

# Package ‘CIAAWconsensus’

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**Type** Package

**Title** Isotope Ratio Meta-Analysis

**Version** 1.3

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**Description** Calculation of consensus values for atomic weights, isotope amount ratios, and isotopic abundances with the associated uncertainties using multivariate meta-regression approach for consensus building.

**License** Unlimited

**LazyData** yes

**Imports** mvtnorm, stringr, numDeriv, stats, Matrix

**NeedsCompilation** no

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abundances2ratios      *Isotope ratios of a chemical element from isotopic abundances*

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### Description

This function calculates the isotope ratios of a chemical element from the given isotopic abundances and their uncertainties. The uncertainty evaluation is done using the propagation of uncertainty and the missing correlations between the isotopic abundances are reconstructed using Monte Carlo methods.

### Usage

```
abundances2ratios(x, ux, ref=1, iterations=1e4)
```

### Arguments

x	A vector of isotopic abundances of an element
ux	Standard uncertainties of x
ref	Index to specify the desired reference isotope for isotope amount ratios
iterations	Number of iterations for isotopic abundance correlation mapping

### Details

Situations are often encountered where isotopic abundances are reported but not the isotope ratios. In such cases we reconstruct the isotope ratios that are consistent with the abundances and their uncertainties. Given only the abundances and their uncertainties, for elements with four or more isotopes one cannot unambiguously infer the uncertainties of the ratios due to the unknown correlations between isotopic abundances. This missing information can be reconstructed by mapping all possible correlations between isotopic abundances.

### Value

R	Isotope ratio vector, excluding the trivial ratio
R.u	Standard uncertainties of the isotope ratios
R.cov	Isotope ratio covariance matrix
N	Number of successful Monte Carlo iterations

### Author(s)

Juris Meija <juris.meija@nrc-cnrc.gc.ca> and Antonio Possolo

## References

J. Meija and Z. Mester (2008) **Atomic weight uncertainty calculation from isotopic composition of the elements**. *Metrologia*, 45, 459

J. Meija and A. Possolo (2017) **Data reduction framework for standard atomic weights and isotopic compositions of the elements**. *Metrologia*, 54, 229-238

JCGM 101:2008 Evaluation of measurement data - Supplement 1 to the "Guide to the expression of uncertainty in measurement" - Propagation of distributions using a Monte Carlo method

## Examples

```
## Isotope ratios of zinc from the isotopic abundances
x = c(0.48630, 0.27900, 0.04100, 0.18750, 0.00620)
ux = c(0.00091, 0.00076, 0.00031, 0.00135, 0.00010)
abundances2ratios(x,ux,ref=2)

## The corresponding atomic weight can be obtained using at.weight(z$R,z$cov,"zinc","66Zn")
```

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at.weight	<i>Atomic weight and isotopic abundances of a chemical element from isotope ratios</i>
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## Description

This function calculates the isotopic abundances and the atomic weight of a chemical element from the given isotope amount ratios and their uncertainties. The uncertainty evaluation is done using the Monte Carlo method and the relevant masses of the isotopes are extracted from the [www.ciaaw.org](http://www.ciaaw.org).

## Usage

```
at.weight(ratio, ratio.cov, element, ref.isotope, data=NULL)
```

## Arguments

ratio	A vector of nontrivial isotope amount ratios of an element
ratio.cov	A covariance matrix of ratio
element	A string consisting of the lowercase English name of the element. For example, "zinc"
ref.isotope	A string which specifies the reference isotope. For example, "64Zn"
data	Nuclide mass dataframe. Default dataframe is <code>ciaaw.mass.2016</code>

## Details

The isotopic composition of an element with N isotopes is characterized using a set of N-1 nontrivial isotope amount ratios. As an example, silicon has three stable isotopes (silicon-28, silicon-29, and silicon-30) and its isotope ratios can be reported against either of its stable isotopes in three distinct ways: (1)  $^{29}\text{Si}/^{28}\text{Si}$  and  $^{30}\text{Si}/^{28}\text{Si}$  or (2)  $^{28}\text{Si}/^{29}\text{Si}$  and  $^{30}\text{Si}/^{29}\text{Si}$ , or (3)  $^{28}\text{Si}/^{30}\text{Si}$  and  $^{29}\text{Si}/^{30}\text{Si}$ .

