

# Package ‘PBD’

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**Type** Package

**Title** Protracted Birth-Death Model of Diversification

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**Imports** deSolve, ade4, ape, DDD, phytools, graphics, stats, utils

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**Description** Conducts maximum likelihood analysis and simulation of the protracted birth-death model of diversification. See Etienne, R.S. & J. Rosindell 2012 <[doi:10.1093/sysbio/syr091](https://doi.org/10.1093/sysbio/syr091)>; Lambert, A., H. Morlon & R.S. Etienne 2014, <[doi:10.1007/s00285-014-0767-x](https://doi.org/10.1007/s00285-014-0767-x)>; Etienne, R.S., H. Morlon & A. Lambert 2014, <[doi:10.1111/evo.12433](https://doi.org/10.1111/evo.12433)>.

**License** GPL-2

**Suggests** knitr, rmarkdown

**VignetteBuilder** knitr

**RoxygenNote** 5.0.1

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PBD-package

*Protracted Birth-Death Model of Diversification*


---

## Description

This package computes the (maximum) likelihood of the protracted speciation model for a given set of branching times. This package is a likelihood-based statistical package to estimate parameters under the protracted speciation model.

First version: 0.8

New in version 0.9

- Bug fix for stem age

New in version 0.91

- Reports loglik = -Inf on an error in the deSolve package (function ode)

New in version 0.92

- Correcting order of parameters of pbm\_sim

New in version 0.93

- pbm\_sim produces a tree, a matrix containing all events in the simulation, and a tree with one sample per species.

New in version 1.0

- Conditioning is also possible on a range of values of the number of species.

New in version 1.1

- Simulation of the protracted speciation tree has more features.

New in version 1.2

- Optimization can make use of subplex (default) and simplex (older versions).

New in version 1.3

- Contains a function to carry out a bootstrap likelihood ratio test.

- Vignette and test added.

- Reports an error if exteq = TRUE and initparsopt contains 4 parameters.

- Option to limit a simulation to a certain maximum number of species; if exceeded, the simulation is ignored.

New in version 1.4:

- Includes all special cases in pbm\_durspec\_mean

- Fixes a bug in conditioning on a range of values of the number of species

**Details**

Package: PBD  
Type: Package  
Version: 1.4  
Date: 2017-5-4  
License: GPL-2

pbd\_loglik computes the likelihood of the protracted birth-death model of diversification, given a set of parameters and a data set of phylogenetic branching times.

pbd\_ML finds the parameters that maximizes the likelihood computed by pbd\_loglik.

pbd\_bootstrap performs a maximum likelihood analysis and simulates with the maximum likelihood parameters. The ML parameters of the simulated data sets are then estimated, providing an uncertainty distribution for the original ML estimate on the original data.

**Author(s)**

Rampal S. Etienne Maintainer: Rampal S. Etienne <r.s.etienne@rug.nl>

**References**

- Etienne, R.S. & J. Rosindell 2012. Systematic Biology 61: 204-213.
- Lambert, A., H. Morlon & R.S. Etienne 2014. Journal of Mathematical Biology 70: 367-397. doi:10.1007/s00285-014-0767-x
- Etienne, R.S., H. Morlon & A. Lambert 2014. Evolution 68: 2430-2440, doi:10.1111/evo.12433
- . - Etienne, R.S., A.L. Pigot & A.B. Phillimore 2016. Methods in Ecology & Evolution 7: 1092-1099, doi: 10.1111/2041-210X.12565

**See Also**

DDD

---

pbd\_bootstrap

*Bootstrap analysis under protracted birth-death model of diversification*

---

**Description**

Likelihood maximization for protracted birth-death model of diversification followed by simulations of the model using the maximum likelihood parameter estimates to compute an estimate of the error in these estimates and to assess the goodness-of-fit of the model by comparing maximum likelihoods of the simulated data sets to the maximum likelihood of the real data set.

**Usage**

```

pbd_bootstrap(
  brts,
  initparsopt = c(0.2,0.1,1),
  idparsopt = 1:length(initparsopt),
  idparsfix = NULL,
  parsfix = NULL,
  exteq = (length(initparsopt) < 4),
  parsfunc = c(function(t,pars) {pars[1]},function(t,pars) {pars[2]},
function(t,pars) {pars[3]}, function(t,pars) {pars[4]}),
  misssnumspec = 0,
  cond = 1,
  btorph = 0,
  soc = 2,
  plotlitt = 1,
  methode = "lsoda",
  n_low = 0,
  n_up = 0,
  tol = c(1E-4, 1E-4, 1E-6),
  maxiter = 1000 * round((1.25)^length(idparsopt)),
  endmc = 100,
  seed = 42
)

