

Package ‘MaOEA’

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Type Package

Title Many Objective Evolutionary Algorithm

Version 0.6.2

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Description A set of evolutionary algorithms to solve many-objective optimization. Hybridization between the algorithms are also facilitated. Available algorithms are: 'SMS-EMOA' <[doi:10.1016/j.ejor.2006.08.008](https://doi.org/10.1016/j.ejor.2006.08.008)> 'NSGA-III' <[doi:10.1109/TEVC.2013.2281535](https://doi.org/10.1109/TEVC.2013.2281535)> 'MO-CMA-ES' <[doi:10.1145/1830483.1830573](https://doi.org/10.1145/1830483.1830573)> The following many-objective benchmark problems are also provided: 'DTLZ1'-'DTLZ4' from Deb, et al. (2001) <[doi:10.1007/1-84628-137-7_6](https://doi.org/10.1007/1-84628-137-7_6)> and 'WFG4'-'WFG9' from Huband, et al. (2005) <[doi:10.1109/TEVC.2005.861417](https://doi.org/10.1109/TEVC.2005.861417)>.

License GPL (>= 3)

Encoding UTF-8

LazyData true

BugReports <https://github.com/dots26/MaOEA/issues>

URL <https://github.com/dots26/MaOEA>

RoxygenNote 7.1.1

Imports reticulate, nsga2R, lhs, nnet, stringr, randtoolbox, e1071, MASS, gtools, stats, utils, pracma

Suggests testthat

SystemRequirements Python 3.x with following modules: PyGMO, NumPy, and cloudpickle

NeedsCompilation no

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Description

MaOEA contains several algorithms for solving many-objective optimization problems. The algorithms are provided as a sequence of operators used in a single iteration. For example, the SM-SEMOA function calls the recombination (SBX) and mutation operator (polynomial mutation) to produce 1 offspring, and perform the S-metric selection. The function then returns a list containing the population and population objective after the procedure is conducted once. The purpose of only doing a single iteration is to support users if they wish to formulate hybrid algorithms.

Details

Alternatively, users can use the `optimMaOEA` function to solve an optimization problem with their chosen algorithm. This function is a simple wrapper to call the algorithms listed above for several iterations. Using this function, users can simply supply the initial population, objective function, the chosen algorithm, and the number of iterations. If number of iteration is not supplied, then only a single iteration is conducted.

Note: This package uses column-major ordering, i.e. an individual should be contained in a single column, each row represents different variable. All optimization variable should be scaled to 0-1.

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See Also

Main interface function is [optimMaOEA](#).

AdaptiveNormalization *Objective space normalization.*

Description

Normalize the objectives to 0-1. The origin is the ideal point. (1,...,1) is not the nadir point. The normalization is done by using adaptive normalization used in NSGA-III.

Usage

```
AdaptiveNormalization(objectiveValue)
```

Arguments

objectiveValue Set of objective vectors to normalize

Value

A list containing the following: normalizedObjective The normalized values idealPoint The ideal point corresponding to the origin nadirPoint The location of nadir point in the normalized Space

Examples

```
nObj <- 5
nIndividual <- 100
nVar <- 10
population <- InitializePopulationLHS(nIndividual,nVar,FALSE)
objective <- matrix(,nrow=nObj,ncol=nIndividual)
for(individual in 1:nIndividual){
  objective[,individual] <- WFG4(population[,individual],nObj)
}
AdaptiveNormalization(objective)
```

cmaes_gen

Generator for cmaes_gen class.

Description

Create a list with cmaes_gen class. Basically, the function transform the population into a class that is accepted by the MOCMAES and SMOCMAES function.

Usage

```
cmaes_gen(
  population,
  ps_target = (1/(5 + (1/2)^0.5)),
  stepSize = 0.5,
  evoPath = rep(0, nrow(population)),
  covarianceMatrix = diag(nrow(population))
)
```

Arguments

`population` The number of objective functions. A scalar value.

`ps_target` The target success rate. Used to initialize `cmaes_gen$averageSuccessRate`.

`stepSize` The initial step size.

`evoPath` A vector of numbers indicating evolution path of each variable.

`covarianceMatrix`
Covariance matrix of the variables.

Value

An object of `cmaes_gen` class. It can be used as MO-CMA-ES parent. It is a 5 tuple: `x` (the design point, `length = number of variable`), `averageSuccessRate` (scalar), `stepSize` (scalar), `evoPath` (evolution path, vector, `length = number of variable`), `covarianceMatrix` (square matrix with `ncol = nrow = number of variable`).

Examples

```
nVar <- 14
nObjective <- 5
nIndividual <- 100
crossoverProbability <- 1
ps_target <- 1 / (5 + ( 1 / 2 )^0.5 )
pop <- matrix(stats::runif(nIndividual*nVar), nrow = nVar) # create the population
a_list <- cmaes_gen(pop)
control <- list(successProbTarget=ps_target,crossoverProbability=crossoverProbability)

# run a generation of MO-CMA-ES with standard WFG8 test function.
numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready) # prevent error on testing the example
newGeneration <- MOCMAES(a_list,nObjective,WFG8,control,nObjective)
```

compute_R2HV	<i>Modified powered tchebyscheff R2-indicator designed to approximate HV</i>
--------------	--

Description

Compute the R2-HV from Shang et al.