**Value**

aw	Atomic weight
aw.u	Standard uncertainty of the atomic weight
aw.U95	Expanded uncertainty of the atomic weight corresponding to 95% confidence
abundances	Isotopic abundances
abundances.u	Standard uncertainty of the isotopic abundances
abundances.U95	Expanded uncertainty of the isotopic abundances corresponding to 95% confidence
abundances.cov	Covariance matrix of the isotopic abundances

**Author(s)**

Juris Meija <juris.meija@nrc-cnrc.gc.ca> and Antonio Possolo

**References**

- J.Meija and Z. Mester (2008) **Uncertainty propagation of atomic weight measurement results**. *Metrologia*, 45, 53-62
- J. Meija and A. Possolo (2017) **Data reduction framework for standard atomic weights and isotopic compositions of the elements**. *Metrologia*, 54, 229-238
- JCGM 101:2008 Evaluation of measurement data - Supplement 1 to the "Guide to the expression of uncertainty in measurement" - Propagation of distributions using a Monte Carlo method

**Examples**

```
## Atomic weight and isotopic abundances of iridium which correspond
## to the isotope ratio 191Ir/193Ir = 0.59471(13)
at.weight(0.59471, matrix(0.00013^2), "iridium", "193Ir")

## Atomic weight and isotopic abundances of silicon which correspond
## to isotope ratios 28Si/29Si = 1.074(69) and 30Si/29Si = 260(11)
## with a correlation of 0.80 between the two isotope ratios
ratios = c(1.074,260)
r.cov = matrix(c(0.069^2,0.80*0.069*11,0.80*0.069*11,11^2),ncol=2,byrow=TRUE)
at.weight(ratios, r.cov, "silicon", "29Si")
```

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ciaaw.mass.2003

*Atomic masses of isotopes (IUPAC/CIAAW 2003)*

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**Description**

This data set gives the atomic masses and uncertainties of all polyisotopic nuclides as they are used by the IUPAC/CIAAW.

**Usage**

ciaaw.mass.2003

**Format**

A data frame with 268 rows and 4 variables:

- isotope: Symbol of the isotope
- element: Name of the element (lowercase english)
- mass: Atomic mass of the isotope in daltons
- uncertainty: Uncertainty of the atomic mass of the isotope as used by the IUPAC-CIAAW

**Source**

AME2003, <http://www.ciaaw.org/>

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ciaaw.mass.2012

*Atomic masses of isotopes (IUPAC/CIAAW 2012)*

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**Description**

This data set gives the atomic masses and uncertainties of all polyisotopic nuclides as they are used by the IUPAC/CIAAW.

**Usage**

ciaaw.mass.2012

**Format**

A data frame with 268 rows and 4 variables:

- isotope: Symbol of the isotope
- element: Name of the element (lowercase english)
- mass: Atomic mass of the isotope in daltons
- uncertainty: Uncertainty of the atomic mass of the isotope as used by the IUPAC-CIAAW

**Source**

AME2012 <https://doi.org/10.1088/1674-1137/41/3/030003>, <http://www.ciaaw.org/>

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ciaaw.mass.2016      *Atomic masses of isotopes (IUPAC/CIAAW 2016)*

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**Description**

This data set gives the atomic masses and uncertainties of all polyisotopic nuclides as they are used by the IUPAC/CIAAW.

**Usage**

ciaaw.mass.2016

**Format**

A data frame with 268 rows and 4 variables:

- isotope: Symbol of the isotope
- element: Name of the element (lowercase english)
- mass: Atomic mass of the isotope in daltons
- uncertainty: Uncertainty of the atomic mass of the isotope as used by the IUPAC-CIAAW

**Source**

AME2016 <https://doi.org/10.1088/1674-1137/41/3/030003>, <http://www.ciaaw.org/>

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iridium.data      *Iridium isotope ratio data from various studies*

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**Description**

This data set gives the iridium isotope ratios as reported by various studies. These data are used by the IUPAC/CIAAW to determine the standard atomic weight of iridium.

**Usage**

iridium.data

**Format**

A data frame.

**Source**

IUPAC/CIAAW 2018

**Description**

This function provides meta-analysis of multivariate correlated data using the marginal method of moments with working independence assumption as described by Chen et al (2016). As such, the meta-analysis does not require correlations between the outcomes within each dataset.