```

**Arguments**

<code>brts</code>	A set of branching times of a phylogeny, all positive
<code>initparsopt</code>	The initial values of the parameters that must be optimized
<code>idparsopt</code>	The ids of the parameters that must be optimized, e.g. 1:4 for all parameters. The ids are defined as follows: id == 1 corresponds to b (speciation-initiation rate) id == 2 corresponds to mu_1 (extinction rate of good species) id == 3 corresponds to la_1 (speciation-completion rate) id == 4 corresponds to mu_2 (extinction rate of incipient species)
<code>idparsfix</code>	The ids of the parameters that should not be optimized, e.g. c(2,4) if mu_1 and mu_2 should not be optimized, but only b and la_1. In that case idparsopt must be c(1,3).
<code>parsfix</code>	The values of the parameters that should not be optimized
<code>exteq</code>	Sets whether incipient species have the same (1) or different (0) extinction rate as good species. If exteq = 0, then idparsfix and idparsopt should together have all parameters 1:4
<code>parsfunc</code>	Specifies functions how the rates depend on time, default functions are constant functions
<code>misssnumspec</code>	The number of species that are in the clade but missing in the phylogeny

cond	Conditioning: cond == 0 : conditioning on stem or crown age cond == 1 : conditioning on stem or crown age and non-extinction of the phylogeny
btorph	Sets whether the likelihood is for the branching times (0) or the phylogeny (1)
soc	Sets whether the first element of the branching times is the stem (1) or the crown (2) age
plotlft	Sets whether the lineage-through-time plot should be plotted (1) or not (0)
methode	Sets which method should be used in the ode-solver. Default is 'lsoda'. See package deSolve for details.
n_low	Sets the lower bound of the number of species on which conditioning should be done when cond = 2. Set this to 0 when conditioning should be done on precisely the number of species (default)
n_up	Sets the upper bound of the number of species on which conditioning should be done when cond = 2. Set this to 0 when conditioning should be done on precisely the number of species (default)
tol	Sets the tolerances in the optimization. Consists of: reltolx = relative tolerance of parameter values in optimization reltolf = relative tolerance of function value in optimization abstolx = absolute tolerance of parameter values in optimization
maxiter	Sets the maximum number of iterations in the optimization
endmc	Sets the number of simulations for the bootstrap
seed	Sets the seed for the simulations of the bootstrap

### Value

A list of three dataframes. The first dataframe contains the maximum likelihood results of the real data set, the second contains the simulated trees, and the third dataframe, with number of rows equal to endmc, contain the maximum likelihood results for the simulated data. The columns of both frames contains the following elements for each simulated data set:

ntips	gives the number of tips
b	gives the maximum likelihood estimate of b
mu_1	gives the maximum likelihood estimate of mu_1
la_1	gives the maximum likelihood estimate of la_1
mu_2	gives the maximum likelihood estimate of mu_2
loglik	gives the maximum loglikelihood
df	gives the number of estimated parameters, i.e. degrees of freedom
conv	gives a message on convergence of optimization; conv = 0 means convergence
exp_durspec	gives the expected duration of speciation
median_durspec	gives the median duration of speciation

**Author(s)**

Rampal S. Etienne

**See Also**[pbd\\_ML](#)


---

pbd\_brts\_density      *Node depth probability density for protracted birth-death model of diversification*

---

**Description**

pbd\_brts\_density computes the probability density of node depths under the protracted speciation model given a set of parameters

**Usage**

```
pbd_brts_density(
  pars1,
  pars1f = c(function(t,pars) {pars[1]},function(t,pars) {pars[2]},
  function(t,pars) {pars[3]}, function(t,pars) {pars[4]}),
  methode = "lsoda",
  brts
)
```

**Arguments**

**pars1**      Vector of parameters:

pars1[1] corresponds to  $b$  (=  $la_1$  in Etienne & Rosindell R2012) = speciation initiation rate  
 pars1[2] corresponds to  $\mu_1$  (=  $\mu_g$  in Etienne & Rosindell 2012) = extinction rate of good species  
 pars1[3] corresponds to  $la_1$  (=  $la_2$  in Etienne & Rosindell 2012) = speciation completion rate  
 pars1[4] corresponds to  $\mu_2$  (=  $\mu_i$  in ER2012) = extinction rate of incipient species  
 When rates depend on time this time dependence should be specified in pars1f and pars1 then becomes the parameters used in pars1f

**pars1f**      Vector of functions how the rates depend on time, default functions are constant functions of the parameters in pars1:

pars1f[1] corresponds to time-dependence of  $b$  (=  $la_1$  in Etienne & Rosindell R2012) = speciation initiation rate

