

Package ‘adamethods’

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Author Guillermo Vinue, Irene Epifanio

Maintainer Guillermo Vinue <Guillermo.Vinue@uv.es>

Description Collection of several algorithms to obtain archetypoids with small and large databases, and with both classical multivariate data and functional data (univariate and multivariate). Some of these algorithms also allow to detect anomalies (outliers). Please see Vinue and Epifanio (2020) <[doi:10.1007/s11634-020-00412-9](https://doi.org/10.1007/s11634-020-00412-9)>.

License GPL (>= 2)

URL <https://www.r-project.org>

Depends R (>= 3.4.0)

Imports Anthropometry, archetypes, FNN, foreach, graphics, nnls, parallel, stats, tolerance, univOutl, utils

Suggests doParallel, fda

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Description

The ADALARA algorithm is based on the CLARA clustering algorithm. This is the parallel version of the algorithm to try to get faster results. It allows to detect anomalies (outliers). There are two different methods to detect them: the adjusted boxplot (default and most reliable option) and tolerance intervals. If needed, tolerance intervals allow to define a degree of outlieriness.

Usage

```
adalara(data, N, m, numArchoid, numRep, huge, prob, type_alg = "ada",
        compare = FALSE, vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
        outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
        method = "adjbox", frame)
```

Arguments

data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric. The data must have row names so that the algorithm can identify the archetypoids in every sample.
N	Number of samples.
m	Sample size of each sample.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArchoid, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
type_alg	String. Options are 'ada' for the non-robust adalara algorithm and 'ada_rob' for the robust adalara algorithm.
compare	Boolean argument to compute the robust residual sum of squares if type_alg = "ada" and the non-robust if type_alg = "ada_rob".
vect_tol	Vector with the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlieriness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.
frame	Boolean value to indicate whether the frame is computed (Mair et al., 2017) or not. The frame is made up of a subset of extreme points, so the archetypoids are only computed on the frame. Low frame densities are obtained when only small portions of the data were extreme. However, high frame densities reduce this speed-up.

Value

A list with the following elements:

- cases Optimal vector of archetypoids.
- rss Optimal residual sum of squares.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

- Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>
- Hubert, M. and Vandervieren, E., An adjusted boxplot for skewed distributions, 2008. *Computational Statistics and Data Analysis* **52(12)**, 5186-5201, <https://doi.org/10.1016/j.csda.2007.11.008>
- Kaufman, L. and Rousseeuw, P.J., Clustering Large Data Sets, 1986. *Pattern Recognition in Practice*, 425-437.
- Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.
- Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>
- Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, <https://doi.org/10.18637/jss.v077.i06>

See Also

[do_ada](#), [do_ada_robust](#), [adalara_no_parallel](#)

Examples

```
## Not run:
library(Anthropometry)
library(doParallel)

# Prepare parallelization (including the seed for reproducibility):
no_cores <- detectCores() - 1
cl <- makeCluster(no_cores)
registerDoParallel(cl)
clusterSetRNGStream(cl, iseed = 1)

# Load data:
data(mtcars)
data <- mtcars
n <- nrow(data)

# Arguments for the archetype/archetypoid algorithm:
# Number of archetypoids:
k <- 3
numRep <- 2
huge <- 200

# Size of the random sample of observations:
m <- 10
```

```

# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N

prob <- 0.75

# ADALARA algorithm:
preproc <- preprocessing(data, stand = TRUE, percAccomm = 1)
data1 <- as.data.frame(preproc$data)

adalara_aux <- adalara(data1, N, m, k, numRep, huge, prob,
                      "ada_rob", FALSE, method = "adjbox", frame = FALSE)

#adalara_aux <- adalara(data1, N, m, k, numRep, huge, prob,
#                      "ada_rob", FALSE, vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
#                      outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
#                      method = "toler", frame = FALSE)

# Take the minimum RSS, which is in the second position of every sublist:
adalara <- adalara_aux[which.min(unlist(sapply(adalara_aux, function(x) x[2])))] [[1]]
adalara

# End parallelization:
stopCluster(cl)

## End(Not run)

```

adalara_no_parallel	<i>Multivariate non-parallel archetypoid algorithm for large applications (ADALARA)</i>
---------------------	---

Description

The ADALARA algorithm is based on the CLARA clustering algorithm. This is the non-parallel version of the algorithm. It allows to detect anomalies (outliers). There are two different methods to detect them: the adjusted boxplot (default and most reliable option) and tolerance intervals. If needed, tolerance intervals allow to define a degree of outlieriness.