Usage

```
compute_R2HV(dataPoints, reference, weights = NULL, nPoints = 100)
```

Arguments

dataPoints	The Points coordinate. Each column contains a single point (column major).
reference	The reference point for computing R2-mtch (similar as reference for HV)
weights	The weights/direction to be used to compute the achievement scalarization. Each column contains a single weight vector. If no weight is supplied, weights are generated using Sobol sequences.
nPoints	Used only when no weights are supplied. An input for the weight generator (sobol sequences). This defines how many points are created.

Value

The function return the powered R2-indicator of the set.

References

Ke Shang, Hisao Ishibuchi, Min-Ling Zhang, and Yiping Liu. 2018. A new R2 indicator for better hypervolume approximation. In Proceedings of the Genetic and Evolutionary Computation Conference (GECCO '18), Hernan Aguirre (Ed.). ACM, New York, NY, USA, 745-752. DOI: <https://doi.org/10.1145/3205455.3205543>

Examples

```
nPointToSample <- 100
nObjective <- 3
points <- matrix(runif(nPointToSample*nObjective), nrow = nObjective) # sample the points
ranks <- nsga2R::fastNonDominatedSorting(t(points)) # non-dominated sorting
points <- points[,ranks[[1]],drop=FALSE] # take only the non-dominated front
nPoints <- ncol(points) # check how many points are on the non-dominated front
reference <- rep(2,nObjective)

compute_R2HV(points,reference)
```

compute_R2HVC	<i>Modified tchebyscheff R2-indicator contribution designed to approximate HV</i>
---------------	---

Description

Compute the R2-HVC from Shang et al.

Usage

```
compute_R2HVC(  
    dataPoints,  
    reference,  
    weights = NULL,  
    alpha = 1,  
    nWeight = 300,  
    indexOfInterest = 1:ncol(dataPoints)  
)
```

Arguments

dataPoints	The Points coordinate. Each column contains a single point (column major).
reference	The reference point for computing R2-mtch (similar as reference for HV)
weights	The weights/direction to be used to compute the achievement scalarization. Each column contains a single weight vector. If no weight is supplied, weights are generated using Sobol sequences
alpha	Power factor on the gmtch and g*2tch utility functions.
nWeight	Used only when no weights are supplied. The number of weights generated by sobol sequence.
indexOfInterest	individuals to be evaluated. The R2 values will only be reported/returned for these individuals.

Value

The function return R2-indicator contribution of each point.

References

K. Shang, H. Ishibuchi and X. Ni, "R2-based Hypervolume Contribution Approximation," in IEEE Transactions on Evolutionary Computation. doi: 10.1109/TEVC.2019.2909271

Examples

```

nPointToSample <- 100
nObjective <- 3
points <- matrix(runif(nPointToSample*nObjective), nrow = nObjective) # sample the points
ranks <- nsga2R::fastNonDominatedSorting(t(points)) # non-dominated sorting
points <- points[,ranks[[1]],drop=FALSE] # take only the non-dominated front
nPpoints <- ncol(points) # check how many points are on the non-dominated front
reference <- rep(2,nObjective)

compute_R2HVC(points,reference)

```

compute_R2mtch

Modified tchebyscheff R2-indicator

Description

Compute the R2-mtch indicator from Shang et al.

Usage

```
compute_R2mtch(dataPoints, reference, weights = NULL, nWeight = 100)
```

Arguments

dataPoints	The Points coordinate. Each column contains a single point (column major).
reference	The reference point for computing R2-mtch (similar as reference for HV)
weights	The weights/direction to be used to compute the achievement scalarization. Each column contains a single weight vector. If no weight is supplied, weights are generated using Sobol sequences.
nWeight	Used only when no weights are supplied. An input for the sobol weight generation. This defines how many points to be generated.

Value

The function return the R2-indicator of the set.

References

Ke Shang, Hisao Ishibuchi, Min-Ling Zhang, and Yiping Liu. 2018. A new R2 indicator for better hypervolume approximation. In Proceedings of the Genetic and Evolutionary Computation Conference (GECCO '18), Hernan Aguirre (Ed.). ACM, New York, NY, USA, 745-752. DOI: <https://doi.org/10.1145/3205455.3205543>

Examples

```

nPointToSample <- 100
nObjective <- 3
points <- matrix(runif(nPointToSample*nObjective), nrow = nObjective) # sample the points
ranks <- nsga2R::fastNonDominatedSorting(t(points)) # non-dominated sorting
points <- points[,ranks[[1]],drop=FALSE] # take only the non-dominated front
nPpoints <- ncol(points) # check how many points are on the non-dominated front
reference <- rep(2,nObjective)

compute_R2mtch(points,reference)

```

createWeights	<i>Das and Dennis's structured weight generation, normal boundary intersection (NBI).</i>
---------------	---

Description

Generate a set of weights following Das and Dennis's method. Each column returned is a weight vector.

Usage

```
createWeights(nDim, axisDivision = nDim + 2, noZero = FALSE)
```

Arguments

nDim	The dimensionality of the problem. In EA, usually this is used in the objective space, hence nDim = nObjective
axisDivision	Used only when no weights are supplied. An input for the structured weight distribution. This defines how many division are created in each axis.
noZero	Default to false. If set to TRUE, reference vector containing zero, e.g. (1,0,0) will be removed. Used to generate weight in modified tch method.

Value

The function return a set of weight vectors.