`pars1f[2]` corresponds to time-dependence of  $\mu_1$  (=  $\mu_g$  in Etienne & Rosindell 2012) = extinction rate of good species  
`pars1f[3]` corresponds to time-dependence of  $\lambda_1$  (=  $\lambda_2$  in Etienne & Rosindell 2012) = speciation completion rate  
`pars1f[4]` corresponds to time-dependence of  $\mu_2$  (=  $\mu_i$  in ER2012) = extinction rate of incipient species

**methode** sets which method should be used in the ode-solver. Default is 'lsoda'. See package `deSolve` for details.

**brts** A set of branching times of a phylogeny, all positive, for which the density must be computed

**Value**

The probability density for all branching times

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_ML](#)

**Examples**

```
pbd_brts_density(pars1 = c(0.2,0.1,1,0.1), methode = "lsoda",brts = 1:10)
```

---

`pbd_durspec_cumdensity`

*Cumulative density of duration of speciation under protracted birth-death model of diversification*

---

**Description**

`pbd_durspec_cumdensity` computes the cumulative density of the duration of speciation under the protracted speciation model for a given set of parameters

**Usage**

```
pbd_durspec_cumdensity(
  pars,
  tau
)
```

**Arguments**

pars	Vector of parameters:  pars[1] corresponds to b (= la_3 in Etienne & Rosindell R2012) = speciation initiation rate pars[2] corresponds to la_1 (= la_2 in Etienne & Rosindell 2012) = speciation completion rate pars[3] corresponds to mu_2 (= mu_i in ER2012) = extinction rate of incipient species
tau	Value of the duration of speciation at which the cumulative density must be computed

**Value**

The cumulative density of the duration of speciation

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_durspec\\_density](#)  
[pbd\\_durspec\\_mean](#)  
[pbd\\_durspec\\_mode](#)  
[pbd\\_durspec\\_quantile](#)  
[pbd\\_durspec\\_moment](#)  
[pbd\\_durspec\\_var](#)

**Examples**

```
pbd_durspec_cumdensity(pars = c(0.5,0.3,0.1),3)
```

---

pbd\_durspec\_density     *Probability density for duration of speciation under protracted birth-death model of diversification*

---

**Description**

pbd\_durspec\_density computes the probability density of the duration of speciation under the protracted speciation model for a given set of parameters

**Usage**

```
pbd_durspec_density(  
  pars,  
  tau  
)
```

**Arguments**

`pars`            Vector of parameters:  
  
                  `pars[1]` corresponds to `b` (= `la_3` in Etienne & Rosindell R2012) = speciation initiation rate  
                  `pars[2]` corresponds to `la_1` (= `la_2` in Etienne & Rosindell 2012) = speciation completion rate  
                  `pars[3]` corresponds to `mu_2` (= `mu_i` in ER2012) = extinction rate of incipient species

`tau`            The duration of speciation for which the density must be computed

**Value**

The probability density

**Author(s)**

Rampal S. Etienne

**See Also**

[pbddurspec\\_cumdensity](#)  
[pbddurspec\\_mean](#)  
[pbddurspec\\_mode](#)  
[pbddurspec\\_quantile](#)  
[pbddurspec\\_moment](#)  
[pbddurspec\\_var](#)

**Examples**

```
pbddurspec_density(pars = c(0.5,0.3,0.1), tau = 1)
```

---

`pbddurspec_mean`            *Mean duration of speciation under protracted birth-death model of diversification*

---

**Description**

`pbddurspec_mean` computes the mean duration of speciation under the protracted speciation model for a given set of parameters

**Usage**

```
pbddurspec_mean(  
  pars  
)
```

**Arguments**

`pars` Vector of parameters:

`pars[1]` corresponds to  $b$  (=  $la_3$  in Etienne & Rosindell R2012) = speciation initiation rate  
`pars[2]` corresponds to  $la_1$  (=  $la_2$  in Etienne & Rosindell 2012) = speciation completion rate  
`pars[3]` corresponds to  $\mu_2$  (=  $\mu_i$  in ER2012) = extinction rate of incipient species

**Value**

The expected duration of speciation

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_durspec\\_density](#)  
[pbd\\_durspec\\_cumdensity](#)  
[pbd\\_durspec\\_mode](#)  
[pbd\\_durspec\\_quantile](#)  
[pbd\\_durspec\\_moment](#)  
[pbd\\_durspec\\_var](#)

**Examples**

```
pbd_durspec_mean(pars = c(0.5, 0.3, 0.1))
```

---

`pbd_durspec_mode`      *mode of the duration of speciation under protracted birth-death model of diversification*

