Package 'DiscreteDists'

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Title Discrete Statistical Distributions

Version 1.1.2

Description Implementation of new discrete statistical distributions. Each distribution includes the traditional functions as well as an additional function called the family function, which can be used to estimate parameters within the 'gamlss' framework.

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Imports gamlss, gamlss.dist, pracma, Rcpp, COMPoissonReg, nleqslv

LinkingTo Rcpp

Encoding UTF-8

RoxygenNote 7.3.2

Suggests knitr, rmarkdown

URL https://github.com/fhernanb/DiscreteDists

BugReports https://github.com/fhernanb/DiscreteDists/issues

Depends R (>= 4.1)

LazyData true

NeedsCompilation yes

Author Freddy Hernandez-Barajas [aut, cre] (ORCID: <https://orcid.org/0000-0001-7459-3329>), Fernando Marmolejo-Ramos [aut] (ORCID: <https://orcid.org/0000-0003-4680-1287>), Olga Usuga-Manco [aut] (ORCID: <https://orcid.org/0000-0003-3062-1820>), Jamiu Olumoh [aut] (ORCID: <https://orcid.org/0000-0002-7371-3920>), Osho Ajayi [aut]

Maintainer Freddy Hernandez-Barajas <fhernanb@unal.edu.co>

Repository CRAN

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Contents

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add *Sum of One-Dimensional Functions*

Description

Sum of One-Dimensional Functions

Usage

```
add(f, lower, upper, ..., abs.tol = .Machine$double.eps)
```

Arguments

f	an R function taking a numeric first argument and returning a numeric vector of the same length.
lower	the lower limit of sum. Can be infinite.
upper	the upper limit of sum. Can be infinite.
...	additional arguments to be passed to f.
abs.tol	absolute accuracy requested.

Value

This function returns the sum value.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

Examples

```
# Poisson expected value
add(f=function(x, lambda) x*dpois(x, lambda), lower=0, upper=Inf,
    lambda=7.5)

# Binomial expected value
add(f=function(x, size, prob) x*dbinom(x, size, prob), lower=0, upper=20,
    size=20, prob=0.5)

# Examples with infinite series
add(f=function(x) 0.5^x, lower=0, upper=100) # Ans=2
add(f=function(x) (1/3)^(x-1), lower=1, upper=Inf) # Ans=1.5
add(f=function(x) 4/(x^2+3*x+2), lower=0, upper=Inf, abs.tol=0.001) # Ans=4.0
add(f=function(x) 1/(x*(log(x)^2)), lower=2, upper=Inf, abs.tol=0.000001) # Ans=2.02
add(f=function(x) 3*0.7^(x-1), lower=1, upper=Inf) # Ans=10
add(f=function(x, a, b) a*b^(x-1), lower=1, upper=Inf, a=3, b=0.7) # Ans=10
add(f=function(x, a=3, b=0.7) a*b^(x-1), lower=1, upper=Inf) # Ans=10
```

BerG *The Bernoulli-geometric distribution*

Description

The function `BerG()` defines the Bernoulli-geometric distribution, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BerG(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The BerG distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \frac{(1-\mu+\sigma)}{(1+\mu+\sigma)}$ if $x = 0$,

$f(x|\mu,\sigma) = 4\mu\frac{(\mu+\sigma-1)^{x-1}}{(\mu+\sigma+1)^{x+1}}$ if $x = 1, 2, ...,$

with $\mu > 0$, $\sigma > 0$ and $\sigma > |\mu - 1|$.

Value

Returns a `gamlss.family` object which can be used to fit a BerG distribution in the `gamlss()` function.

Author(s)

Hermes Marques, <hermes.marques@ufrn.br>

References

Bourguignon, M., & de Medeiros, R. M. (2022). A simple and useful regression model for fitting count data. Test, 31(3), 790-827.

See Also

dBerG.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rBerG(n=500, mu=0.75, sigma=0.5)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, family=BerG,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu and sigma
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ BerG
```

```
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  x3 <- runif(n)
  x4 <- runif(n)
  mu    <- exp(1 + 1.2*x1 + 0.2*x2)
  sigma <- exp(2 + 1.5*x3 + 1.5*x4)
  y <- rBerG(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2, x3=x3, x4=x4)
}

set.seed(16494786)
datos <- gendat(n=500)

mod2 <- gamlss(y~x1+x2, sigma.fo=~x3+x4, family=BerG, data=datos,
               control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)

# Example using the dataset grazing from the bergreg package
# https://github.com/rdmatheus/bergreg

# This example corresponds to example 5.1
# presented by Bourguignon & Medeiros (2022)
# A simple and useful regression model for fitting count data

data("grazing")
hist(grazing$birds)

mod3 <- gamlss(birds ~ when + grazed,
               sigma.fo=~1,
               family=BerG, data=grazing,
               control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod3)
```

COMPO *The COMPO family*

Description

The function `COMPO()` defines the Conway-Maxwell-Poisson distribution, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
COMPO(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The COMPO distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \frac{\mu^x}{(x!)^\sigma Z(\mu,\sigma)}$

with $\mu > 0$, $\sigma \geq 0$ and

$Z(\mu,\sigma) = \sum_{j=0}^{\infty} \frac{\mu^j}{(j!)^\sigma}$.

The proposed functions here are based on the functions from the COMPoissonReg package.

Value

Returns a `gamlss.family` object which can be used to fit a COMPO distribution in the `gamlss()` function.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Shmueli, G., Minka, T. P., Kadane, J. B., Borle, S., & Boatwright, P. (2005). A useful distribution for fitting discrete data: revival of the Conway–Maxwell–Poisson distribution. Journal of the Royal Statistical Society Series C: Applied Statistics, 54(1), 127-142.

See Also

dCOMPO.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
## Not run:
set.seed(12)
y <- rCOMPO(n=100, mu=10, sigma=3)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=COMPO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
```

```
exp(coef(mod1, what="sigma"))

## End(Not run)

# Example 2
# Generating random values under some model

## Not run:
# A function to simulate a data set with Y ~ COMPO
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(2 + 1 * x1) # 12 approximately
  sigma <- exp(2 - 2 * x2) # 2.71 approximately
  y <- rCOMPO(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=100)

# Fitting the model
mod2 <- NULL
mod2 <- gamlss(y~x1, sigma.fo=~x2, family=COMPO, data=dat,
               control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)

## End(Not run)

# Example 3
# Using the data from Shmueli et al. (2005) page 134
# The dataset consists of quarterly sales of a well-known brand of a
# particular article of clothing at stores of a large national retailer.
## Not run:
values <- 0:30
freq <- c(514, 503, 457, 423, 326, 233, 195, 139, 101, 77, 56, 40,
          37, 22, 9, 7, 10, 9, 3, 2, 2, 2, 0, 0, 0, 0, 0, 0, 0, 0, 1)

y <- rep(x=values, times=freq)

mod3 <- gamlss(y~1, sigma.fo=~1, family=COMPO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

estim_mu_sigma_COMPO(y)

library(COMPoissonReg)
fit <- glm.cmp(y ~ 1)
res <- exp(fit$opt.res$par)
res
```

```
## End(Not run)

# Example 4
# Using the data from Shmueli et al. (2005) page 134
# The dataset contains lengths of words (numbers of syllables)
# in a Hungarian dictionary

## Not run:
# Slovak dictionary
y <- rep(x=1:5, times=c(7, 33, 49, 22, 6))

# Hungarian dictionary
y <- rep(x=1:9, times=c(1421, 12333, 20711, 15590, 5544, 1510, 289, 60, 1))

mod4 <- gamlss(y~1, sigma.fo=~1, family=COMPO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

exp(coef(mod4, what="mu"))
exp(coef(mod4, what="sigma"))

estim_mu_sigma_COMPO(y)

library(COMPoissonReg)
fit <- glm.cmp(y ~ 1)
res <- exp(fit$opt.res$par)
res


## End(Not run)
```

COMPO2 *The COMPO2 family (with mu as mean)*

Description

The function `COMPO2()` defines the Conway-Maxwell-Poisson distribution a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`. This parameterization was proposed by Ribeiro et al. (2020) and the main characteristic is that $E(X) = \mu$.

Usage

```
COMPO2(mu.link = "log", sigma.link = "identity")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "identity" link as the default for the sigma.

Details

The COMPO2 distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \left(\mu + \frac{\exp(\sigma)-1}{2\exp(\sigma)}\right)^{x\exp(\sigma)} \frac{(x!)^{\exp(\sigma)}}{Z(\mu,\sigma)}$

with $\mu > 0$, $\sigma \in \Re$ and

$Z(\mu,\sigma) = \sum_{j=0}^{\infty} \frac{\mu^j}{(j!)^\sigma}$.

The proposed functions here are based on the functions from the COMPoissonReg package.

Value

Returns a `gamlss.family` object which can be used to fit a COMPO2 distribution in the `gamlss()` function.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Ribeiro Jr, Eduardo E., et al. "Reparametrization of COM–Poisson regression models with applications in the analysis of experimental data." Statistical Modelling 20.5 (2020): 443-466.

See Also

dCOMPO2.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rCOMPO2(n=500, mu=10, sigma=-1)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=COMPO2,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
coef(mod1, what="sigma")

# Example 2
# Generating random values under some model

## Not run:
# A function to simulate a data set with Y ~ COMPO2
gendat <- function(n) {
```

```
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(2 + 1 * x1) # 12 approximately
  sigma <- 1 - 2 * x2      # 0 approximately
  y <- rCOMPO2(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=200)

# Fitting the model
mod2 <- NULL
mod2 <- gamlss(y~x1, sigma.fo=~x2, family=COMPO2, data=dat)

summary(mod2)

## End(Not run)
```

---

dBerG *Bernoulli-geometric distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Bernoulli-geometric distribution with parameters μ and σ.