References

Indraneel Das and J. E. Dennis. 1998. Normal-Boundary Intersection: A New Method for Generating the Pareto Surface in Nonlinear Multicriteria Optimization Problems. *SIAM Journal on Optimization* 1998 8:3, 631-657.

Examples

```

nObjective <- 3
axisDiv <- 6

createWeights(nObjective,axisDiv)

```

`createWeightsSobol` *Sobol sequence weights*

Description

Generate a set of weights following Sobol sequence generator

Usage

```
createWeightsSobol(nWeights, nDim, seed = 4177)
```

Arguments

<code>nWeights</code>	Number of weights to generate.
<code>nDim</code>	The dimensionality of the problem. In EA, usually this is used in the objective space, hence <code>nDim = nObjective</code>
<code>seed</code>	Seed for scrambling

Value

The function return a set of weight vectors.

Examples

```
nObjective <- 3
nPoint <- 1000

createWeightsSobol(nPoint,nObjective)
```

`DTLZ1` *The DTLZ1 test function.*

Description

The DTLZ1 test function.

Usage

```
DTLZ1(individual, nObj)
```

Arguments

<code>individual</code>	The vector of individual (or matrix of population) to be evaluated.
<code>nObj</code>	The number of objective

Value

A matrix of size nObjective x population size, containing the objective values for each individual.

References

Deb, K., Thiele, L., Laumanns, M., Zitzler, E.: Scalable Multi-Objective Optimization Test Problems. In: Congress on Evolutionary Computation (CEC). pp. 825–830. IEEE Press, Piscataway, NJ (2002)

Examples

```
individual <- stats::runif(14)
nObj <- 4
DTLZ1(individual,nObj)
```

DTLZ2

The DTLZ2 test function.

Description

The DTLZ2 test function.

Usage

```
DTLZ2(individual, nObj)
```

Arguments

individual The vector of individual (or matrix of population) to be evaluated.
nObj The number of objective

Value

A matrix of size nObjective x population size, containing the objective values for each individual.

References

Deb, K., Thiele, L., Laumanns, M., Zitzler, E.: Scalable Multi-Objective Optimization Test Problems. In: Congress on Evolutionary Computation (CEC). pp. 825–830. IEEE Press, Piscataway, NJ (2002)

Examples

```
individual <- stats::runif(14)
nObj <- 4
DTLZ2(individual,nObj)
```

DTLZ3

The DTLZ3 test function.

Description

The DTLZ3 test function.

Usage

```
DTLZ3(individual, nObj)
```

Arguments

`individual` The vector of individual (or matrix of population) to be evaluated.
`nObj` The number of objective

Value

A matrix of size `nObjective` x population size, containing the objective values for each individual.

References

Deb, K., Thiele, L., Laumanns, M., Zitzler, E.: Scalable Multi-Objective Optimization Test Problems. In: Congress on Evolutionary Computation (CEC). pp. 825–830. IEEE Press, Piscataway, NJ (2002)

Examples

```
individual <- stats::runif(14)
nObj <- 4
DTLZ3(individual,nObj)
```

DTLZ4

The DTLZ4 test function.

Description

The DTLZ4 test function.

Usage

```
DTLZ4(individual, nObj, alpha = 100)
```

Arguments

individual	The vector of individual (or matrix of population) to be evaluated.
nObj	The number of objective
alpha	Alpha value of DTLZ4 function.

Value

A matrix of size nObjective x population size, containing the objective values for each individual.

References

Deb, K., Thiele, L., Laumanns, M., Zitzler, E.: Scalable Multi-Objective Optimization Test Problems. In: Congress on Evolutionary Computation (CEC). pp. 825–830. IEEE Press, Piscataway, NJ (2002)

Examples

```
individual <- stats::runif(14)
nObj <- 4
DTLZ4(individual,nObj)
```

EvaluateIndividual *Evaluate objective values of a single individual*

Description

Evaluate individual with the specified test function. Non-feasible solution are given Inf as objective values.

Usage

```
EvaluateIndividual(individual, fun, ...)
```

Arguments

individual	The individual to be evaluated
fun	A string containing which problem is being solved. Currently available DTLZ1-DTLZ4, WFG4-WFG9.
...	Further parameters used by fun

Value

A matrix of size nObjective, containing the objective values.

Examples

```
individual <- stats::runif(8)
EvaluateIndividual(individual,WFG4,3) # the 3 is passed to WFG4 nObj
```

EvaluatePopulation *Evaluate objective value of a set of individuals*

Description

Evaluate a population with the specified test function. Non-feasible solution are given Inf as objective values.

Usage

```
EvaluatePopulation(pop, fun, ...)
```

Arguments

pop	The population to be evaluated
fun	A string containing which problem is being solved. Currently available in the package: DTLZ1-DTLZ4, WFG4-WFG9.
...	Further parameters used by fun

Value

A matrix of size nObjective, containing the objective values.

Examples

```
pop <- matrix(runif(8*50),nrow=8) # 8 variables, 50 individuals
EvaluatePopulation(pop,WFG4,3) # the 3 is passed to WFG4 nObj
```

GetHVContribution *Get HV contribution of all points.*

Description

Get the hypervolume (HV) contribution of the population. Dominated front will give 0 contribution.