---

**Description**

`pbd_durspec_mode` computes the mode of the duration of speciation under the protracted speciation model for a given set of parameters

**Usage**

```
pbd_durspec_mode(  
  pars  
)
```

**Arguments**

`pars` Vector of parameters:

`pars[1]` corresponds to  $b$  (= `la_3` in Etienne & Rosindell R2012) = speciation initiation rate  
`pars[2]` corresponds to  $la_1$  (= `la_2` in Etienne & Rosindell 2012) = speciation completion rate  
`pars[3]` corresponds to  $\mu_2$  (= `mu_i` in ER2012) = extinction rate of incipient species

**Value**

The expected duration of speciation

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_durspec\\_density](#)  
[pbd\\_durspec\\_cumdensity](#)  
[pbd\\_durspec\\_mean](#)  
[pbd\\_durspec\\_quantile](#)  
[pbd\\_durspec\\_moment](#)  
[pbd\\_durspec\\_var](#)

**Examples**

```
pbd_durspec_moment(pars = c(0.5, 0.3, 0.1))
```

---

`pbd_durspec_moment` *Moments of duration of speciation under protracted birth-death model of diversification*

---

**Description**

`pbd_durspec_moment` computes the moments of the duration of speciation under the protracted speciation model for a given set of parameters

**Usage**

```
pbd_durspec_moment(  
  pars,  
  order  
)
```

**Arguments**

`pars`                    Vector of parameters:

`pars[1]` corresponds to  $b$  (= `la_3` in Etienne & Rosindell R2012) = speciation initiation rate  
`pars[2]` corresponds to  $la_1$  (= `la_2` in Etienne & Rosindell 2012) = speciation completion rate  
`pars[3]` corresponds to  $\mu_2$  (=  $\mu_i$  in ER2012) = extinction rate of incipient species

`order`                    order of the moment to compute (1 is first moment, giving the mean)

**Value**

The moment of the duration of speciation

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_durspec\\_density](#)  
[pbd\\_durspec\\_cumdensity](#)  
[pbd\\_durspec\\_mean](#)  
[pbd\\_durspec\\_mode](#)  
[pbd\\_durspec\\_quantile](#)  
[pbd\\_durspec\\_var](#)

**Examples**

```
pbd_durspec_moment(pars = c(0.5, 0.3, 0.1), 2)
```

---

`pbd_durspec_quantile`    *Quantiles of duration of speciation under protracted birth-death model of diversification*

---

**Description**

`pbd_durspec_quantile` computes a quantile of the duration of speciation under the protracted speciation model for a given set of parameters

**Usage**

```
pbd_durspec_quantile(  
  pars,  
  p  
)
```

**Arguments**

pars	Vector of parameters:  pars[1] corresponds to b (= la_3 in Etienne & Rosindell R2012) = speciation initiation rate pars[2] corresponds to la_1 (= la_2 in Etienne & Rosindell 2012) = speciation completion rate pars[3] corresponds to mu_2 (= mu_i in ER2012) = extinction rate of incipient species
p	Quantile (e.g. p = 0.5 gives the median)

**Value**

The quantil of the duration of speciation

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_durspec\\_density](#)  
[pbd\\_durspec\\_cumdensity](#)  
[pbd\\_durspec\\_mean](#)  
[pbd\\_durspec\\_mode](#)  
[pbd\\_durspec\\_moment](#)  
[pbd\\_durspec\\_var](#)

**Examples**

```
pbd_durspec_quantile(pars = c(0.5,0.3,0.1),0.5)
```

---

pbd_durspec_var	<i>Variance in duration of speciation under protracted birth-death model of diversification</i>
-----------------	---

---

**Description**

pbd\_durspec\_var computes the variance in the duration of speciation under the protracted speciation model for a given set of parameters

**Usage**

```
pbd_durspec_var(  
  pars  
)
```

**Arguments**

`pars` Vector of parameters:

`pars[1]` corresponds to  $b$  (=  $la_3$  in Etienne & Rosindell R2012) = speciation initiation rate  
`pars[2]` corresponds to  $la_1$  (=  $la_2$  in Etienne & Rosindell 2012) = speciation completion rate  
`pars[3]` corresponds to  $\mu_2$  (=  $\mu_i$  in ER2012) = extinction rate of incipient species

**Value**

The variance in the duration of speciation

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_durspec\\_density](#)  
[pbd\\_durspec\\_cumdensity](#)  
[pbd\\_durspec\\_mean](#)  
[pbd\\_durspec\\_mode](#)  
[pbd\\_durspec\\_quantile](#)  
[pbd\\_durspec\\_moment](#)