Usage

```
dBerG(x, mu, sigma, log = FALSE)

pBerG(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rBerG(n, mu, sigma)

qBerG(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
n	number of random values to return.
p	vector of probabilities.

Details

The BerG distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \frac{(1-\mu+\sigma)}{(1+\mu+\sigma)}$ if $x = 0$,

$f(x|\mu,\sigma) = 4\mu\frac{(\mu+\sigma-1)^{x-1}}{(\mu+\sigma+1)^{x+1}}$ if $x = 1, 2, ...,$

with $\mu > 0$, $\sigma > 0$ and $\sigma > |\mu - 1|$.

Value

`dBerG` gives the density, `pBerG` gives the distribution function, `qBerG` gives the quantile function, `rBerG` generates random deviates.

Author(s)

Hermes Marques, <hermes.marques@ufrn.br>

References

Bourguignon, M., & de Medeiros, R. M. (2022). A simple and useful regression model for fitting count data. Test, 31(3), 790-827.

See Also

BerG.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 20
probs1 <- dBerG(x=0:x_max, mu=0.7, sigma=0.5)
probs2 <- dBerG(x=0:x_max, mu=0.3, sigma=1)
probs3 <- dBerG(x=0:x_max, mu=2, sigma=3)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for BerG",
     ylim=c(0, 0.80))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=0.7, sigma=0.5",
                "mu=0.3, sigma=1",
                "mu=2, sigma=3"))

# Example 2
# Checking if the cumulative curves converge to 1

#plot1
```

```
x_max <- 10
plot_discrete_cdf(x=0:x_max,
                  fx=dBerG(x=0:x_max, mu=1, sigma=2),
                  col="dodgerblue",
                  main="CDF for BerG",
                  lwd=3)
legend("bottomright", legend="mu=1, sigma=2",
       col="dodgerblue", lty=1, lwd=2, cex=0.8)


#plot2
plot_discrete_cdf(x=0:x_max,
                  fx=dBerG(x=0:x_max, mu=3, sigma=3),
                  col="tomato",
                  main="CDF for BerG",
                  lwd=3)
legend("bottomright", legend="mu=3, sigma=3",
       col="tomato", lty=1, lwd=2, cex=0.8)


#plot3
plot_discrete_cdf(x=0:x_max,
                  fx=dBerG(x=0:x_max, mu=5, sigma=5),
                  col="green4",
                  main="CDF for BerG",
                  lwd=3)
legend("bottomright", legend="mu=5, sigma=5",
       col="green4", lty=1, lwd=2, cex=0.8)


# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 15
probs1 <- dBerG(x=0:x_max, mu=0.5, sigma=5)
names(probs1) <- 0:x_max

x <- rBerG(n=1000, mu=0.5, sigma=5)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside=TRUE, names.arg=cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function
```

```
mu <- 1
sigma <- 2
p <- seq(from=0, to=1, by=0.01)
qxx <- qBerG(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of DBerG(mu=1, sigma=2)")
```

DBH *The Discrete Burr Hatke family*

Description

The function DBH() defines the Discrete Burr Hatke distribution a single parameter distribution, for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
DBH(mu.link = "logit")
```

Arguments

mu.link	defines the mu.link, with "logit" link as the default for the mu parameter. Other links are "probit" and "cloglog"'(complementary log-log)

Details

The Discrete Burr-Hatke distribution with parameter μ has a support 0, 1, 2, ... and its probability mass function (pmf) is given by

$f(x|\mu) = (\frac{1}{x+1} - \frac{\mu}{x+2})\mu^x$

The pmf is log-convex for all values of $0 < \mu < 1$, where $\frac{f(x+1;\mu)}{f(x;\mu)}$ is an increasing function in x for all values of the parameter μ.

Note: in this implementation we changed the original parameters λ for μ, we did it to implement this distribution within gamlss framework.

Value

Returns a gamlss.family object which can be used to fit a Discrete Burr-Hatke distribution in the gamlss() function.

Author(s)

Valentina Hurtado Sepulveda, <vhurtados@unal.edu.co>

References

El-Morshedy, M., Eliwa, M. S., & Altun, E. (2020). Discrete Burr-Hatke distribution with properties, estimation methods and regression model. IEEE access, 8, 74359-74370.

See Also

dDBH.

Examples

```
# Example 1
# Generating some random values with
# known mu
y <- rDBH(n=1000, mu=0.74)

library(gamlss)
mod1 <- gamlss(y~1, family=DBH,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
# using the inverse logit function
inv_logit <- function(x) exp(x) / (1+exp(x))
inv_logit(coef(mod1, parameter="mu"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ DBH
gendat <- function(n) {
  x1 <- runif(n)
  mu    <- inv_logit(-3 + 5 * x1)
  y <- rDBH(n=n, mu=mu)
  data.frame(y=y, x1=x1)
}

datos <- gendat(n=150)

mod2 <- NULL
mod2 <- gamlss(y~x1, family=DBH, data=datos,
               control=gamlss.control(n.cyc=500, trace=FALSE))

summary(mod2)

# Example 3
# Number of carious teeth among the four deciduous molars.
# Taken from EL-MORSHEDY (2020) page 74364.

y <- rep(0:4, times=c(64, 17, 10, 6, 3))

mod3 <- gamlss(y~1, family=DBH,
               control=gamlss.control(n.cyc=500, trace=FALSE))
```

```
# Extracting the fitted values for mu
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))
inv_logit(coef(mod3, what="mu"))

# Example 4
# Counts of cysts of kidneys using steroids.
# Taken from EL-MORSHEDY (2020) page 74365.

y <- rep(0:11, times=c(65, 14, 10, 6, 4, 2, 2, 2, 1, 1, 1, 2))

mod4 <- gamlss(y~1, family=DBH,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))
inv_logit(coef(mod4, what="mu"))
```

---

dCOMPO *The COMPO distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Conway-Maxwell-Poisson distribution with parameters μ and σ.

Usage

```
dCOMPO(x, mu, sigma, log = FALSE)

pCOMPO(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qCOMPO(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rCOMPO(n, mu, sigma)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
p	vector of probabilities.
n	number of random values to return.

Details

The COMPO distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \frac{\mu^x}{(x!)^\sigma Z(\mu,\sigma)}$

with $\mu > 0$, $\sigma \geq 0$ and

$Z(\mu,\sigma) = \sum_{j=0}^{\infty} \frac{\mu^j}{(j!)^\sigma}$.

The proposed functions here are based on the functions from the COMPoissonReg package.

Value

`dCOMPO` gives the density, `pCOMPO` gives the distribution function, `qCOMPO` gives the quantile function, `rCOMPO` generates random deviates.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Shmueli, G., Minka, T. P., Kadane, J. B., Borle, S., & Boatwright, P. (2005). A useful distribution for fitting discrete data: revival of the Conway–Maxwell–Poisson distribution. Journal of the Royal Statistical Society Series C: Applied Statistics, 54(1), 127-142.

See Also

COMPO.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 20
probs1 <- dCOMPO(x=0:x_max, mu=2, sigma=0.5)
probs2 <- dCOMPO(x=0:x_max, mu=8, sigma=1.0)
probs3 <- dCOMPO(x=0:x_max, mu=15, sigma=1.5)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for COMPO",
     ylim=c(0, 0.30))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=2, sigma=0.5",
                "mu=8, sigma=1.0",
                "mu=15, sigma=1.5"))

# Example 2
```

```
# Checking if the cumulative curves converge to 1

x_max <- 20
cumulative_probs1 <- pCOMPO(q=0:x_max, mu=2, sigma=0.5)
cumulative_probs2 <- pCOMPO(q=0:x_max, mu=8, sigma=1.0)
cumulative_probs3 <- pCOMPO(q=0:x_max, mu=15, sigma=1.5)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for COMPO",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
legend("bottomright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=2, sigma=0.5",
                "mu=8, sigma=1.0",
                "mu=15, sigma=1.5"))

# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 50
probs1 <- dCOMPO(x=0:x_max, mu=5, sigma=0.5)
names(probs1) <- 0:x_max

x <- rCOMPO(n=1000, mu=5, sigma=0.5)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside = TRUE, names.arg = cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 3
sigma <- 1.5
p <- seq(from=0.01, to=0.99, by=0.01)
qxx <- qCOMPO(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of COMPO(mu = 3, sigma = 1.5)")
```

---

dCOMPO2 *The COMPO2 distribution (with mu as mean)*

Description

These functions define the density, distribution function, quantile function and random generation for the Comway-Maxwell-Poisson distribution with parameters μ and σ. This parameterization was proposed by Ribeiro et al. (2020) and the main characteristic is that $E(X) = \mu$.

Usage

```
dCOMPO2(x, mu, sigma, log = FALSE)

pCOMPO2(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qCOMPO2(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rCOMPO2(n, mu, sigma)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
p	vector of probabilities.
n	number of random values to return.

Details

The COMPO2 distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \left(\mu + \frac{\exp(\sigma)-1}{2\exp(\sigma)}\right)^{x\exp(\sigma)} \frac{(x!)^{\exp(\sigma)}}{Z(\mu,\sigma)}$

with $\mu > 0$, $\sigma \in \Re$ and

$Z(\mu,\sigma) = \sum_{j=0}^{\infty} \frac{\mu^j}{(j!)^{\sigma}}$.

The proposed functions here are based on the functions from the COMPoissonReg package.

Value

dCOMPO2 gives the density, pCOMPO2 gives the distribution function, qCOMPO2 gives the quantile function, rCOMPO2 generates random deviates.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Ribeiro Jr, Eduardo E., et al. "Reparametrization of COM–Poisson regression models with applications in the analysis of experimental data." Statistical Modelling 20.5 (2020): 443-466.

See Also

COMPO2.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 20
probs1 <- dCOMPO2(x=0:x_max, mu=2, sigma=-0.7)
probs2 <- dCOMPO2(x=0:x_max, mu=8, sigma=0)
probs3 <- dCOMPO2(x=0:x_max, mu=15, sigma=0.7)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for COMPO2",
     ylim=c(0, 0.30))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=2, sigma=-0.7",
                "mu=8, sigma=0",
                "mu=15, sigma=0.7"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 20
cumulative_probs1 <- pCOMPO2(q=0:x_max, mu=2, sigma=-0.7)
cumulative_probs2 <- pCOMPO2(q=0:x_max, mu=8, sigma=0)
cumulative_probs3 <- pCOMPO2(q=0:x_max, mu=15, sigma=0.7)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for COMPO2",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
legend("bottomright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=2, sigma=-0.7",
                "mu=8, sigma=0",
                "mu=15, sigma=0.7"))

# Example 3
# Comparing the random generator output with
# the theoretical probabilities
```

```
x_max <- 15
probs1 <- dCOMPO2(x=0:x_max, mu=5, sigma=0.5)
names(probs1) <- 0:x_max

x <- rCOMPO2(n=1000, mu=5, sigma=0.5)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside = TRUE, names.arg = cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 3
sigma <- 0.15
p <- seq(from=0.01, to=0.99, by=0.01)
qxx <- qCOMPO2(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of COMPO2(mu = 3, sigma = 0.15)")
```

---

dDBH *The Discrete Burr Hatke distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Discrete Burr Hatke distribution with parameter μ.

Usage