Usage

```
GetHVContribution(
  populationObjective,
  reference = NULL,
  method = "exact",
  ref_multiplier = 1.1
)
```

Arguments

populationObjective The objective value of the corresponding individual
 reference The reference point for computing HV
 method the HV computation method. Currently ignored and uses the WFG exact method.
 ref_multiplier Multiplier to the nadir point for dynamic reference point location

Value

A vector of length ncol(populationObjective)

Examples

```

nObjective <- 5 # the number of objectives
nPoint <- 10 # the number of points that will form the hypervolume
objective <- matrix(stats::runif(nObjective*nPoint), nrow = nObjective, ncol = nPoint)
numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready) # prevent error on testing the example
  GetHypervolume(objective,,"exact") # no reference supplied

reference <- rep(2,nObjective) # create a reference point at (2,2,2,2,2)
if(py_module_ready) # prevent error on testing the example
  GetHVContribution(objective,reference)

```

GetHypervolume	<i>Compute hypervolume</i>
----------------	----------------------------

Description

Compute the hypervolume formed by the points w.r.t. a reference point. If no reference is supplied, use the nadir point*(1.1,...,1.1).

Usage

```

GetHypervolume(
  objective,
  reference = NULL,
  method = "exact",
  ref_multiplier = 1.1
)

```

Arguments

objective	The set of points in the objective space (The objective values). A single column should contain one point, so the size would be numberOfObjective x nPoint, e.g. in 5 objective problem, it is 5 x n.
reference	The reference point for HV computation. A column vector.
method	Exact using WFG method or approximate HV using the method by Bringmann and Friedrich. Default to "exact".
ref_multiplier	Multiplier to the nadir point for dynamic reference point location

Value

Hypervolume size, a scalar value.

Examples

```
nObjective <- 5 # the number of objectives
nPoint <- 10 # the number of points that will form the hypervolume
objective <- matrix(stats::runif(nObjective*nPoint), nrow = nObjective, ncol = nPoint)
numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready) # prevent error on testing the example
  GetHypervolume(objective,,"exact") # no reference supplied

reference <- rep(2,nObjective) # create a reference point at (2,2,2,2,2)
if(py_module_ready) # prevent error on testing the example
  GetHypervolume(objective,reference,"exact") # using reference point
```

 GetIGD

Get IGD value

Description

Get Inverted Generational Distance (IGD) value of the population objective w.r.t. a matrix of reference set (each row contain 1 point).

Usage

```
GetIGD(populationObjective, referenceSet)
```

Arguments

populationObjective	The objective value of the corresponding individual
referenceSet	The reference points for computing IGD

Value

The IGD metric. A Scalar value.

GetLeastContribution *Get least HV contribution*

Description

Get the hypervolume (HV) contribution of the individual with least HV contribution.

Usage

```
GetLeastContribution(
  populationObjective,
  reference = NULL,
  method = "exact",
  ref_multiplier = 1.1
)
```

Arguments

populationObjective	The objective value of the corresponding individual
reference	The reference point for computing HV
method	the HV computation method
ref_multiplier	Multiplier to the nadir point for dynamic reference point location

Value

The HV contribution value of the least contributor.

Examples

```
nObjective <- 5 # the number of objectives
nPoint <- 10 # the number of points that will form the hypervolume
objective <- matrix(stats::runif(nObjective*nPoint), nrow = nObjective, ncol = nPoint)
numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready) # prevent error on testing the example
  GetHypervolume(objective,,"exact") # no reference supplied

reference <- rep(2,nObjective) # create a reference point at (2,2,2,2,2)
if(py_module_ready) # prevent error on testing the example
  GetLeastContribution(objective,reference,"exact")
```

GetLeastContributor *Get least HV contributor*

Description

Get index of the individual with least hypervolume (HV) contribution. For the contribution itself, use GetLeastContribution()

Usage

```
GetLeastContributor(
  populationObjective,
  reference = NULL,
  method = "exact",
  hypervolumeMethodParam = list(),
  ref_multiplier = 1.1
)
```

Arguments

populationObjective	The objective value of the corresponding individual
reference	The reference point for computing HV
method	the HV computation method
hypervolumeMethodParam	A list of parameters to be passed to the hypervolumeMethod
ref_multiplier	Multiplier to the nadir point for dynamic reference point location

Value

The index of the least contributor, an integer.

Examples

```
nObjective <- 5 # the number of objectives
nPoint <- 10 # the number of points that will form the hypervolume
objective <- matrix(stats::runif(nObjective*nPoint), nrow = nObjective, ncol = nPoint)
# run a generation of MO-CMA-ES with standard WFG8 test function.
numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready) # prevent error on testing the example
GetHypervolume(objective,,"exact") # no reference supplied

reference <- rep(2,nObjective) # create a reference point at (2,2,2,2,2)
if(py_module_ready) # prevent error on testing the example
GetLeastContributor(objective,reference,"exact")
```

`InitializePopulationLHS`*Initialize population with Latin Hypercube Sampling*

Description

Create initial sample using Latin Hypercube Sampling (LHS) method. The variables will be ranged between 0-1

Usage

```
InitializePopulationLHS(  
  numberOfIndividuals,  
  chromosomeLength,  
  minVal = 0,  
  maxVal = 1,  
  samplingMethod = 0  
)
```

Arguments

<code>numberOfIndividuals</code>	The number of individual in the population (ncol). Integer > 0.
<code>chromosomeLength</code>	The number of variables per individual (nrow)
<code>minVal</code>	Minimum value of the resulting sample
<code>maxVal</code>	Maximum value of the resulting sample
<code>samplingMethod</code>	Not used

Value

A matrix of size `chromosomeLength` x `nIndividual`.