**Examples**

```
pbd_durspec_var(pars = c(0.5,0.3,0.1))
```

---

pbd\_loglik

*Loglikelihood for protracted birth-death model of diversification*

---

**Description**

`pbd_loglik` computes the loglikelihood of the parameters of the protracted speciation model given a set of branching times and number of missing species

**Usage**

```
pbd_loglik(
  pars1,
  pars1f = c(function(t,pars) {pars[1]},function(t,pars) {pars[2]}),
  function(t,pars) {pars[3]}, function(t,pars) {pars[4]}),
  pars2 = c(1,1,2,1,"lsoda",0,0),
```

```

    brts,
    missnumspec = 0
)

```

### Arguments

- pars1**            Vector of parameters:
- pars1[1] corresponds to  $b$  (=  $la_1$  in Etienne & Rosindell R2012) = speciation initiation rate  
 pars1[2] corresponds to  $\mu_1$  (=  $\mu_g$  in Etienne & Rosindell 2012) = extinction rate of good species  
 pars1[3] corresponds to  $la_1$  (=  $la_2$  in Etienne & Rosindell 2012) = speciation completion rate  
 pars1[4] corresponds to  $\mu_2$  (=  $\mu_i$  in ER2012) = extinction rate of incipient species  
 When rates depend on time this time dependence should be specified in pars1f and pars1 then becomes the parameters used in pars1f
- pars1f**            Vector of functions how the rates depend on time, default functions are constant functions of the parameters in pars1:
- pars1f[1] corresponds to time-dependence of  $b$  (=  $la_1$  in Etienne & Rosindell R2012) = speciation initiation rate  
 pars1f[2] corresponds to time-dependence of  $\mu_1$  (=  $\mu_g$  in Etienne & Rosindell 2012) = extinction rate of good species  
 pars1f[3] corresponds to time-dependence of  $la_1$  (=  $la_2$  in Etienne & Rosindell 2012) = speciation completion rate  
 pars1f[4] corresponds to time-dependence of  $\mu_2$  (=  $\mu_i$  in ER2012) = extinction rate of incipient species
- pars2**            Vector of model settings:
- pars2[1] set the conditioning on non-extinction of the clade (1) or not (0)
- pars2[2] sets whether the likelihood is for the branching times (0) or the phylogeny (1)
- pars2[3] sets whether the first element of the branching times is the stem (1) or the crown (2) age
- pars2[4] sets whether the parameters and likelihood should be shown on screen (1) or not (0)
- pars2[5] sets which method should be used in the ode-solver. Default is 'lsoda'. See package deSolve for details.

pars2[6] Sets the lower bound of the number of species on which conditioning should be done when `cond = 2`. Set this to 0 when conditioning should be done on precisely the number of species (default)

pars2[7] Sets the upper bound of the number of species on which conditioning should be done when `cond = 2`. Set this to 0 when conditioning should be done on precisely the number of species (default)

`brts` A set of branching times of a phylogeny, all positive  
`missnumspec` The number of species that are in the clade but missing in the phylogeny

### Value

The loglikelihood

### Author(s)

Rampal S. Etienne

### See Also

[pbd\\_ML](#)

### Examples

```
pbd_loglik(pars1 = c(0.2,0.1,1,0.1), pars2 = c(1,1,2,0,"lsoda"),brts = 1:10)
```

---

pbd_LR	<i>Bootstrap likelihood ratio test of protracted birth-death model of diversification</i>
--------	---

---

### Description

This function computes the maximum likelihood and the associated estimates of the parameters of a protracted birth-death model of diversification for a given set of phylogenetic branching times. It then performs a bootstrap likelihood ratio test of the protracted birth-death (PBD) model against the constant-rates (CR) birth-death model. Finally, it computes the power of this test.

### Usage

```
pbd_LR(  
  brts,  
  initparsoptPBD,  
  initparsoptCR,  
  missnumspec,
```

```

outputfilename = NULL,
seed = 42,
endmc = 1000,
alpha = 0.05,
plotit = TRUE,
parsfunc = c(function(t,pars) {pars[1]},
function(t,pars) {pars[2]},
function(t,pars) {pars[3]},
function(t,pars) {pars[4]}),
cond = 1,
btorph = 1,
soc = 2,
methode = 'lsoda',
n_low = 0,
n_up = 0,
tol = c(1E-6,1E-6,1E-6),
maxiter = 2000,
optimmethod = 'subplex',
verbose = FALSE
)

