

**Value**

coef	Bias-corrected parameter estimates using Shama-Stine formula
resid	residuals
forecast	point forecasts from bias-corrected parameter estimates

**Author(s)**

Jae H. Kim

**References**

Kim, J.H., 2003, Forecasting Autoregressive Time Series with Bias-Corrected Parameter Estimators, *International Journal of Forecasting*, 19, 493-502.

Shaman, P., & Stine, R. A. (1988). The bias of autoregressive coefficient estimators. *Journal of the American Statistical Association*, 83, 842-848.

Stine, R. A., & Shaman, P. (1989). A fixed point characterization for bias of autoregressive estimators. *The Annals of Statistics*, 17, 1275-1284.

Kilian, L. (1998a). Small sample confidence intervals for impulse response functions. *The Review of Economics and Statistics*, 80, 218-230.

**Examples**

```
data(IPdata)  
Stine.Shaman(IPdata,p=6,h=10,type="const+trend")
```

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