Examples

```
nVar <- 14  
nIndividual <- 100  
InitializePopulationLHS(nIndividual,nVar,FALSE)
```

install_python_dependencies

Install python modules required by MaOEA: numpy and PyGMO

Description

Install the required python package via conda.

Usage

```
install_python_dependencies(conda = "auto", envname = NULL, ...)
```

Arguments

conda	Default: auto
envname	Python virtual environment where the modules will be installed, default to 'r-reticulate'
...	Further argument to pass to reticulate::py_install

Value

0 if dependencies installed and loaded successfully, 1 if fails.

load_python_dependencies

Install python modules required by MaOEA: numpy and PyGMO

Description

Import the required python package if it fails onLoad.

Usage

```
load_python_dependencies()
```

Value

0 if dependencies loaded successfully, 1 if fails.

Description

Do an iteration of population based Multi-Objective Covariance Matrix Adaptation Evolution Strategy (MO-CMA-ES). The variation is using simulated binary crossover (SBX) and mutation following the CMA. The original MO-CMA-ES does not use crossover, to do this simply set crossover-Probability to zero.

Usage

```
MOCMAES(parent, nObjective, fun, control = list(), ...)
```

Arguments

parent	The parent generation, an object of class <code>cmaes_gen</code> . The MO-CMA-ES parent is a 5 tuple: <code>x</code> (the design point, length = number of variable), <code>averageSuccessRate</code> (scalar), <code>stepSize</code> (scalar), <code>evoPath</code> (evolution path, vector, length = number of variable), <code>covarianceMatrix</code> (square matrix with <code>ncol</code> = <code>nrow</code> = number of variable). The parent is then should be a vector of lists (see example).
nObjective	The number of objective functions. A scalar value.
fun	Objective function being solved.
control	List of parameters for CMA-ES. Available control are as follows: <code>successProbTarget</code> Target success probability <code>successProbThreshold</code> The threshold for success probability. If the average success probability is higher than this value, the success rate growth is slowed. <code>crossoverProbability</code> The probability of doing crossover. Should be between 0-1. Negative value will behave like a zero, and values larger than 1 will behave like 1. Default to 1. <code>crossoverDistribution</code> The distribution index for SBX. Larger index makes the distribution sharper around each parent.
...	Further arguments to be passed to fun

Value

Returns a list for the next generation. It contains `list$new_generation` (class: `cmaes_gen`), `list$population` (basically a copy of `list$new_generation[[]]$x`), and `list$populationObjective`

References

Voß, T., Hansen, N., Igel, C.: Improved step size adaptation for the MO-CMA-ES. In: Genetic and Evolutionary Computation (GECCO). pp. 487–494. ACM, New York, NY (2010)

Examples

```

nVar <- 14
nObjective <- 5
nIndividual <- 100
crossoverProbability <- 1
ps_target <- 1 / ( 5 + ( 1 / 2 )^0.5 )
pop <- matrix(stats::runif(nIndividual*nVar), nrow = nVar) # create the population
a_list <- cmaes_gen(pop)
control <- list(successProbTarget=ps_target,crossoverProbability=crossoverProbability)

# run a generation of MO-CMA-ES with standard WFG8 test function.
numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready) # prevent error on testing the example
newGeneration <- MOCMAES(a_list,nObjective,WFG8,control,nObjective)

```

Normalize

Objective space normalization.

Description

Normalize the objectives AND reference (combined) to 0-1. The origin is the ideal point. (1,...,1) is the nadir.

Usage

```
Normalize(objectiveValue, referencePoints = NULL)
```

Arguments

`objectiveValue` Set of objective vectors to normalize

`referencePoints`

Set of reference points to transform following the objective vector normalization

Value

A list containing the following: `normalizedObjective` The normalized values `idealPoint` The ideal point corresponding to the origin transformed `referencePoints` The location of reference points in the normalized Space

Examples

```

nObj <- 5
nVar <- 10
nIndividual <- 100
population <- InitializePopulationLHS(nIndividual,nVar,FALSE)
objective <- matrix(,nrow=nObj,ncol=nIndividual)

```

```

for(individual in 1:nIndividual){
  objective[,individual] <- WFG4(population[,individual],nObj)
}
Normalize(objective)

```

NSGA3

*Elitist Non-dominated Sorting Genetic Algorithm version III***Description**

Do an iteration of Elitist Non-dominated Sorting Genetic Algorithm version III (NSGA-III). The variation is using SBX and polynomial mutation.

Usage

```
NSGA3(population, fun, nObjective, control = list(), ...)
```

Arguments

population	The parent generation. One individual per column. nrow = number of variable, ncol = number of individuals in the population.
fun	Objective function being solved. Currently available in the package DTLZ1-DTLZ4, WFG4-WFG9.
nObjective	The number of objective functions. A scalar value. Needed to generate weight vectors.
control	A list, containing the following: <code>weightVector</code> NSGA-III require a set of reference points defined a priori. The reference can be any point. If not supplied, $5 \cdot nObjective$ points are generated from a sobol sequence. Column major: nrow = nObjective, ncol = number of reference points <code>crossoverProbability</code> The probability of doing crossover. Should be between 0-1. Negative value will behave like a zero, and values larger than 1 will behave like 1. Default to 1. <code>mutationProbability</code> The probability of doing mutation. Should be between 0-1. Negative value will behave like a zero, and values larger than 1 will behave like 1. Default to 1 <code>mutationDistribution</code> The distribution index for polynomial mutation. Larger index makes the distribution sharper around the parent. <code>crossoverDistribution</code> The distribution index for SBX. Larger index makes the distribution sharper around each parent.
...	Further arguments to be passed to fun

Value

#' @return Returns a list for the next generation `population` The new generation design points. Column major. `populationObjective` The new generation's objective values. Column major.