```

### Arguments

brts	A set of branching times of a phylogeny, all positive
initparsoptPBD	The initial values of the parameters that must be optimized for the protracted birth-death (PBD) model: b, mu and lambda
initparsoptCR	The initial values of the parameters that must be optimized for the constant-rates (CR) model: b and mu
missnumspec	The number of species that are in the clade but missing in the phylogeny
outputfilename	The name (and location) of the file where the output will be saved. Default is no save.
seed	The seed for the pseudo random number generator for simulating the bootstrap data
endmc	The number of bootstraps
alpha	The significance level of the test
plotit	Boolean to plot results or not
parsfunc	Specifies functions how the rates depend on time, default functions are constant functions
cond	Conditioning: cond == 0 : conditioning on stem or crown age cond == 1 : conditioning on stem or crown age and non-extinction of the phylogeny cond == 2 : conditioning on stem or crown age and on the total number of extant taxa (including missing species) cond == 3 : conditioning on the total number of extant taxa (including missing species)

Note: `cond == 3` assumes a uniform prior on stem age, as is the standard in constant-rate birth-death models, see e.g. D. Aldous & L. Popovic 2004. *Adv. Appl. Prob.* 37: 1094-1115 and T. Stadler 2009. *J. Theor. Biol.* 261: 58-66.

<code>btorph</code>	Sets whether the likelihood is for the branching times (0) or the phylogeny (1)
<code>soc</code>	Sets whether stem or crown age should be used (1 or 2)
<code>methode</code>	The numerical method used to solve the master equation, such as 'lsoda' or 'ode45'.
<code>n_low</code>	Sets the lower bound of the number of species on which conditioning should be done when <code>cond = 2</code> . Set this to 0 when conditioning should be done on precisely the number of species (default)
<code>n_up</code>	Sets the upper bound of the number of species on which conditioning should be done when <code>cond = 2</code> . Set this to 0 when conditioning should be done on precisely the number of species (default)
<code>tol</code>	Sets the tolerances in the optimization. Consists of: <code>reoltox</code> = relative tolerance of parameter values in optimization <code>reoltol</code> = relative tolerance of function value in optimization <code>abstolx</code> = absolute tolerance of parameter values in optimization
<code>maxiter</code>	Sets the maximum number of iterations in the optimization
<code>optimmethod</code>	Method used in optimization of the likelihood. Current default is 'subplex'. Alternative is 'simplex'.
<code>verbose</code>	if TRUE, explanatory text will be shown

### Details

The output is a list with 3 elements:

### Value

<code>brtsCR</code>	a list of sets of branching times generated under the constant-rates model using the ML parameters under the CR model
<code>brtsDD</code>	a list of sets of branching times generated under the protracted birth-death model using the ML parameters under the PBD model
<code>out</code>	a dataframe with the parameter estimates and maximum likelihoods for protracted birth-death and constant-rates models <code>\$model</code> - the model used to generate the data. 0 = unknown (for real data), 1 = CR, 2 = PBD <code>\$mc</code> - the simulation number for each model <code>\$b_CR</code> - speciation rate estimated under CR <code>\$mu_CR</code> - extinction rate estimated under CR <code>\$LL_CR</code> - maximum likelihood estimated under CR <code>\$conv_CR</code> - convergence code for likelihood optimization; <code>conv = 0</code> means convergence <code>\$b_PBD1</code> - speciation-ination rate estimated under PBD for first set of initial values <code>\$mu_PB1</code> - extinction rate estimated under DD for first set of initial values <code>\$lambda_PB1</code> - speciation-completion rate estimated under PBD for first set of initial values

	\$LL_PBD1 - maximum likelihood estimated under DD for first set of initial values
	\$conv_PBD1 - convergence code for likelihood optimization for first set of initial values; conv = 0 means convergence
	\$b_PBD2 - speciation-imitation rate estimated under PBD for second set of initial values
	\$mu_PB2 - extinction rate estimated under DD for second set of initial values
	\$lambda_PB2 - speciation-completion rate estimated under PBD for second set of initial values
	\$LL_PBD2 - maximum likelihood estimated under DD for second set of initial values
	\$conv_PBD2 - convergence code for likelihood optimization for second set of initial values; conv = 0 means convergence
	\$LR - likelihood ratio between DD and CR
pvalue	p-value of the test
LRalpha	Likelihood ratio at the significance level alpha
powerof test	power of the test for significance level alpha

**Author(s)**

Rampal S. Etienne

**References**

- Etienne, R.S. et al. 2016. Meth. Ecol. Evol. 7: 1092-1099, doi: 10.1111/2041-210X.12565

**See Also**

[pb<sub>d</sub>\\_loglik](#), [pb<sub>d</sub>\\_ML](#)

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pb <sub>d</sub> _ML	<i>Maximization of loglikelihood under protracted birth-death model of diversification</i>
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**Description**