```
dDBH(x, mu, log = FALSE)

pDBH(q, mu, lower.tail = TRUE, log.p = FALSE)

qDBH(p, mu = 1, lower.tail = TRUE, log.p = FALSE)

rDBH(n, mu = 1)
```

Arguments

x, q	vector of (non-negative integer) quantiles.

mu	vector of the mu parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
p	vector of probabilities.
n	number of random values to return

Details

The Discrete Burr-Hatke distribution with parameters μ has a support 0, 1, 2, ... and density given by

$f(x|\mu) = (\frac{1}{x+1} - \frac{\mu}{x+2})\mu^x$

The pmf is log-convex for all values of $0 < \mu < 1$, where $\frac{f(x+1;\mu)}{f(x;\mu)}$ is an increasing function in x for all values of the parameter μ.

Note: in this implementation we changed the original parameters λ for μ, we did it to implement this distribution within gamlss framework.

Value

dDBH gives the density, pDBH gives the distribution function, qDBH gives the quantile function, rDBH generates random deviates.

Author(s)

Valentina Hurtado Sepulveda, <vhurtados@unal.edu.co>

References

El-Morshedy, M., Eliwa, M. S., & Altun, E. (2020). Discrete Burr-Hatke distribution with properties, estimation methods and regression model. IEEE access, 8, 74359-74370.

See Also

DBH.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

plot(x=0:5, y=dDBH(x=0:5, mu=0.1),
     type="h", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", ylim=c(0, 1),
     main="Probability mu=0.1")

plot(x=0:10, y=dDBH(x=0:10, mu=0.5),
     type="h", lwd=2, col="tomato", las=1,
     ylab="P(X=x)", xlab="X", ylim=c(0, 1),
     main="Probability mu=0.5")
```

```
plot(x=0:15, y=dDBH(x=0:15, mu=0.9),
     type="h", lwd=2, col="green4", las=1,
     ylab="P(X=x)", xlab="X", ylim=c(0, 1),
     main="Probability mu=0.9")

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 15
cumulative_probs1 <- pDBH(q=0:x_max, mu=0.1)
cumulative_probs2 <- pDBH(q=0:x_max, mu=0.5)
cumulative_probs3 <- pDBH(q=0:x_max, mu=0.9)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for Burr-Hatke",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
legend("bottomright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=0.1",
                "mu=0.5",
                "mu=0.9"))

# Example 3
# Comparing the random generator output with
# the theoretical probabilities

mu <- 0.4
x_max <- 10
probs1 <- dDBH(x=0:x_max, mu=mu)
names(probs1) <- 0:x_max

x <- rDBH(n=1000, mu=mu)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside = TRUE, names.arg = cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 0.97
p <- seq(from=0, to=1, by = 0.01)
qxx <- qDBH(p, mu, lower.tail = TRUE, log.p = FALSE)
```

```
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of BH(mu=0.97)")
```

---

dDGEII *Discrete generalized exponential distribution - a second type*

Description

These functions define the density, distribution function, quantile function and random generation for the Discrete generalized exponential distribution a second type with parameters μ and σ.

Usage

```
dDGEII(x, mu = 0.5, sigma = 1.5, log = FALSE)

pDGEII(q, mu = 0.5, sigma = 1.5, lower.tail = TRUE, log.p = FALSE)

rDGEII(n, mu = 0.5, sigma = 1.5)

qDGEII(p, mu = 0.5, sigma = 1.5, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
n	number of random values to return.
p	vector of probabilities.

Details

The DGEII distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = (1-\mu^{x+1})^{\sigma} - (1-\mu^{x})^{\sigma}$

with $0 < \mu < 1$ and $\sigma > 0$. If $\sigma = 1$, the DGEII distribution reduces to the geometric distribution with success probability $1 - \mu$.

Note: in this implementation we changed the original parameters p to μ and α to σ, we did it to implement this distribution within gamlss framework.

Value

dDGEII gives the density, pDGEII gives the distribution function, qDGEII gives the quantile function, rDGEII generates random deviates.

Author(s)

Valentina Hurtado Sepulveda, <vhurtados@unal.edu.co>

References

Nekoukhou, V., Alamatsaz, M. H., & Bidram, H. (2013). Discrete generalized exponential distribution of a second type. Statistics, 47(4), 876-887.

See Also

DGEII.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 40
probs1 <- dDGEII(x=0:x_max, mu=0.1, sigma=5)
probs2 <- dDGEII(x=0:x_max, mu=0.5, sigma=5)
probs3 <- dDGEII(x=0:x_max, mu=0.9, sigma=5)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for DGEII",
     ylim=c(0, 0.60))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=0.1, sigma=5",
                "mu=0.5, sigma=5",
                "mu=0.9, sigma=5"))

# Example 2
# Checking if the cumulative curves converge to 1

#plot1
x_max <- 10
plot_discrete_cdf(x=0:x_max,
                  fx=dDGEII(x=0:x_max, mu=0.3, sigma=15),
                  col="dodgerblue",
                  main="CDF for DGEII",
                  lwd=3)
legend("bottomright", legend="mu=0.3, sigma=15",
       col="dodgerblue", lty=1, lwd=2, cex=0.8)


#plot2
plot_discrete_cdf(x=0:x_max,
                  fx=dDGEII(x=0:x_max, mu=0.5, sigma=30),
                  col="tomato",
                  main="CDF for DGEII",
```

```
                  lwd=3)
legend("bottomright", legend="mu=0.5, sigma=30",
       col="tomato", lty=1, lwd=2, cex=0.8)


#plot3
plot_discrete_cdf(x=0:x_max,
                  fx=dDGEII(x=0:x_max, mu=0.5, sigma=50),
                  col="green4",
                  main="CDF for DGEII",
                  lwd=3)
legend("bottomright", legend="mu=0.5, sigma=50",
       col="green4", lty=1, lwd=2, cex=0.8)


# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 15
probs1 <- dDGEII(x=0:x_max, mu=0.5, sigma=5)
names(probs1) <- 0:x_max

x <- rDGEII(n=1000, mu=0.5, sigma=5)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside=TRUE, names.arg=cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 0.5
sigma <- 5
p <- seq(from=0, to=1, by=0.01)
qxx <- qDGEII(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of DDGEII(mu=0.5, sigma=5)")
```

---

dDIKUM *The discrete Inverted Kumaraswamy distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the discrete Inverted Kumaraswamy, DIKUM(), distribution with parameters μ and σ.

Usage

```
dDIKUM(x, mu = 1, sigma = 5, log = FALSE)

pDIKUM(q, mu = 1, sigma = 5, lower.tail = TRUE, log.p = FALSE)

rDIKUM(n, mu = 1, sigma = 5)

qDIKUM(p, mu = 1, sigma = 5, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
n	number of random values to return.
p	vector of probabilities.

Details

The discrete Inverted Kumaraswamy distribution with parameters μ and σ has a support 0, 1, 2, ... and density given by

$f(x|\mu,\sigma) = (1-(2+x)^{-\mu})^{\sigma} - (1-(1+x)^{-\mu})^{\sigma}$

with $\mu > 0$ and $\sigma > 0$.

Note: in this implementation we changed the original parameters α and β for μ and σ respectively, we did it to implement this distribution within gamlss framework.

Value

dDIKUM gives the density, pDIKUM gives the distribution function, qDIKUM gives the quantile function, rDIKUM generates random deviates.

Author(s)

Daniel Felipe Villa Rengifo, <dvilla@unal.edu.co>

References

El-Helbawy, A. A., Hegazy, M. A., Al-Dayian, G. R., & Abd EL-Kader, R. E. (2022). A discrete analog of the inverted Kumaraswamy distribution: properties and estimation with application to COVID-19 data. Pakistan Journal of Statistics and Operation Research, 18(1), 297-328.

See Also

DIKUM.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 30

probs1 <- dDIKUM(x=0:x_max, mu=1, sigma=5)
probs2 <- dDIKUM(x=0:x_max, mu=1, sigma=20)
probs3 <- dDIKUM(x=0:x_max, mu=1, sigma=50)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for Inverted Kumaraswamy Distribution",
     ylim=c(0, 0.12))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=1, sigma=5",
                "mu=1, sigma=20",
                "mu=1, sigma=50"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 500

cumulative_probs1 <- pDIKUM(q=0:x_max, mu=1, sigma=5)
cumulative_probs2 <- pDIKUM(q=0:x_max, mu=1, sigma=20)
cumulative_probs3 <- pDIKUM(q=0:x_max, mu=1, sigma=50)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for Inverted Kumaraswamy Distribution",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
legend("bottomright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=1, sigma=5",
                "mu=1, sigma=20",
                "mu=1, sigma=50"))

# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 20
probs1 <- dDIKUM(x=0:x_max, mu=3, sigma=20)
names(probs1) <- 0:x_max
```

```
x <- rDIKUM(n=1000, mu=3, sigma=20)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
nombres <- cn
mp <- barplot(height, beside = TRUE, names.arg = nombres,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 1
sigma <- 5
p <- seq(from=0.01, to=0.99, by=0.1)
qxx <- qDIKUM(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of HP(mu = sigma = 3)")
```

---

dDLD *The Discrete Lindley distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Discrete Lindley distribution with parameter μ.

Usage

```
dDLD(x, mu, log = FALSE)

pDLD(q, mu, lower.tail = TRUE, log.p = FALSE)

qDLD(p, mu, lower.tail = TRUE, log.p = FALSE)

rDLD(n, mu = 0.5)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of positive values of this parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).

lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
p	vector of probabilities.
n	number of random values to return.

Details

The Discrete Lindley distribution with parameters μ has a support 0, 1, 2, ... and density given by

$f(x|\mu) = \frac{e^{-\mu x}}{1+\mu}\,[\mu(1-2e^{-\mu}) + (1-e^{-\mu})(1+\mu x)]$

Note: in this implementation we changed the original parameters θ for μ, we did it to implement this distribution within gamlss framework.

Value

dDLD gives the density, pDLD gives the distribution function, qDLD gives the quantile function, rDLD generates random deviates.

Author(s)

Yojan Andrés Alcaraz Pérez, <yalcaraz@unal.edu.co>

References

Bakouch, H. S., Jazi, M. A., & Nadarajah, S. (2014). A new discrete distribution. Statistics, 48(1), 200-240.

See Also

DLD.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

plot(x=0:25, y=dDLD(x=0:25, mu=0.2),
     type="h", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", ylim=c(0, 0.1),
     main="Probability mu=0.2")

plot(x=0:15, y=dDLD(x=0:15, mu=0.5),
     type="h", lwd=2, col="tomato", las=1,
     ylab="P(X=x)", xlab="X", ylim=c(0, 0.25),
     main="Probability mu=0.5")

plot(x=0:8, y=dDLD(x=0:8, mu=1),
     type="h", lwd=2, col="green4", las=1,
     ylab="P(X=x)", xlab="X", ylim=c(0, 0.5),
     main="Probability mu=1")

plot(x=0:5, y=dDLD(x=0:5, mu=2),
```

```
     type="h", lwd=2, col="red", las=1,
     ylab="P(X=x)", xlab="X", ylim=c(0, 1),
     main="Probability mu=2")

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 10
cumulative_probs1 <- pDLD(q=0:x_max, mu=0.2)
cumulative_probs2 <- pDLD(q=0:x_max, mu=0.5)
cumulative_probs3 <- pDLD(q=0:x_max, mu=1)
cumulative_probs4 <- pDLD(q=0:x_max, mu=2)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for Lindley",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
points(x=0:x_max, y=cumulative_probs4, type="o", col="magenta")
legend("bottomright",
       col=c("dodgerblue", "tomato", "green4", "magenta"), lwd=3,
       legend=c("mu=0.2",
                "mu=0.5",
                "mu=1",
                "mu=2"))

# Example 3
# Comparing the random generator output with
# the theoretical probabilities

mu <- 0.6
x <- rDLD(n = 1000, mu = mu)
x_max <- max(x)
probs1 <- dDLD(x = 0:x_max, mu = mu)
names(probs1) <- 0:x_max

probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])

mp <- barplot(height, beside = TRUE, names.arg = cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function
```

```
mu <- 0.9
p <- seq(from=0, to=1, by=0.01)
qxx <- qDLD(p, mu, lower.tail = TRUE, log.p = FALSE)
plot(p, qxx, type="S", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of DL(mu=0.9)")
```

---

dDMOLBE *The DMOLBE distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Discrete Marshall–Olkin Length Biased Exponential DMOLBE distribution with parameters μ and σ.