**Usage**

```
mmm(y, uy, knha = TRUE, verbose = TRUE)
```

**Arguments**

y	A matrix of results from each of the n laboratories (rows) where each study reports m isotope ratios (columns)
uy	A matrix with uncertainties of the results given in y
knha	(Logical) Allows for the adjustment of consensus uncertainties using the Birge ratio (Knapp-Hartung adjustment)
verbose	(Logical) Requests annotated summary output of the results

**Details**

The marginal method of moments delivers the inference for correlated effect sizes using multiple univariate meta-analyses.

**Value**

studies	The number of independent studies
beta	The consensus estimates for all outcomes
beta.u	Standard uncertainties of the consensus estimates
beta.U95	Expanded uncertainties of the consensus estimates corresponding to 95% confidence
beta.cov	Covariance matrix of the consensus estimates
beta.cor	Correlation matrix of the consensus estimates
H	Birge ratios (Knapp-Hartung adjustment) which were applied to adjust the standard uncertainties of each consensus outcome
I2	Relative total variability due to heterogeneity (in percent) for each outcome

**Author(s)**

Juris Meija <juris.meija@nrc-cnrc.gc.ca> and Antonio Possolo

## References

- Y. Chen, Y. Cai, C. Hong, and D. Jackson (2016) [Inference for correlated effect sizes using multiple univariate meta-analyses](#). *Statistics in Medicine*, 35, 1405-1422
- J. Meija and A. Possolo (2017) [Data reduction framework for standard atomic weights and isotopic compositions of the elements](#). *Metrologia*, 54, 229-238

## Examples

```
## Consensus isotope amount ratios for platinum
df=normalize.ratios(platinum.data, "platinum", "195Pt")
mmm(df$R, df$u.R)
```

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normalize.ratios	<i>Normalize isotope amount ratios to a common reference isotope</i>
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## Description

This function converts the isotope amount ratios of an element from various studies to a single common reference isotope so that all isotope ratios can be directly compared to one another. The conversion involves a direct application of the law of propagation of uncertainty and this function discards the possible covariances between the isotope ratios.

## Usage

```
normalize.ratios(dat, element, ref.isotope, expand = FALSE)
```

## Arguments

dat	A data frame of results from each study where each study reports one or more isotope ratios (outcomes). The data frame must include the following named columns: Study, Year, Author, Outcome, Value, Unc, k_extra (see Details).
element	Lowercase english name of the element, e.g., "antimony"
ref.isotope	Desired reference isotope, e.g., "121Sb"
expand	(Logical) Specification of whether or not to expand the isotope ratio uncertainties using the values of dat\$k_extra

## Details

The isotope ratio vector  $R$  is transformed to the reference isotope  $R_{ref}$  by dividing each element of the set to the chosen reference isotope. The covariances of the transformed isotope ratios are obtained using the Law of Propagation of Uncertainty. This function assumes all isotope ratios reported by a given study as uncorrelated. While this is not strictly true in practice, such assumption is made largely because of the lack of reported correlations in the literature.

The format of dat data frame for a simple dataset is as follows:

Study	Year	Author	Outcome	Value	Unc	k_extra
1	1954	Howard	191Ir/193Ir	0.5949	0.0025	9
2	1991	Creaser	191Ir/193Ir	0.5948	0.0001	9
3	1992	Chang	191Ir/193Ir	0.59399	0.00103	6
4	1993	Walczyk	191Ir/193Ir	0.59418	0.00037	9
5	2017	Zhu	191Ir/193Ir	0.59290	0.00021	6

### Value

R	A list of the normalized isotope amount ratios
u.R	A list of standard uncertainties for R
cov.R	A list of covariance matrices for R (forced to zero covariances)

### Author(s)

Juris Meija <juris.meija@nrc-cnrc.gc.ca> and Antonio Possolo

### References

- J. Meija and Z. Mester (2008) [Uncertainty propagation of atomic weight measurement results](#). *Metrologia*, 45, 53-62
- J. Meija and A. Possolo (2017) [Data reduction framework for standard atomic weights and isotopic compositions of the elements](#). *Metrologia*, 54, 229-238

### Examples

```
## Normalize all platinum isotope data to platinum-195
normalize.ratios(platinum.data, "platinum", "195Pt")
```

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platinum.data	<i>Platinum isotope ratio data from various studies</i>
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### Description

This data set gives the platinum isotope ratios as reported by various studies. These data are used by the IUPAC/CIAAW to determine the standard atomic weight of platinum.

### Usage

```
platinum.data
```

### Format

A data frame.

### Source

IUPAC/CIAAW 2016

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