References

Deb, K., Jain, H.: An evolutionary many-objective optimization algorithm using reference-point-based nondominated sorting approach, part I: Solving problems with box constraints. *Trans. Evol. Comp.* 18 (4), 577–601 (2014)

Examples

```
nVar <- 14
nObjective <- 5
nIndividual <- 100
#control for NSGA3
ctrl <- list(crossoverProbability = 1,
            mutationProbability = 1/nVar)
#Initial population
population <- matrix(runif(nIndividual*nVar), nrow = nVar)

# run a generation of NSGA-III with standard WFG8 test function.
NSGA3(population, WFG8, nObjective, ctrl, nObjective)
```

optimMaOEA

Elitist Non-dominated Sorting Genetic Algorithm version III

Description

Main interface for the many-objective optimization evolutionary algorithm (MaOEA) package.

Usage

```
optimMaOEA(
  x = NULL,
  fun,
  solver = NSGA3,
  nObjective,
  nGeneration = 1,
  nVar = nrow(x),
  populationSize = ncol(x),
  seed = 2000,
  control = list(),
  ...
)
```

Arguments

x	The initial population. If not supplied, will be generated using LHS. Column major, each column contain one entry.
fun	Objective function being solved.

solver	Function name of the solver. Currently available: SMSEMOA, MOCMAES, SMOcMAES, and NSGA3.
nObjective	The number of objective functions. A scalar value.
nGeneration	Optional, the number of generation the solver should run.
nVar	Number of variables, will be used if x is not given.
populationSize	Number of individuals in the population, will be used if x is not given.
seed	random number seed for reproduction of code
control	A list, containing the following: <code>weightVectorSet</code> A set of weight vector for the optimizer. The weight vector can be any point in the objective space. If not supplied, $5 \times nObjective$ points are generated from a sobol sequence. Size: <code>nrow = nObjective, ncol = number of weight vectors</code> <code>crossoverProbability</code> The probability of doing crossover. Should be between 0-1. Negative value will behave like a zero, and values larger than 1 will behave like 1. Default to 1. <code>mutationProbability</code> The probability of doing mutation. Should be between 0-1. Negative value will behave like a zero, and values larger than 1 will behave like 1. Default to 1 <code>WFGScaling</code> The use of scaling factor in WFG. Will be ignored in DTLZ problems. Without the scaling, the Pareto front would be on the all-positive portion of hypersphere with radius 1. <code>mutationDistribution</code> The distribution index for polynomial mutation. Larger index makes the distribution sharper around the parent. <code>crossoverDistribution</code> The distribution index for SBX. Larger index makes the distribution sharper around each parent.
...	Further arguments to be passed to fun

Value

Returns a list for the next generation `population` The new generation design points. `populationObjective` The new generation's objective values.

Examples

```
nVar <- 14
nObjective <- 5
nIndividual <- 100
#control for NSGA3
ctrl <- list(crossoverProbability = 1,
            mutationProbability = 1/nVar)
#Initial population can be supplied, like below but for this example, we skip it
#population <- matrix(runif(nIndividual*nVar), nrow = nVar)

numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready){ # prevent error on testing the example
# Hybrid NSGA-III and SMSEMOA example
# 2 calls for nObjective. 1 for optimMaOEA, 1 for WFG8
# generate initial population and run 10 gen. NSGA-III with standard WFG8 test function.
newPop <- optimMaOEA( , WFG8,NSGA3,nObjective,10,nVar,nIndividual,,ctrl,nObjective)$x
```

```
# run 5 generations of SMSEMOA with standard WFG8 test function starting with newPop.
result <- optimMaOEA( newPop, WFG8,SMSEMOA,nObjective,5,,1000,ctrl,nObjective)
finalPop <- result$x
finalObjective <- result$y
}
```

SMOCMAES

*Steady-state Multi-Objective CMA-ES***Description**

Do an iteration of population based steady state Multi-Objective Covariance Matrix Adaptation Evolution Strategy (MO-CMA-ES). The variation is using simulated binary crossover (SBX) and mutation following the CMA. The original MO-CMA-ES does not use crossover, to do this simply set `crossoverProbability` to zero.