Usage

```
dDMOLBE(x, mu = 1, sigma = 1, log = FALSE)

pDMOLBE(q, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rDMOLBE(n, mu = 1, sigma = 1)

qDMOLBE(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
n	number of random values to return.
p	vector of probabilities.

Details

The DMOLBE distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \frac{\sigma((1+x/\mu)\exp(-x/\mu)-(1+(x+1)/\mu)\exp(-(x+1)/\mu))}{(1-(1-\sigma)(1+x/\mu)\exp(-x/\mu))((1-(1-\sigma)(1+(x+1)/\mu)\exp(-(x+1)/\mu))}$

with $\mu > 0$ and $\sigma > 0$

Value

dDMOLBE gives the density, pDMOLBE gives the distribution function, qDMOLBE gives the quantile function, rDMOLBE generates random deviates.

Author(s)

Olga Usuga, <olga.usuga@udea.edu.co>

References

Aljohani, H. M., Ahsan-ul-Haq, M., Zafar, J., Almetwally, E. M., Alghamdi, A. S., Hussam, E., & Muse, A. H. (2023). Analysis of Covid-19 data using discrete Marshall–Olkinin length biased exponential: Bayesian and frequentist approach. Scientific Reports, 13(1), 12243.

See Also

DMOLBE.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 20
probs1 <- dDMOLBE(x=0:x_max, mu=0.5, sigma=0.5)
probs2 <- dDMOLBE(x=0:x_max, mu=5, sigma=0.5)
probs3 <- dDMOLBE(x=0:x_max, mu=1, sigma=2)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for DMOLBE",
     ylim=c(0, 0.80))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=0.5, sigma=0.5",
                "mu=5, sigma=0.5",
                "mu=1, sigma=2"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 20
cumulative_probs1 <- pDMOLBE(q=0:x_max, mu=0.5, sigma=0.5)
cumulative_probs2 <- pDMOLBE(q=0:x_max, mu=5, sigma=0.5)
cumulative_probs3 <- pDMOLBE(q=0:x_max, mu=1, sigma=2)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for DMOLBE",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
legend("bottomright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=0.5, sigma=0.5",
                "mu=5, sigma=0.5",
                "mu=1, sigma=2"))
```

```
# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 50
probs1 <- dDMOLBE(x=0:x_max, mu=5, sigma=0.5)
names(probs1) <- 0:x_max

x <- rDMOLBE(n=1000, mu=5, sigma=0.5)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside = TRUE, names.arg = cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 3
sigma <-3
p <- seq(from=0, to=1, by=0.01)
qxx <- qDMOLBE(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of DMOLBE(mu = 3, sigma = 3)")
```

---

dDPERKS *The Discrete Perks distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Discrete Perks, DPERKS(), distribution with parameters μ and σ.

Usage

```
dDPERKS(x, mu = 0.5, sigma = 0.5, log = FALSE)

pDPERKS(q, mu = 0.5, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rDPERKS(n, mu = 0.5, sigma = 0.5)

qDPERKS(p, mu = 0.5, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
n	number of random values to return.
p	vector of probabilities.

Details

The discrete Perks distribution with parameters $\mu > 0$ and $\sigma > 0$ has a support 0, 1, 2, ... and density given by

$f(x|\mu,\sigma) = \frac{\mu(1+\mu)(e^{\sigma}-1)e^{\sigma x}}{(1+\mu e^{\sigma x})(1+\mu e^{\sigma(x+1)})}$

Note: in this implementation we changed the original parameters λ for μ and β for σ, we did it to implement this distribution within gamlss framework.

Value

dDPERKS gives the density, pDPERKS gives the distribution function, qDPERKS gives the quantile function, rDPERKS generates random deviates.

Author(s)

Veronica Seguro Varela, <vseguro@unal.edu.co>

References

Tyagi, A., Choudhary, N., & Singh, B. (2020). A new discrete distribution: Theory and applications to discrete failure lifetime and count data. J. Appl. Probab. Statist, 15, 117-143.

See Also

DPERKS.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 25
probs1 <- dDPERKS(x=0:x_max, mu=0.001, sigma=0.52)
probs2 <- dDPERKS(x=0:x_max, mu=0.001, sigma=0.85)
probs3 <- dDPERKS(x=0:x_max, mu=0.001, sigma=1.5)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="green4", las=1,
```

```
     ylab="P(X=x)", xlab="X", main="Probability for DPERKS",
     ylim=c(0, 0.40))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="black")
legend("topright", col=c("green4", "tomato", "black"), lwd=3,
       legend=c("mu=0.001, sigma=0.52 ",
                "mu=0.001, sigma=0.85",
                "mu=0.001, sigma=1.5"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 25
cumulative_probs1 <- pDPERKS(q=0:x_max, mu=0.001, sigma=0.52)
cumulative_probs2 <- pDPERKS(q=0:x_max, mu=0.001, sigma=0.85)
cumulative_probs3 <- pDPERKS(q=0:x_max, mu=0.001, sigma=1.5)

plot(x=0:x_max, y=cumulative_probs1, col="green4",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for DPERKS",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="black")
legend("bottomright", col=c("green4", "tomato", "black"), lwd=3,
       legend=c("mu=0.001, sigma=0.52 ",
                "mu=0.001, sigma=0.85",
                "mu=0.001, sigma=1.5"))

# Example 3
# Comparing the random generator output with the theoretical probabilities

x_max <- 20
mu <- 2.5
sigma <- 0.4
probs1 <- dDPERKS(x=0:x_max, mu=mu, sigma=sigma)
names(probs1) <- 0:x_max

x <- rDPERKS(n=10000, mu=mu, sigma=sigma)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
nombres <- cn
mp <- barplot(height, beside = TRUE, names.arg = nombres,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function
```

```
mu <- 0.2
sigma <- 0.2
p <- seq(from=0, to=1, by=0.01)
qxx <- qDPERKS(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of DPERKS(mu = sigma = 0.2)")
```

---

dDsPA *The DsPA distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the discrete power-Ailamujia distribution with parameters μ and σ.

Usage

```
dDsPA(x, mu, sigma, log = FALSE)

pDsPA(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qDsPA(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rDsPA(n, mu, sigma)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
p	vector of probabilities.
n	number of random values to return.

Details

The DsPA distribution with parameters μ and σ has a support 0, 1, 2, ...

Note:in this implementation we changed the original parameters β and λ for μ and σ respectively, we did it to implement this distribution within gamlss framework.

Value

dDsPA gives the density, pDsPA gives the distribution function, qDsPA gives the quantile function.

Author(s)

Maria Camila Mena Romana, <mamenar@unal.edu.co>

References

Alghamdi, A. S., Ahsan-ul-Haq, M., Babar, A., Aljohani, H. M., Afify, A. Z., & Cell, Q. E. (2022). The discrete power-Ailamujia distribution: properties, inference, and applications. AIMS Math, 7(5), 8344-8360.

See Also

DsPA.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 30
probs1 <- dDsPA(x=0:x_max, mu=1.2, sigma=0.5)
probs2 <- dDsPA(x=0:x_max, mu=1.2, sigma=0.7)
probs3 <- dDsPA(x=0:x_max, mu=1.2, sigma=0.9)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for DsPA",
     ylim=c(0, 0.40))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=1.2, sigma=0.5",
                "mu=1.2, sigma=0.7",
                "mu=1.2, sigma=0.9"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 15
cumulative_probs1 <- pDsPA(q=0:x_max, mu=1.2, sigma=0.5)
cumulative_probs2 <- pDsPA(q=0:x_max, mu=1.2, sigma=0.7)
cumulative_probs3 <- pDsPA(q=0:x_max, mu=1.2, sigma=0.9)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for DsPA",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
legend("bottomright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=1.2, sigma=0.5",
                "mu=1.2, sigma=0.7",
                "mu=1.2, sigma=0.9"))
```

```
# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 50
probs1 <- dDsPA(x=0:x_max, mu=1.2, sigma=0.9)
names(probs1) <- 0:x_max

x <- rDsPA(n=1000, mu=1.2, sigma=0.9)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside=TRUE, names.arg=cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 1.2
sigma <- 0.9
p <- seq(from=0, to=1, by=0.01)
qxx <- qDsPA(p=p, mu=mu, sigma=sigma,
                lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of DsPA(mu=1.2, sigma=0.9)")
```

DGEII *The DGEII distribution*

Description

The function DGEII() defines the Discrete generalized exponential distribution of a Second type a two parameter distribution, for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
DGEII(mu.link = "logit", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "logit" link as the default for the mu parameter. Other links are "probit" and "cloglog"'(complementary log-log).
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The DGEII distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = (1-\mu^{x+1})^{\sigma} - (1-\mu^{x})^{\sigma}$

with $0 < \mu < 1$ and $\sigma > 0$. If $\sigma = 1$, the DGEII distribution reduces to the geometric distribution with success probability $1 - \mu$.

Note: in this implementation we changed the original parameters p to μ and α to σ, we did it to implement this distribution within gamlss framework.

Value

Returns a `gamlss.family` object which can be used to fit a DGEII distribution in the `gamlss()` function.

Author(s)

Valentina Hurtado Sepúlveda, <vhurtados@unal.edu.co>

References

Nekoukhou, V., Alamatsaz, M. H., & Bidram, H. (2013). Discrete generalized exponential distribution of a second type. Statistics, 47(4), 876-887.

See Also

dDGEII.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma

y <- rDGEII(n=100, mu=0.75, sigma=0.5)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, family=DGEII,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))
```

```
inv_logit(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ DGEII
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- inv_logit(1.7 - 2.8*x1)
  sigma <- exp(0.73 + 1*x2)
  y <- rDGEII(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

datos <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2, family=DGEII, data=datos,
               control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)

# Example 3
# Number of accidents to 647 women working on H. E. Shells
# for 5 weeks. Taken from
# Nekoukhou V, Alamatsaz MH, Bidram H (2013) page 886.

y <- rep(x=0:5, times=c(447, 132, 42, 21, 3, 2))

mod3 <- gamlss(y~1, family=DGEII,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))
inv_logit(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))
```

---

dGGEO *The GGEO distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Generalized Geometric distribution with parameters μ and σ.

Usage

```
dGGEO(x, mu = 0.5, sigma = 1, log = FALSE)

pGGEO(q, mu = 0.5, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rGGEO(n, mu = 0.5, sigma = 1)

qGGEO(p, mu = 0.5, sigma = 1, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
n	number of random values to return.
p	vector of probabilities.