Likelihood maximization for protracted birth-death model of diversification

**Usage**

```
pbd_ML(  
  brts,  
  initparsopt = c(0.2,0.1,1),  
  idparsopt = 1:length(initparsopt),  
  idparsfix = NULL,  
  parsfix = NULL,
```

```

    exteq = 1,
    parsfunc = c(function(t,pars) {pars[1]},function(t,pars) {pars[2]},
function(t,pars) {pars[3]}, function(t,pars) {pars[4]}),
    misnumspec = 0,
    cond = 1,
    btorph = 1,
    soc = 2,
    methode = "lsoda",
    n_low = 0,
    n_up = 0,
    tol = c(1E-6, 1E-6, 1E-6),
    maxiter = 1000 * round((1.25)^length(idparsopt)),
    optimmethod = 'subplex',
    verbose = TRUE
)

```

### Arguments

<code>brts</code>	A set of branching times of a phylogeny, all positive
<code>initparsopt</code>	The initial values of the parameters that must be optimized
<code>idparsopt</code>	The ids of the parameters that must be optimized, e.g. 1:4 for all parameters. The ids are defined as follows: id == 1 corresponds to b (speciation-initiation rate) id == 2 corresponds to mu_1 (extinction rate of good species) id == 3 corresponds to la_1 (speciation-completion rate) id == 4 corresponds to mu_2 (extinction rate of incipient species)
<code>idparsfix</code>	The ids of the parameters that should not be optimized, e.g. c(2,4) if mu_1 and mu_2 should not be optimized, but only b and la_1. In that case idparsopt must be c(1,3).
<code>parsfix</code>	The values of the parameters that should not be optimized
<code>exteq</code>	Sets whether incipient species have the same (1) or different (0) extinction rate as good species. If exteq = 0, then idparsfix and idparsopt should together have all parameters 1:4
<code>parsfunc</code>	Specifies functions how the rates depend on time, default functions are constant functions
<code>misnumspec</code>	The number of species that are in the clade but missing in the phylogeny
<code>cond</code>	Conditioning: cond == 0 : conditioning on stem or crown age cond == 1 : conditioning on stem or crown age and non-extinction of the phylogeny cond == 2 : conditioning on stem or crown age and number of extant taxa
<code>btorph</code>	Sets whether the likelihood is for the branching times (0) or the phylogeny (1)
<code>soc</code>	Sets whether the first element of the branching times is the stem (1) or the crown (2) age

methode	Sets which method should be used in the ode-solver. Default is 'lsoda'. See package deSolve for details.
n_low	Sets the lower bound of the number of species on which conditioning should be done when cond = 2. Set this to 0 when conditioning should be done on precisely the number of species (default)
n_up	Sets the upper bound of the number of species on which conditioning should be done when cond = 2. Set this to 0 when conditioning should be done on precisely the number of species (default)
tol	Sets the tolerances in the optimization. Consists of: reltolx = relative tolerance of parameter values in optimization reltolf = relative tolerance of function value in optimization abstolx = absolute tolerance of parameter values in optimization
maxiter	Sets the maximum number of iterations in the optimization
optimmethod	Method used in optimization of the likelihood. Current default is 'subplex'. Alternative is 'simplex' (default of previous versions)
verbose	if TRUE, explanatory text will be shown

**Value**

A data frame with the following components:

b	gives the maximum likelihood estimate of b
mu_1	gives the maximum likelihood estimate of mu_1
la_1	gives the maximum likelihood estimate of la_1
mu_2	gives the maximum likelihood estimate of mu_2
loglik	gives the maximum loglikelihood
df	gives the number of estimated parameters, i.e. degrees of freedom
conv	gives a message on convergence of optimization; conv = 0 means convergence

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_loglik](#)

**Examples**

```
pbd_ML(1:10, initparsopt = c(4.640321, 4.366528, 0.030521), exteq = 1)
```

pbd\_sim

*Function to simulate the protracted speciation process***Description**

Simulating the protracted speciation process using the Doob-Gillespie algorithm. This function differs from pbd\_sim\_cpp that 1) it does not require that the speciation-initiation rate is the same for good and incipient species, and 2) that it simulates the exact protracted speciation process, and not the approximation made by the coalescent point process. This function provides also the conversion to the approximation as output.

**Usage**

```
pbd_sim(
  pars,
  age,
  soc = 2,
  plotit = FALSE,
  limitsize = Inf
)
```

**Arguments**

pars	Vector of parameters:  pars[1] corresponds to b_1, the speciation-initiation rate of good species pars[2] corresponds to la_1, the speciation-completion rate pars[3] corresponds to b_2, the speciation-initiation rate of incipient species pars[4] corresponds to mu_1, the extinction rate of good species pars[5] corresponds to mu_2, the extinction rate of incipient species
age	Sets the age for the simulation
soc	Sets whether this age is the stem (1) or crown (2) age
plotit	Sets whether the various trees produced by the function should be plotted or not
limitsize	Sets a maximum to the number of incipient + good species that are created during the simulation; if exceeded, the simulation is aborted and removed.