Usage

```
SMOCMAES(parent, nObjective, fun, control = list(), ...)
```

Arguments

<code>parent</code>	The parent generation, an object of class <code>cmaes_gen</code> . The MO-CMA-ES parent is a 5 tuple: <code>x</code> (the design point, <code>length = number of variable</code>), <code>averageSuccessRate</code> (scalar), <code>stepSize</code> (scalar), <code>evoPath</code> (evolution path, vector, <code>length = number of variable</code>), <code>covarianceMatrix</code> (square matrix with <code>ncol = nrow = number of variable</code>). The parent is then should be a vector of lists (see example).
<code>nObjective</code>	The number of objective functions. A scalar value.
<code>fun</code>	Objective function being solved.
<code>control</code>	List of parameters for CMA-ES. Available control are as follows: <code>successProbTarget</code> Target success probability <code>successProbThreshold</code> The threshold for success probability. If the average success probability is higher than this value, the success rate growth is slowed. <code>crossoverProbability</code> The probability of doing crossover. Should be between 0-1. Negative value will behave like a zero, and values larger than 1 will behave like 1. Default to 1. <code>crossoverDistribution</code> The distribution index for SBX. Larger index makes the distribution sharper around each parent.
<code>...</code>	Further arguments to be passed to <code>fun</code>

Value

Returns a list for the next generation. It contains `list$new_generation` (class: `cmaes_gen`), `list$population` (basically a copy of `list$new_generation[[]]$x`), and `list$populationObjective`

References

Voß, T., Hansen, N., Igel, C.: Improved step size adaptation for the MO-CMA-ES. In: Genetic and Evolutionary Computation (GECCO). pp. 487–494. ACM, New York, NY (2010)

Examples

```
nVar <- 14
nObjective <- 5
nIndividual <- 100
crossoverProbability <- 1
ps_target <- 1 / (5 + ( 1 / 2 ) )
pop <- matrix(stats::runif(nIndividual*nVar), nrow = nVar) # create the population
a_list <- cmaes_gen(pop)
control <- list(successProbTarget=ps_target,crossoverProbability=crossoverProbability)
# run a generation of SMO-CMA-ES with standard WFG8 test function.
numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready) # prevent error on testing the example
newGeneration <- SMOcMAES(a_list,nObjective,WFG8,control,nObjective)
```

SMSEMOA

S-Metric Selection EMOA

Description

Do an iteration of S-Metric Selection (SMS)-EMOA. The variation used is simulated binary crossover (SBX) and polynomial mutation.

Usage

```
SMSEMOA(population, fun, nObjective, control = list(), ...)
```

Arguments

population	The parent generation. One individual per column.
fun	Objective function being solved. Currently available in the package DTLZ1-DTLZ4, WFG4-WFG9.
nObjective	Number of objective. Ignored as of version 0.6.1; number of row from fun is used instead.
control	(list) Options to control the SMS-EMOA: <code>mutationProbability</code> The probability of doing mutation. Should be between 0-1. Negative value will behave like a zero, and values larger than 1 will behave like 1. Default to 1 <code>mutationDistribution</code> The distribution index for polynomial mutation. Larger index makes the distribution sharper around the parent. <code>crossoverDistribution</code> The distribution index for SBX. Larger index makes the distribution sharper

around each parent. `referencePoint` The reference point for HV computation on normalized objective space, i.e. $(1, \dots, 1)$ is the nadir point. If not supplied, the `ref_multiplier` is used instead. `ref_multiplier` In case that a reference point is not supplied, the reference is set as a multiply of the current nadir. Default to 1.1. `lbound` A vector containing the lower bound for each gene `ubound` A vector containing the upper bound for each gene `scaleinput` Whether the input should be scaled to 0-1.

... Further arguments to be passed to fun

Value

Returns a list for the next generation population The new generation. Column major, each row contain 1 set of objectives. `successfulOffspring` Binary, 1 if the offspring is kept in the new generation. Used in some adaptive schemes. `populationObjective` The new generation's objective values.

References

Beume, N., Naujoks, B., Emmerich, M.: SMS-EMOA: Multiobjective selection based on dominated hypervolume. *Eur. J. Oper. Res.* 181 (3), 1653 – 1669 (2007)

Examples

```
nVar <- 14
nObjective <- 5
nIndividual <- 100
crossoverProbability <- 1
mutationProbability <- 1/nVar
population <- matrix(runif(nIndividual*nVar), nrow = nVar)

# run a generation of SMS-EMOA with standard WFG6 test function.
numpyready <- reticulate::py_module_available('numpy')
pygmoready <- reticulate::py_module_available('pygmo')
py_module_ready <- numpyready && pygmoready
if(py_module_ready) # prevent error on testing the example
  SMSEMOA(population,WFG6,nObjective,list(crossoverProbability = crossoverProbability,
                                          mutationProbability = mutationProbability),nObjective)
```

WFG1

The WFG1 test function.

Description

The WFG1 test function.

Usage

```
WFG1(individual, nObj, k = nObj - 1)
```

Arguments

<code>individual</code>	The individual to be evaluated, the search space should be in $[0-2i]$ for variable number i . Can accept multiple individualm each in different column.
<code>nObj</code>	The number of objective
<code>k</code>	Number of distance related parameters. The reference suggests a positive integer multiplied by $(nObj-1)$. Default to $nObj-1$

Value

A matrix of size `nObjective`, containing the objective values.

References

Huband, S., Hingston, P., Barone, L., While, L.: A review of multiobjective test problems and a scalable test problem toolkit. *Trans. Evol. Comp* 10 (5), 477–506 (2006)

Examples

```
individual <- runif(14)
nObj <- 4
WFG1(individual,nObj)
```

WFG2

The WFG2 test function.

Description

The WFG2 test function.