Details

The GGEO distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \frac{\sigma\mu^x(1-\mu)}{(1-(1-\sigma)\mu^{x+1})(1-(1-\sigma)\mu^x)}$

with $0 < \mu < 1$ and $\sigma > 0$. If $\sigma = 1$, the GGEO distribution reduces to the geometric distribution with success probability $1 - \mu$.

Note: in this implementation we changed the original parameters θ for μ and α for σ, we did it to implement this distribution within gamlss framework.

Value

dGGEO gives the density, pGGEO gives the distribution function, qGGEO gives the quantile function, rGGEO generates random deviates.

Author(s)

Valentina Hurtado Sepulveda, <vhurtados@unal.edu.co>

References

Gómez-Déniz, E. (2010). Another generalization of the geometric distribution. Test, 19, 399-415.

See Also

GGEO.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 80
probs1 <- dGGEO(x=0:x_max, mu=0.5, sigma=10)
probs2 <- dGGEO(x=0:x_max, mu=0.7, sigma=30)
probs3 <- dGGEO(x=0:x_max, mu=0.9, sigma=50)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for GGEO",
     ylim=c(0, 0.20))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=0.5, sigma=10",
                "mu=0.7, sigma=30",
                "mu=0.9, sigma=50"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 10
plot_discrete_cdf(x=0:x_max,
                  fx=dGGEO(x=0:x_max, mu=0.3, sigma=15),
                  col="dodgerblue",
                  main="CDF for GGEO",
                  lwd= 3)
legend("bottomright", legend="mu=0.3, sigma=15", col="dodgerblue",
       lty=1, lwd=2, cex=0.8)

plot_discrete_cdf(x=0:x_max,
                  fx=dGGEO(x=0:x_max, mu=0.5, sigma=30),
                  col="tomato",
                  main="CDF for GGEO",
                  lwd=3)
legend("bottomright", legend="mu=0.5, sigma=30",
       col="tomato", lty=1, lwd=2, cex=0.8)

plot_discrete_cdf(x=0:x_max,
                  fx=dGGEO(x=0:x_max, mu=0.5, sigma=50),
                  col="green4",
                  main="CDF for GGEO",
                  lwd=3)
legend("bottomright", legend="mu=0.5, sigma=50",
       col="green4", lty=1, lwd=2, cex=0.8)

# Example 3
# Comparing the random generator output with
# the theoretical probabilities
```

```
x_max <- 15
probs1 <- dGGEO(x=0:x_max, mu=0.5, sigma=5)
names(probs1) <- 0:x_max

x <- rGGEO(n=1000, mu=0.5, sigma=5)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside=TRUE, names.arg=cn,
              col=c("dodgerblue3", "firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 0.5
sigma <- 5
p <- seq(from=0, to=1, by=0.01)
qxx <- qGGEO(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of GGEO(mu=0.5, sigma=0.5)")
```

---

dHYPERPO *The hyper-Poisson distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the hyper-Poisson, HYPERPO(), distribution with parameters μ and σ.

Usage

```
dHYPERPO(x, mu = 1, sigma = 1, log = FALSE)

pHYPERPO(q, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rHYPERPO(n, mu = 1, sigma = 1)

qHYPERPO(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of (non-negative integer) quantiles.

mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
n	number of random values to return.
p	vector of probabilities.

Details

The hyper-Poisson distribution with parameters μ and σ has a support 0, 1, 2, ... and density given by

$f(x|\mu,\sigma) = \frac{\mu^x}{{}_1F_1(1;\mu;\sigma)} \frac{\Gamma(\sigma)}{\Gamma(x+\sigma)}$

where the function ${}_1F_1(a;c;z)$ is defined as

${}_1F_1(a;c;z) = \sum_{r=0}^{\infty} \frac{(a)_r}{(c)_r} \frac{z^r}{r!}$

and $(a)_r = \frac{\gamma(a+r)}{\gamma(a)}$ for $a > 0$ and r positive integer.

Note: in this implementation we changed the original parameters λ and γ for μ and σ respectively, we did it to implement this distribution within gamlss framework.

Value

dHYPERPO gives the density, pHYPERPO gives the distribution function, qHYPERPO gives the quantile function, rHYPERPO generates random deviates.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Sáez-Castillo, A. J., & Conde-Sánchez, A. (2013). A hyper-Poisson regression model for overdispersed and underdispersed count data. Computational Statistics & Data Analysis, 61, 148-157.

See Also

HYPERPO.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 30
probs1 <- dHYPERPO(x=0:x_max, mu=5, sigma=0.1)
probs2 <- dHYPERPO(x=0:x_max, mu=5, sigma=1.0)
probs3 <- dHYPERPO(x=0:x_max, mu=5, sigma=1.8)

# To plot the first k values
```

```
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for hyper-Poisson",
     ylim=c(0, 0.20))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=5, sigma=0.1",
                "mu=5, sigma=1.0",
                "mu=5, sigma=1.8"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 15
cumulative_probs1 <- pHYPERPO(q=0:x_max, mu=5, sigma=0.1)
cumulative_probs2 <- pHYPERPO(q=0:x_max, mu=5, sigma=1.0)
cumulative_probs3 <- pHYPERPO(q=0:x_max, mu=5, sigma=1.8)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for hyper-Poisson",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
legend("bottomright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=5, sigma=0.1",
                "mu=5, sigma=1.0",
                "mu=5, sigma=1.8"))

# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 15
probs1 <- dHYPERPO(x=0:x_max, mu=3, sigma=1.1)
names(probs1) <- 0:x_max

x <- rHYPERPO(n=1000, mu=3, sigma=1.1)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
nombres <- cn
mp <- barplot(height, beside = TRUE, names.arg = nombres,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
       legend=c("Theoretical", "Simulated"),
       bty="n", lwd=3,
       col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function
```

```
mu <- 3
sigma <-3
p <- seq(from=0, to=1, by=0.01)
qxx <- qHYPERPO(p=p, mu=mu, sigma=sigma,
                lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of HP(mu=3, sigma=3)")
```

---

dHYPERPO2 *The hyper-Poisson distribution (with mu as mean)*

Description

These functions define the density, distribution function, quantile function and random generation for the hyper-Poisson in the second parameterization with parameters μ (as mean) and σ as the dispersion parameter.

Usage

```
dHYPERPO2(x, mu = 1, sigma = 1, log = FALSE)

pHYPERPO2(q, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rHYPERPO2(n, mu = 1, sigma = 1)

qHYPERPO2(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of positive values of this parameter.
sigma	vector of positive values of this parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
n	number of random values to return
p	vector of probabilities.

Details

The hyper-Poisson distribution with parameters μ and σ has a support 0, 1, 2, ...

Note: in this implementation the parameter μ is the mean of the distribution and σ corresponds to the dispersion parameter. If you fit a model with this parameterization, the time will increase because an internal procedure to convert μ to λ parameter.

Value

dHYPERPO2 gives the density, pHYPERPO2 gives the distribution function, qHYPERPO2 gives the quantile function, rHYPERPO2 generates random deviates.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Sáez-Castillo, A. J., & Conde-Sánchez, A. (2013). A hyper-Poisson regression model for overdispersed and underdispersed count data. Computational Statistics & Data Analysis, 61, 148-157.

See Also

HYPERPO2, HYPERPO.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 30
probs1 <- dHYPERPO2(x=0:x_max, sigma=0.01, mu=3)
probs2 <- dHYPERPO2(x=0:x_max, sigma=0.50, mu=5)
probs3 <- dHYPERPO2(x=0:x_max, sigma=1.00, mu=7)
# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for hyper-Poisson",
     ylim=c(0, 0.30))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("sigma=0.01, mu=3",
                "sigma=0.50, mu=5",
                "sigma=1.00, mu=7"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 15
cumulative_probs1 <- pHYPERPO2(q=0:x_max, mu=1, sigma=1.5)
cumulative_probs2 <- pHYPERPO2(q=0:x_max, mu=3, sigma=1.5)
cumulative_probs3 <- pHYPERPO2(q=0:x_max, mu=5, sigma=1.5)

plot(x=0:x_max, y=cumulative_probs1, col="dodgerblue",
     type="o", las=1, ylim=c(0, 1),
     main="Cumulative probability for hyper-Poisson",
     xlab="X", ylab="Probability")
points(x=0:x_max, y=cumulative_probs2, type="o", col="tomato")
points(x=0:x_max, y=cumulative_probs3, type="o", col="green4")
legend("bottomright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
```

```
       legend=c("sigma=1.5, mu=1",
                "sigma=1.5, mu=3",
                "sigma=1.5, mu=5"))

# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 15
probs1 <- dHYPERPO2(x=0:x_max, mu=3, sigma=1.1)
names(probs1) <- 0:x_max

x <- rHYPERPO2(n=1000, mu=3, sigma=1.1)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
nombres <- cn
mp <- barplot(height, beside = TRUE, names.arg = nombres,
              col=c('dodgerblue3','firebrick3'), las=1,
              xlab='X', ylab='Proportion')
legend('topright',
       legend=c('Theoretical', 'Simulated'),
       bty='n', lwd=3,
       col=c('dodgerblue3','firebrick3'), lty=1)

# Example 4
# Checking the quantile function

mu <- 3
sigma <-3
p <- seq(from=0, to=1, by=0.01)
qxx <- qHYPERPO2(p=p, mu=mu, sigma=sigma, lower.tail=TRUE, log.p=FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles of HP2(mu = sigma = 3)")
```

DIKUM *The discrete Inverted Kumaraswamy family*

Description

The function `DIKUM()` defines the discrete Inverted Kumaraswamy distribution a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
DIKUM(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The discrete Inverted Kumaraswamy distribution with parameters μ and σ has a support 0, 1, 2, ... and density given by

$f(x|\mu,\sigma) = (1-(2+x)^{-\mu})^{\sigma} - (1-(1+x)^{-\mu})^{\sigma}$

with $\mu > 0$ and $\sigma > 0$.

Note: in this implementation we changed the original parameters α and β for μ and σ respectively, we did it to implement this distribution within gamlss framework.

Value

Returns a `gamlss.family` object which can be used to fit a discrete Inverted Kumaraswamy distribution in the `gamlss()` function.

Author(s)

Daniel Felipe Villa Rengifo, <dvilla@unal.edu.co>

References

El-Helbawy, A. A., Hegazy, M. A., Al-Dayian, G. R., & Abd EL-Kader, R. E. (2022). A discrete analog of the inverted Kumaraswamy distribution: properties and estimation with application to COVID-19 data. Pakistan Journal of Statistics and Operation Research, 18(1), 297-328.

See Also

dDIKUM.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(150)
y <- rDIKUM(1000, mu=1, sigma=5)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y ~ 1, sigma.fo = ~1, family=DIKUM,
               control = gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))
```

```
# Example 2
# Generating random values under some model

library(gamlss)

# A function to simulate a data set with Y ~ DIKUM
gendat <- function(n) {
  x1 <- runif(n, min=0.4, max=0.6)
  x2 <- runif(n, min=0.4, max=0.6)
  mu    <- exp(1.21 - 3 * x1) # 0.75 approximately
  sigma <- exp(1.26 - 2 * x2) # 1.30 approximately
  y <- rDIKUM(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

dat <- gendat(n=1000)

# Fitting the model
mod2 <- gamlss(y ~ x1, sigma.fo = ~x2, family = "DIKUM", data=dat,
               control=gamlss.control(n.cyc=500, trace=FALSE))

summary(mod2)
```

DLD *The Discrete Lindley family*

Description

The function `DLD()` defines the Discrete Lindley distribution a single parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
DLD(mu.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.