**Value**

out	A list with the following elements:  tree is the tree of extant species in phylo format stree_random is a tree with one random sample per species in phylo format stree_oldest is a tree with the oldest sample per species in phylo format stree_youngest is a tree with the youngest sample per species in phylo format L is a matrix of all events in the simulation where
-----	---

- the first column is the incipient-level label of a species
- the second column is the incipient-level label of the parent of the species
- the third column is the time at which a species is born as incipient species
- the fourth column is the time of speciation-completion of the species

If the fourth element equals -1, then the species is still incipient. - the fifth column is the time of extinction of the species

If the fifth element equals -1, then the species is still extant. - The sixth column is the species-level label of the species

sL\_random is a matrix like L but for stree\_random

sL\_oldest is a matrix like L but for stree\_oldest

sL\_youngest is a matrix like L but for stree\_youngest

igtree\_extinct is the tree in simmap format with incipient and good flags and including extinct species

igtree\_extant is the tree in simmap format with incipient and good flags without extinct species

recontree is the reconstructed tree in phylo format, reconstructed using the approximation in Lambert et al. 2014

reconL is the matrix corresponding to recontree

L0 is a matrix where the crown age is at 0; for internal use only

**Author(s)**

Rampal S. Etienne

**See Also**

[pbd\\_sim\\_cpp](#)

**Examples**

```
pbd_sim(c(0.2,1,0.2,0.1,0.1),15)
```

---

pbd\_sim\_cpp

*Function to simulate the approximate protracted speciation process*

---

**Description**

Simulating the protracted speciation process according to the approximate model of Lambert et al. 2014. This function differs from pbd\_sim that 1) it requires that the speciation-initiation rate is the same for good and incipient species, and 2) that it does not simulate the exact protracted speciation process, but an approximation made by the coalescent point process.

**Usage**

```

pbd_sim_cpp(
  pars,
  parsf = c(function(t,pars) {pars[1]},function(t,pars) {pars[2]},
function(t,pars) {pars[3]},function(t,pars) {pars[4]}),
  age,
  soc = 2,
  plotlft = 1,
  methode = "lsoda"
)

```

**Arguments**

pars	<p>Vector of parameters:</p> <p>pars[1] corresponds to <math>b</math> (= <math>la_1</math> in Etienne &amp; Rosindell R2012) = speciation initiation rate</p> <p>pars[2] corresponds to <math>\mu_1</math> (= <math>\mu_g</math> in Etienne &amp; Rosindell 2012) = extinction rate of good species</p> <p>pars[3] corresponds to <math>la_1</math> (= <math>la_2</math> in Etienne &amp; Rosindell 2012) = speciation completion rate</p> <p>pars[4] corresponds to <math>\mu_2</math> (= <math>\mu_i</math> in ER2012) = extinction rate of incipient species</p> <p>When rates depend on time this time dependence should be specified in pars1f and pars1 then becomes the parameters used in pars1f</p>
parsf	<p>Vector of functions how the rates depend on time, default functions are constant functions of the parameters in pars1:</p> <p>parsf[1] corresponds to time-dependence of <math>b</math> (= <math>la_1</math> in Etienne &amp; Rosindell R2012) = speciation initiation rate</p> <p>parsf[2] corresponds to time-dependence of <math>\mu_1</math> (= <math>\mu_g</math> in Etienne &amp; Rosindell 2012) = extinction rate of good species</p> <p>parsf[3] corresponds to time-dependence of <math>la_1</math> (= <math>la_2</math> in Etienne &amp; Rosindell 2012) = speciation completion rate</p> <p>parsf[4] corresponds to time-dependence of <math>\mu_2</math> (= <math>\mu_i</math> in ER2012) = extinction rate of incipient species</p>
age	Sets the crown age for the simulation
soc	Determines whether the simulation should start at stem (1) or crown (2) age
plotlft	Sets whether the lineage-through-time plot should be plotted (1) or not (0)
methode	Sets which method should be used in the ode-solver. Default is 'lsoda'. See package deSolve for details.

**Value**

A set of branching times

**Author(s)**

Rampal S. Etienne

**See Also**

[pbdsim](#)

**Examples**

```
pbdsim_cpp(pars = c(0.2,1,0.2,0.1),age = 15)
```

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