Usage

```
WFG2(individual, nObj, k = nObj - 1)
```

Arguments

<code>individual</code>	The individual to be evaluated, the search space should be in $[0-2i]$ for variable number i . Can accept multiple individualm each in different column.
<code>nObj</code>	The number of objective
<code>k</code>	Number of distance related parameters. The reference suggests a positive integer multiplied by $(nObj-1)$. Default to $nObj-1$

Value

A matrix of size `nObjective`, containing the objective values.

References

Huband, S., Hingston, P., Barone, L., While, L.: A review of multiobjective test problems and a scalable test problem toolkit. *Trans. Evol. Comp* 10 (5), 477–506 (2006)

Examples

```
individual <- runif(14)
nObj <- 4
WFG2(individual,nObj)
```

WFG4

The WFG4 test function.

Description

The WFG4 test function.

Usage

```
WFG4(individual, nObj, k = nObj - 1)
```

Arguments

<code>individual</code>	The individual to be evaluated, the search space should be in $[0-2i]$ for variable number i . Can accept multiple individualm each in different column.
<code>nObj</code>	The number of objective
<code>k</code>	Number of distance related parameters. The reference suggests a positive integer multiplied by $(nObj-1)$. Default to $nObj-1$

Value

A matrix of size `nObjective`, containing the objective values.

References

Huband, S., Hingston, P., Barone, L., While, L.: A review of multiobjective test problems and a scalable test problem toolkit. *Trans. Evol. Comp* 10 (5), 477–506 (2006)

Examples

```
individual <- runif(14)
nObj <- 4
WFG4(individual,nObj)
```

WFG5 *The WFG5 test function.*

Description

The WFG5 test function.

Usage

```
WFG5(individual, nObj, k = nObj - 1)
```

Arguments

individual	The individual to be evaluated, the search space should be in $[0-2i]$ for variable number i . Can accept multiple individualm each in different column.
nObj	The number of objective
k	Number of distance related parameters. The reference suggests a positive integer multiplied by $(nObj-1)$. Default to $nObj-1$

Value

A matrix of size $nObjective$, containing the objective values.

References

Huband, S., Hingston, P., Barone, L., While, L.: A review of multiobjective test problems and a scalable test problem toolkit. *Trans. Evol. Comp* 10 (5), 477–506 (2006)

Examples

```
individual <- runif(14)
nObj <- 4
WFG5(individual,nObj)
```

WFG6 *The WFG6 test function.*

Description

The WFG6 test function.

Usage

```
WFG6(individual, nObj, k = nObj - 1)
```

Arguments

individual	The individual to be evaluated, the search space should be in $[0-2i]$ for variable number i . Can accept multiple individualm each in different column.
nObj	The number of objective
k	Number of distance related parameters. The reference suggests a positive integer multiplied by $(nObj-1)$. Default to $nObj-1$

Value

A matrix of size nObjective, containing the objective values.

References

Huband, S., Hingston, P., Barone, L., While, L.: A review of multiobjective test problems and a scalable test problem toolkit. *Trans. Evol. Comp* 10 (5), 477–506 (2006)

Examples

```
individual <- runif(14)
nObj <- 4
WFG6(individual,nObj)
```

WFG7

The WFG7 test function.

Description

The WFG7 test function.

Usage

```
WFG7(individual, nObj, k = nObj - 1)
```

Arguments

individual	The individual to be evaluated, the search space should be in $[0-2i]$ for variable number i . Can accept multiple individualm each in different column.
nObj	The number of objective
k	Number of distance related parameters. The reference suggests a positive integer multiplied by $(nObj-1)$. Default to $nObj-1$

Value

A matrix of size nObjective, containing the objective values.

References

Huband, S., Hingston, P., Barone, L., While, L.: A review of multiobjective test problems and a scalable test problem toolkit. *Trans. Evol. Comp* 10 (5), 477–506 (2006)

Examples

```
individual <- runif(14)
nObj <- 4
WFG7(individual, nObj)
```

WFG8

The WFG8 test function.

Description

The WFG8 test function.

Usage

```
WFG8(individual, nObj, k = nObj - 1)
```

Arguments

individual	The individual to be evaluated, the search space should be in $[0-2i]$ for variable number i . Can accept multiple individualm each in different column.
nObj	The number of objective
k	Number of distance related parameters. The reference suggests a positive integer multiplied by $(nObj-1)$. Default to $nObj-1$

Value

A matrix of size nObjective, containing the objective values.

References

Huband, S., Hingston, P., Barone, L., While, L.: A review of multiobjective test problems and a scalable test problem toolkit. *Trans. Evol. Comp* 10 (5), 477–506 (2006)

Examples

```
individual <- runif(14)
nObj <- 4
WFG8(individual, nObj)
```

WFG9

The WFG9 test function.

Description

The WFG9 test function.

Usage

```
WFG9(individual, nObj, k = nObj - 1)
```

Arguments

<code>individual</code>	The individual to be evaluated, the search space should be in $[0-2i]$ for variable number i . Can accept multiple individualm each in different column.
<code>nObj</code>	The number of objective
<code>k</code>	Number of distance related parameters. The reference suggests a positive integer multiplied by $(nObj-1)$. Default to $nObj-1$

Value

A matrix of size `nObjective`, containing the objective values.

References

Huband, S., Hingston, P., Barone, L., While, L.: A review of multiobjective test problems and a scalable test problem toolkit. *Trans. Evol. Comp* 10 (5), 477–506 (2006)

Examples

```
individual <- runif(14)
nObj <- 4
WFG9(individual,nObj)
```

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