Details

The Discrete Lindley distribution with parameters $\mu > 0$ has a support 0, 1, 2, ... and density given by

$f(x|\mu) = \frac{e^{-\mu x}}{1+\mu}(\mu(1-2e^{-\mu}) + (1-e^{-\mu})(1+\mu x))$

The parameter μ can be interpreted as a strict upper bound on the failure rate function

The conventional discrete distributions (such as geometric, Poisson, etc.) are not suitable for various scenarios like reliability, failure times, and counts. Consequently, alternative discrete distributions have been created by adapting well-known continuous models for reliability and failure times.

Among these, the discrete Weibull distribution stands out as the most widely used. But models like these require two parameters and not many of the known discrete distributions can provide accurate models for both times and counts, which the Discrete Lindley distribution does.

Note: in this implementation we changed the original parameters θ for μ, we did it to implement this distribution within gamlss framework.

Value

Returns a `gamlss.family` object which can be used to fit a Discrete Lindley distribution in the `gamlss()` function.

Author(s)

Yojan Andrés Alcaraz Pérez, <yalcaraz@unal.edu.co>

References

Bakouch, H. S., Jazi, M. A., & Nadarajah, S. (2014). A new discrete distribution. Statistics, 48(1), 200-240.

See Also

dDLD.

Examples

```
# Example 1
# Generating some random values with
# known mu
y <- rDLD(n=100, mu=0.3)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, family=DLD,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
# using the inverse link function
exp(coef(mod1, what="mu"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ DLD
gendat <- function(n) {
  x1 <- runif(n)
  mu    <- exp(2 - 4 * x1)
  y <- rDLD(n=n, mu=mu)
  data.frame(y=y, x1=x1)
}
```

```
set.seed(1235)
datos <- gendat(n=150)

mod2 <- NULL
mod2 <- gamlss(y~x1, sigma.fo=~x2, family=DLD, data=datos,
                control=gamlss.control(n.cyc=500, trace=FALSE))

summary(mod2)

# Example 3
# Survival times in days of 72 guinea pigs.
# Taken from Bakouch et al (2014) page 26.

y <- c(12, 15, 22, 24, 24, 32, 32, 33, 34, 38, 38, 43, 44, 48,
       52, 53, 54, 54, 55, 56, 57, 58, 58, 59, 60, 60, 60, 60,
       61, 62, 63, 65, 65, 67, 68, 70, 70, 72, 73, 75, 76, 76,
       81, 83, 84, 85, 87, 91, 95, 96, 98, 99, 109, 110, 121,
       127, 129, 131, 143, 146, 146, 175, 175, 211, 233, 258,
       258, 263, 297, 341, 341, 376)

mod3 <- gamlss(y~1, family=DLD,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
# using the inverse link function
exp(coef(mod3, what="mu"))


# Example 4
# Remission times in weeks for 20 leukaemia patients.
# Taken from Bakouch et al (2014) page 26.

y <- c(1, 3, 3, 6, 7, 7, 10, 12, 14, 15, 18, 19,
       22, 26, 28, 29, 34, 40, 48, 49)

mod4 <- gamlss(y~1, family=DLD,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
# using the inverse link function
exp(coef(mod4, what="mu"))

# Example 5
# Numbers of fires in Greece for the period from 1
# July 1998 to 31 August of the same year .
# Taken from Bakouch et al (2014) page 26.

y <- c(2, 4, 4, 3, 3, 1, 2, 4, 3, 1, 1, 0, 5, 5, 0, 3, 1,
       1, 0, 1, 0, 2, 0, 1, 2, 0, 0, 0, 0, 0, 0, 0, 0, 0,
       1, 4, 2, 2, 1, 2, 1, 2, 0, 2, 2, 1, 0, 3, 2, 1, 2,
       2, 7, 3, 5, 2, 5, 4, 5, 6, 5, 4, 3, 8, 43, 8, 4, 4,
       3, 10, 5, 4, 5, 12, 3, 8, 12, 10, 11, 6, 1, 8, 9,
       12, 9, 4, 8, 12, 11, 8, 6, 4, 7, 9, 15, 12, 15, 15,
```

```
       12, 9, 16, 7, 11, 9, 11, 6, 5, 20, 9, 8, 8, 5, 7, 10,
       6, 6, 5, 5, 15, 6, 8, 5, 6)

mod5 <- gamlss(y~1, family=DLD,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
# using the inverse link function
exp(coef(mod5, what="mu"))

# Example 6
# Final examination marks of space students in
# mathematics in the Indian Institute of Technology at Kanpur.
# Taken from Bakouch et al (2014) page 26.

y <- c(29, 25, 50, 15, 13, 27, 15, 18, 7, 7, 8, 19, 12,
       18, 5, 21, 15, 86, 21, 15, 14, 39, 15, 14, 70,
       44, 6, 23, 58, 19, 50, 23, 11, 6, 34, 18, 28, 34,
       12, 37, 4, 60, 20, 23, 40, 65, 19, 31)

mod6 <- gamlss(y~1, family=DLD,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
# using the inverse link function
exp(coef(mod6, what="mu"))
```

DMOLBE *The DMOLBE family*

Description

The function `DMOLBE()` defines the Discrete Marshall-Olkin Length Biased Exponential distribution a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
DMOLBE(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The DMOLBE distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \frac{\sigma((1+x/\mu)\exp(-x/\mu)-(1+(x+1)/\mu)\exp(-(x+1)/\mu))}{(1-(1-\sigma)(1+x/\mu)\exp(-x/\mu))((1-(1-\sigma)(1+(x+1)/\mu)\exp(-(x+1)/\mu))}$

with $\mu > 0$ and $\sigma > 0$

Value

Returns a `gamlss.family` object which can be used to fit a DMOLBE distribution in the `gamlss()` function.

Author(s)

Olga Usuga, <olga.usuga@udea.edu.co>

References

Aljohani, H. M., Ahsan-ul-Haq, M., Zafar, J., Almetwally, E. M., Alghamdi, A. S., Hussam, E., & Muse, A. H. (2023). Analysis of Covid-19 data using discrete Marshall–Olkinin length biased exponential: Bayesian and frequentist approach. Scientific Reports, 13(1), 12243.

See Also

dDMOLBE.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(1234)
y <- rDMOLBE(n=200, mu=3, sigma=7)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=DMOLBE)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ DMOLBE
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(1.21 - 3 * x1) # 0.75 approximately
```

```
  sigma <- exp(1.26 - 2 * x2) # 1.30 approximately
  y <- rDMOLBE(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=200)

# Fitting the model
mod2 <- NULL
mod2 <- gamlss(y~x1, sigma.fo=~x2, family=DMOLBE, data=dat,
                 control=gamlss.control(n.cyc=500, trace=FALSE))

summary(mod2)


# Example 3
# Data Set I (death due to coronavirus in China). The first data set is the number
# of deaths due to coronavirus in China from 23 January to 28 March.
# The data sets used in the paper was collected from 2020 year. The data set
# is reported in https://www.worldometers.info/coronavirus/country/china/.
# The data are:

y <- c(8, 16, 15, 24, 26, 26, 38, 43, 46, 45, 57, 64, 65, 73, 73, 86, 89, 97,
       108, 97, 146, 121, 143, 142, 105, 98, 136, 114, 118, 109, 97, 150, 71,
       52, 29, 44, 47, 35, 42, 31, 38, 31, 30, 28, 27, 22, 17, 22, 11, 7,
       13, 10, 14, 13, 11, 8, 3, 7, 6, 9, 7, 4, 6, 5, 3, 5)

# Fitting the model
mod3 <- gamlss(y~1, sigma.fo=~1, family=DMOLBE,
               control=gamlss.control(n.cyc=500, trace=FALSE))

summary(mod3)

# Extracting the fitted values for mu and sigma
# using the inverse link function
mu_hat <- exp(coef(mod3, what="mu"))
mu_hat
sigma_hat <- exp(coef(mod3, what="sigma"))
sigma_hat

# Example 4
# Data Set II (daily death due to coronavirus in Pakistan). The second data
# set is the daily deaths due to coronavirus in Pakistan from 18 March
# to 30 June. The data sets used in the paper was collected from 2020 year.
# The data is reported in
# https://www.worldometers.info/coronavirus/country/Pakistan.
# The data are:

y <- c(1, 6, 6, 4, 4, 4, 1, 20, 5, 2, 3, 15, 17, 7, 8, 25, 8, 25, 11,
       25, 16, 16, 12, 11, 20, 31, 42, 32, 23, 17, 19, 38, 50, 21, 14,
       37, 23, 47, 31, 24, 9, 64, 39, 30, 36, 46, 32, 50, 34, 32, 34,
       30, 28, 35, 57, 78, 88, 60, 78, 67, 82, 68, 97, 67, 65, 105,
```

```
       83, 101, 107, 88, 178, 110, 136, 118, 136, 153, 119, 89, 105,
       60, 148, 59, 73, 83, 49, 137, 91)

# Fitting the model
mod4 <- gamlss(y~1, sigma.fo=~1, family=DMOLBE,
               control=gamlss.control(n.cyc=500, trace=FALSE))

summary(mod4)

# Extracting the fitted values for mu and sigma
# using the inverse link function
mu_hat <- exp(coef(mod4, what="mu"))
mu_hat
sigma_hat <- exp(coef(mod4, what="sigma"))
sigma_hat
```

DPERKS *The Discrete Perks family*

Description

The function `DPERKS()` defines the Discrete Perks distribution a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
DPERKS(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The discrete Perks distribution with parameters $\mu > 0$ and $\sigma > 0$ has a support 0, 1, 2, ... and density given by

$f(x|\mu,\sigma) = \frac{\mu(1+\mu)(e^{\sigma}-1)e^{\sigma x}}{(1+\mu e^{\sigma x})(1+\mu e^{\sigma(x+1)})}$

Note: in this implementation we changed the original parameters λ for μ and β for σ, we did it to implement this distribution within gamlss framework.

Author(s)

Veronica Seguro Varela, <vseguro@unal.edu.co>

References

Tyagi, A., Choudhary, N., & Singh, B. (2020). A new discrete distribution: Theory and applications to discrete failure lifetime and count data. J. Appl. Probab. Statist, 15, 117-143.

See Also

dDPERKS.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(123)
y <- rDPERKS(n=1000, mu=2.5, sigma=0.4)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, family=DPERKS,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ DPERKS
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(-1.6 + 5 * x1)
  sigma <- exp(1.7 - 5 * x2)
  y <- rDPERKS(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(12345)
datos <- gendat(n=1000)

mod2 <- NULL
mod2 <- gamlss(y~x1, sigma.fo=~x2, family=DPERKS, data=datos,
                control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)

# Example 3
# The dataset comes from Tyagi et al. (2020) page 21
# The dataset contains the number of outbreaks of strikes in the
# UK coal mining industries in four successive week periods
# in the year 1948-59.
y <- rep(0:4, times=c(46, 76, 24, 9, 1))

# Fitting the model
library(gamlss)
```

```
mod3 <- gamlss(y~1, family=DPERKS,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

# Example 4
# The dataset comes from Tyagi et al. (2020) page 21
# The dataset contains the number fishes caught
# in traps (David, 1971, pg. 168).
y <- rep(0:9, times=c(1, 2, 11, 20, 29, 23, 10, 3, 1, 0))

# Fitting the model
library(gamlss)
mod4 <- gamlss(y~1, family=DPERKS,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod4, what="mu"))
exp(coef(mod4, what="sigma"))

# Example 5
# The dataset comes from Tyagi et al. (2020) page 24
# This dataset consists of remission times in weeks
# for 20 leukemia patients randomly assigned to a certain treatment
y <- c(1, 3, 3, 6, 7, 7, 10, 12, 14, 15, 18,
       19, 22, 26, 28, 29, 34, 40, 48, 49)

# Fitting the model
library(gamlss)
mod4 <- gamlss(y~1, family=DPERKS)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod4, what="mu"))
exp(coef(mod4, what="sigma"))
```

---

dPOISXL *The Discrete Poisson XLindley*

Description

These functions define the density, distribution function, quantile function and random generation for the Discrete Poisson XLindley distribution with parameter μ.

Usage

```
dPOISXL(x, mu = 0.3, log = FALSE)

pPOISXL(q, mu = 0.3, lower.tail = TRUE, log.p = FALSE)

qPOISXL(p, mu = 0.3, lower.tail = TRUE, log.p = FALSE)

rPOISXL(n, mu = 0.3)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, P[X > x].
p	vector of probabilities.
n	number of random values to return

Details

The Discrete Poisson XLindley distribution with parameters μ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu) = \frac{\mu^2(x+\mu^2+3(1+\mu))}{(1+\mu)^{4+x}}$; with $\mu > 0$.

Note: in this implementation we changed the original parameters α for μ, we did it to implement this distribution within gamlss framework.

Value

dPOISXL gives the density, pPOISXL gives the distribution function, qPOISXL gives the quantile function, rPOISXL generates random deviates.

Author(s)

Mariana Blandon Mejia, <mblandonm@unal.edu.co>

References

Ahsan-ul-Haq, M., Al-Bossly, A., El-Morshedy, M., & Eliwa, M. S. (2022). Poisson XLindley distribution for count data: statistical and reliability properties with estimation techniques and inference. Computational Intelligence and neuroscience, 2022(1), 6503670.

See Also

POISXL.

Examples

```
# Example 1
# Plotting the mass function for different parameter values

x_max <- 20
probs1 <- dPOISXL(x=0:x_max, mu=0.2)
probs2 <- dPOISXL(x=0:x_max, mu=0.5)
probs3 <- dPOISXL(x=0:x_max, mu=1.0)

# To plot the first k values
plot(x=0:x_max, y=probs1, type="o", lwd=2, col="dodgerblue", las=1,
     ylab="P(X=x)", xlab="X", main="Probability for Poisson XLindley",
     ylim=c(0, 0.50))
points(x=0:x_max, y=probs2, type="o", lwd=2, col="tomato")
points(x=0:x_max, y=probs3, type="o", lwd=2, col="green4")
legend("topright", col=c("dodgerblue", "tomato", "green4"), lwd=3,
       legend=c("mu=0.2", "mu=0.5", "mu=1.0"))

# Example 2
# Checking if the cumulative curves converge to 1

x_max <- 20

plot_discrete_cdf(x=0:x_max,
                  fx=dPOISXL(x=0:x_max, mu=0.2), col="dodgerblue",
                  main="CDF for Poisson XLindley with mu=0.2")

plot_discrete_cdf(x=0:x_max,
                  fx=dPOISXL(x=0:x_max, mu=0.5), col="tomato",
                  main="CDF for Poisson XLindley with mu=0.5")

plot_discrete_cdf(x=0:x_max,
                  fx=dPOISXL(x=0:x_max, mu=1.0), col="green4",
                  main="CDF for Poisson XLindley with mu=1.0")

# Example 3
# Comparing the random generator output with
# the theoretical probabilities

x_max <- 15
probs1 <- dPOISXL(x=0:x_max, mu=0.3)
names(probs1) <- 0:x_max

x <- rPOISXL(n=3000, mu=0.3)
probs2 <- prop.table(table(x))

cn <- union(names(probs1), names(probs2))
height <- rbind(probs1[cn], probs2[cn])
mp <- barplot(height, beside = TRUE, names.arg = cn,
              col=c("dodgerblue3","firebrick3"), las=1,
              xlab="X", ylab="Proportion")
legend("topright",
```

```
        legend=c("Theoretical", "Simulated"),
        bty="n", lwd=3,
        col=c("dodgerblue3","firebrick3"), lty=1)

# Example 4
# Checking the quantile function

mu <- 0.3
p <- seq(from=0, to=1, by = 0.01)
qxx <- qPOISXL(p, mu, lower.tail = TRUE, log.p = FALSE)
plot(p, qxx, type="s", lwd=2, col="green3", ylab="quantiles",
     main="Quantiles for Poisson XLindley mu=0.3")
```

DsPA *Discrete power-Ailamujia distribution*

Description

The function `DsPA()` defines the discrete power-Ailamujia distribution a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
DsPA(mu.link = "log", sigma.link = "logit")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "logit" link as the default for the sigma parameter. Other links are "probit" and "cloglog"'(complementary log-log).

Details

The discrete power-Ailamujia distribution with parameters μ and σ has a support 0, 1, 2, ... and density given by

$f(x|\mu,\sigma) = (\sigma^x)^\mu(1 - x^\mu \log(\lambda)) - (\sigma^{(x+1)})^\mu(1 - (x+1)^\mu \log(\lambda))$

Note: in this implementation we changed the original parameters β and λ for μ and σ respectively, we did it to implement this distribution within gamlss framework.

Value

Returns a `gamlss.family` object which can be used to fit a discrete power-Ailamujia distribution in the `gamlss()` function.

Author(s)

Maria Camila Mena Romana, <mamenar@unal.edu.co>

References

Alghamdi, A. S., Ahsan-ul-Haq, M., Babar, A., Aljohani, H. M., Afify, A. Z., & Cell, Q. E. (2022). The discrete power-Ailamujia distribution: properties, inference, and applications. AIMS Math, 7(5), 8344-8360.

See Also

dDsPA.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rDsPA(n=100, mu=1.2, sigma=0.5)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, family=DsPA,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))

exp(coef(mod1, what="mu"))
inv_logit(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ DsPA
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  x3 <- runif(n)
  x4 <- runif(n)
  mu    <- exp(1 + 1.2*x1 + 0.2*x2)
  sigma <- inv_logit(2 + 1.5*x3 + 1.5*x4)
  y <- rDsPA(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2, x3=x3, x4=x4)
}

set.seed(123)
datos <- gendat(n=100)

mod2 <- gamlss(y~x1+x2, sigma.fo=~x3+x4, family=DsPA, data=datos,
               control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)

# Example 3
```

```
# failure times for a sample of 15 electronic components in an acceleration life test
# Taken from
# Alghamdi et. al (202) page 8354.

y <- c(1.0, 5.0, 6.0, 11.0, 12.0, 19.0, 20.0, 22.0,
       23.0, 31.0, 37.0, 46.0, 54.0, 60.0, 66.0)

mod3 <- gamlss(y~1, family=DsPA,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))

exp(coef(mod3, what="mu"))
inv_logit(coef(mod3, what="sigma"))

# Example 4
# number of fires in Greece from July 1, 1998 to August 31, 1998.
# Taken from
# Alghamdi et. al (202) page 8354.

y <- c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
       0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1,
       1, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2,
       2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3,
       3, 3, 3, 3, 3, 3, 3, 3, 4, 4, 4,
       4, 4, 4, 4, 4, 4, 4, 4, 5, 5, 5,
       5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 6,
       6, 6, 6, 6, 6, 6, 6, 7, 7, 7, 7,
       8, 8, 8, 8, 8, 8, 8, 8, 8, 9, 9,
       9, 9, 9, 9, 10, 10, 10, 11, 11,
       11, 11, 12, 12, 12, 12, 12, 12,
       15, 15, 15, 15, 16, 20, 43)

mod4 <- gamlss(y~1, family=DsPA,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))

exp(coef(mod4, what="mu"))
inv_logit(coef(mod4, what="sigma"))
```

GGEO *The GGEO family*

Description

The function GGEO() defines the Generalized Geometric distribution a two parameter distribution, for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
GGEO(mu.link = "logit", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "logit" link as the default for the sigma. Other links are "probit" and "cloglog"'(complementary log-log)

Details

The GGEO distribution with parameters μ and σ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu,\sigma) = \frac{\sigma\mu^x(1-\mu)}{(1-(1-\sigma)\mu^{x+1})(1-(1-\sigma)\mu^x)}$

with $0 < \mu < 1$ and $\sigma > 0$. If $\sigma = 1$, the GGEO distribution reduces to the geometric distribution with success probability $1 - \mu$.

Value

Returns a gamlss.family object which can be used to fit a GGEO distribution in the gamlss() function.

Author(s)

Valentina Hurtado Sepúlveda, <vhurtados@unal.edu.co>

References

Gómez-Déniz, E. (2010). Another generalization of the geometric distribution. Test, 19, 399-415.

See Also

dGGEO.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(123)
y <- rGGEO(n=200, mu=0.95, sigma=1.5)

# Fitting the model
library(gamlss)
```

```
mod1 <- gamlss(y~1, family=GGEO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))

inv_logit(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ GGEO
## Not run:
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- inv_logit(1.7 - 2.8*x1)
  sigma <- exp(0.73 + 1*x2)
  y <- rGGEO(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(78353)
datos <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2, family=GGEO, data=datos,
               control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)

## End(Not run)

# Example 3
# Number of accidents to 647 women working on H. E. Shells
# for 5 weeks. Taken from Gomez-Deniz (2010) page 411.

y <- rep(x=0:5, times=c(447, 132, 42, 21, 3, 2))

mod3 <- gamlss(y~1, family=GGEO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))

inv_logit(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

# Example 4
# Total number of carious teeth among the four deciduous molars
# Taken from Gomez-Deniz (2010) page 412.
```

```
y <- rep(x=0:4, times=c(64, 17, 10, 6, 3))

mod4 <- gamlss(y~1, family=GGEO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))

inv_logit(coef(mod4, what="mu"))
exp(coef(mod4, what="sigma"))

# Example 5
# Results of ten shots fired from a rifle at each of 100 targets.
# Taken from Gomez-Deniz (2010) page 412.

y <- rep(x=0:10, times=c(0, 2, 4, 10, 22, 26, 18, 12, 4, 2, 0))

mod5 <- gamlss(y~1, family=GGEO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))

inv_logit(coef(mod5, what="mu"))
exp(coef(mod5, what="sigma"))

# Example 6
# Fish catch data in Kemp (1992).
# Taken from Gomez-Deniz (2010) page 412.

y <- rep(x=0:9, times=c(1, 2, 11, 20, 29, 23, 10, 3, 1, 0))

mod6 <- gamlss(y~1, family=GGEO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
inv_logit <- function(x) 1/(1 + exp(-x))

inv_logit(coef(mod6, what="mu"))
exp(coef(mod6, what="sigma"))
```

---

grazing *grazing dataset*

Description

In this experiment, the density of understorey birds at a series of sites in two areas either side of a stockproof fence were compared. Once side had limited grazing (mainly from native herbivores), and the other was heavily grazed by feral herbivores, mostly horses. Bird counts were done at the sites either side of the fence (the Before measurements). Then the herbivores were removed, and bird counts done again (the After measurements). The measurements are the total number of understorey-foraging birds observed in three 20-minute surveys of two hectare quadrats.

Usage

```
grazing
```

Format

`grazing`**:**
A data frame with 62 rows and 3 variables:

when when the bird count was conducted

grazed a factor with levels Reference and Feral

birds the number of understorey birds ...

Author(s)

Rodrigo Matheus

Source

https://github.com/rdmatheus/bergreg

`HYPERPO` *The hyper Poisson family*

Description

The function `HYPERPO()` defines the hyper Poisson distribution a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
HYPERPO(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The hyper-Poisson distribution with parameters μ and σ has a support 0, 1, 2, ... and density given by

$f(x|\mu,\sigma) = \frac{\mu^x}{{}_1F_1(1;\mu;\sigma)} \frac{\Gamma(\sigma)}{\Gamma(x+\sigma)}$

where the function ${}_1F_1(a;c;z)$ is defined as

${}_1F_1(a;c;z) = \sum_{r=0}^{\infty} \frac{(a)_r}{(c)_r} \frac{z^r}{r!}$

and $(a)_r = \frac{\gamma(a+r)}{\gamma(a)}$ for $a > 0$ and r positive integer.

Note: in this implementation we changed the original parameters λ and γ for μ and σ respectively, we did it to implement this distribution within gamlss framework.

Value

Returns a `gamlss.family` object which can be used to fit a hyper-Poisson distribution in the `gamlss()` function.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Sáez-Castillo, A. J., & Conde-Sánchez, A. (2013). A hyper-Poisson regression model for overdispersed and underdispersed count data. Computational Statistics & Data Analysis, 61, 148-157.

See Also

dHYPERPO.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(1234)
y <- rHYPERPO(n=200, mu=10, sigma=1.5)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=HYPERPO,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model
```

```
# A function to simulate a data set with Y ~ HYPERPO
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(1.21 - 3 * x1) # 0.75 approximately
  sigma <- exp(1.26 - 2 * x2) # 1.30 approximately
  y <- rHYPERPO(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(1234)
dat <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2, family=HYPERPO, data=dat,
                 control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)
```

HYPERPO2 *The hyper Poisson family (with mu as mean)*

Description

The function HYPERPO2() defines the hyper Poisson distribution (with mu as mean) a two parameter distribution, for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
HYPERPO2(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.

Details

The hyper-Poisson distribution with parameters μ and σ has a support 0, 1, 2, ...

Note: in this implementation the parameter μ is the mean of the distribution and σ corresponds to the dispersion parameter. If you fit a model with this parameterization, the time will increase because an internal procedure to convert μ to λ parameter.

Value

Returns a gamlss.family object which can be used to fit a hyper-Poisson distribution version 2 in the gamlss() function.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Sáez-Castillo, A. J., & Conde-Sánchez, A. (2013). A hyper-Poisson regression model for overdispersed and underdispersed count data. Computational Statistics & Data Analysis, 61, 148-157.

See Also

dHYPERPO2, HYPERPO.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(1234)
y <- rHYPERPO2(n=100, mu=4, sigma=1.5)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=HYPERPO2,
               control=gamlss.control(n.cyc=500, trace=TRUE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model

## Not run:
# A function to simulate a data set with Y ~ HYPERPO2
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(1.21 - 3 * x1) # 0.75 approximately
  sigma <- exp(1.26 - 2 * x2) # 1.30 approximately
  y <- rHYPERPO2(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(12345)
dat <- gendat(n=200)

mod2 <- gamlss(y~x1, sigma.fo=~x2, family=HYPERPO2, data=dat,
               control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)
```

```
## End(Not run)
```

`mean_var_hp` *Mean and variance for hyper-Poisson distribution*

Description

This function calculates the mean and variance for the hyper-Poisson distribution with parameters μ and σ.

Usage

```
mean_var_hp(mu, sigma)

mean_var_hp2(mu, sigma)
```

Arguments

`mu`	value of the mu parameter.
`sigma`	value of the sigma parameter.

Details

The hyper-Poisson distribution with parameters μ and σ has a support 0, 1, 2, ... and density given by

$f(x|\mu,\sigma) = \frac{\mu^x}{{}_1F_1(1;\mu;\sigma)} \frac{\Gamma(\sigma)}{\Gamma(x+\sigma)}$

where the function ${}_1F_1(a;c;z)$ is defined as

${}_1F_1(a;c;z) = \sum_{r=0}^{\infty} \frac{(a)_r}{(c)_r} \frac{z^r}{r!}$

and $(a)_r = \frac{\gamma(a+r)}{\gamma(a)}$ for $a > 0$ and r positive integer.

This function calculates the mean and variance of this distribution.

Value

the function returns a list with the mean and variance.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Sáez-Castillo, A. J., & Conde-Sánchez, A. (2013). A hyper-Poisson regression model for overdispersed and underdispersed count data. Computational Statistics & Data Analysis, 61, 148-157.

See Also

HYPERPO.

Examples

```
# Example 1

# Theoretical values
mean_var_hp(mu=5.5, sigma=0.1)

# Using simulated values
y <- rHYPERPO(n=1000, mu=5.5, sigma=0.1)
mean(y)
var(y)


# Example 2

# Theoretical values
mean_var_hp2(mu=5.5, sigma=1.9)

# Using simulated values
y <- rHYPERPO2(n=1000, mu=5.5, sigma=1.9)
mean(y)
var(y)
```

---

plot_discrete_cdf *Draw the CDF for a discrete random variable*

Description

Draw the CDF for a discrete random variable

Usage

```
plot_discrete_cdf(x, fx, col = "blue", lwd = 3, ...)
```

Arguments

x	vector with the values of the random variable X.
fx	vector with the probabilities of X.
col	color for the line.
lwd	line width.
...	further arguments and graphical parameters.

Value

A plot with the cumulative distribution function.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

Examples

```
# Example 1
# for a particular distribution

x <- 1:6
fx <- c(0.19, 0.21, 0.4, 0.12, 0.05, 0.03)
plot_discrete_cdf(x, fx, las=1, main="")

# Example 2
# for a Poisson distribution
x <- 0:10
fx <- dpois(x, lambda=3)
plot_discrete_cdf(x, fx, las=1,
                  main="CDF for Poisson")
```

POISXL *The Discrete Poisson XLindley*

Description

The function POISXL() defines the Discrete Poisson XLindley distribution a single parameter distribution, for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
POISXL(mu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.

Details

The Discrete Poisson XLindley distribution with parameters μ has a support 0, 1, 2, ... and mass function given by

$f(x|\mu) = \frac{\mu^2(x+\mu^2+3(1+\mu))}{(1+\mu)^{4+x}}$; with $\mu > 0$.

Note: in this implementation we changed the original parameters α for μ, we did it to implement this distribution within gamlss framework.

Value

Returns a gamlss.family object which can be used to fit a Discrete Poisson XLindley distribution in the gamlss() function.

Author(s)

Mariana Blandon Mejia, <mblandonm@unal.edu.co>

References

Ahsan-ul-Haq, M., Al-Bossly, A., El-Morshedy, M., & Eliwa, M. S. (2022). Poisson XLindley distribution for count data: statistical and reliability properties with estimation techniques and inference. Computational Intelligence and neuroscience, 2022(1), 6503670.

See Also

dPOISXL.

Examples

```
# Example 1
# Generating some random values with
# known mu
y <- rPOISXL(n=1000, mu=1)

# Fitting the model
library(gamlss)
mod1 <- gamlss(y~1, family=POISXL,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
# using the inverse link function
exp(coef(mod1, what="mu"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ POISXL
gendat <- function(n) {
  x1 <- runif(n, min=0.4, max=0.6)
  mu <- exp(1.21 - 3 * x1) # 0.75 approximately
  y <- rPOISXL(n=n, mu=mu)
  data.frame(y=y, x1=x1)
}

dat <- gendat(n=1500)

# Fitting the model
mod2 <- NULL
mod2 <- gamlss(y~x1, family=POISXL, data=dat,
               control=gamlss.control(n.cyc=500, trace=FALSE))

summary(mod2)

# Example 3
# The counts the number of borers per hill of corn in an
# experiment conducted randomly on 8 hills in 15 replications.
```

```
# Taken from Ahsan-ul-Haq et al (2022) page 10.

y <- rep(x=0:8, times=c(43, 35, 17, 11, 5, 4, 1, 2, 2))

mod3 <- gamlss(y~1, family=POISXL,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
exp(coef(mod3, what="mu"))

# Example 4
# The number of mammalian cytogenetic dosimetry lesions produced
# by streptogramin exposure in rabbit.
# Taken from Ahsan-ul-Haq et al (2022) page 10.

y <- rep(x=0:4, times=c(200, 57, 30, 7, 6))

mod4 <- gamlss(y~1, family=POISXL,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu
exp(coef(mod4, what="mu"))
```

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