Usage

```

adalara_no_parallel(data, seed, N, m, numArchoid, numRep, huge, prob, type_alg = "ada",
                    compare = FALSE, verbose = TRUE, vect_tol = c(0.95, 0.9, 0.85),
                    alpha = 0.05, outl_degree = c("outl_strong", "outl_semi_strong",
                    "outl_moderate"), method = "adjbox", frame)

```

Arguments

data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric. The data must have row names so that the algorithm can identify the archetypoids in every sample.
seed	Integer value to set the seed. This ensures reproducibility.
N	Number of samples.
m	Sample size of each sample.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArchoid, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
type_alg	String. Options are 'ada' for the non-robust adalaro algorithm and 'ada_rob' for the robust adalaro algorithm.
compare	Boolean argument to compute the robust residual sum of squares if type_alg = "ada" and the non-robust if type_alg = "ada_rob".
verbose	Display progress? Default TRUE.
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.
frame	Boolean value to indicate whether the frame is computed (Mair et al., 2017) or not. The frame is made up of a subset of extreme points, so the archetypoids are only computed on the frame. Low frame densities are obtained when only small portions of the data were extreme. However, high frame densities reduce this speed-up.

Value

A list with the following elements:

- cases Optimal vector of archetypoids.
- rss Optimal residual sum of squares.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

- Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>
- Hubert, M. and Vandervieren, E., An adjusted boxplot for skewed distributions, 2008. *Computational Statistics and Data Analysis* **52(12)**, 5186-5201, <https://doi.org/10.1016/j.csda.2007.11.008>
- Kaufman, L. and Rousseeuw, P.J., Clustering Large Data Sets, 1986. *Pattern Recognition in Practice*, 425-437.
- Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.
- Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>
- Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, <https://doi.org/10.18637/jss.v077.i06>

See Also

[do_ada](#), [do_ada_robust](#), [adalara](#)

Examples

```
## Not run:
library(Anthropometry)

# Load data:
data(mtcars)
data <- mtcars
n <- nrow(data)

# Arguments for the archetype/archetypoid algorithm:
# Number of archetypoids:
k <- 3
numRep <- 2
huge <- 200

# Size of the random sample of observations:
m <- 10
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N

prob <- 0.75

# ADALARA algorithm:
preproc <- preprocessing(data, stand = TRUE, percAccomm = 1)
data1 <- as.data.frame(preproc$data)
res_adalara <- adalara_no_parallel(data1, 1, N, m, k,
                                  numRep, huge, prob, "ada_rob", FALSE, TRUE,
```

```

method = "adjbox", frame = FALSE)

# Examine the results:
res_adalara

res_adalara1 <- adalara_no_paral(data1, 1, N, m, k,
                                numRep, huge, prob, "ada_rob", FALSE, TRUE,
                                vect_tol = c(0.95, 0.9, 0.85),
                                alpha = 0.05, outl_degree = c("outl_strong", "outl_semi_strong",
                                                             "outl_moderate"),
                                method = "toler", frame = FALSE)

res_adalara1

## End(Not run)

```

archetypoids_func *Archetypoid algorithm with the functional Frobenius norm*

Description

Archetypoid algorithm with the functional Frobenius norm to be used with functional data.

Usage

```
archetypoids_func(numArchoid, data, huge = 200, ArchObj, PM)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the stepArchetypesRawData_func function.
PM	Penalty matrix obtained with eval.penalty .

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>

See Also[archetypoids](#)**Examples**

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)
# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

lass <- stepArchetypesRawData_funcnt(data = data_archs, numArch = 3,
                                     numRep = 5, verbose = FALSE,
                                     saveHistory = FALSE, PM)

af <- archetypoids_funcnt(3, data_archs, huge = 200, ArchObj = lass, PM)
str(af)

## End(Not run)
```

 archetypoids_func_multiv

Archetypoid algorithm with the functional multivariate Frobenius norm

Description

Archetypoid algorithm with the functional multivariate Frobenius norm to be used with functional data.

Usage

```
archetypoids_funcnt_multiv(numArchoid, data, huge = 200, ArchObj, PM)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the <code>stepArchetypesRawData_func</code> function.
PM	Penalty matrix obtained with <code>eval.penalty</code> .

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>

See Also

[archetypoids](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, ,1] <- as.matrix(hgtm)
data.array[, ,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)
```

```

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, , 1])), nvars))
X[, , 1] <- t(temp_fd$coef[, , 1])
X[, , 2] <- t(temp_fd$coef[, , 2])

# Standardize the variables:
Xs <- X
Xs[, , 1] <- scale(X[, , 1])
Xs[, , 2] <- scale(X[, , 2])

lass <- stepArchetypesRawData_func_multiv(data = Xs, numArch = 3,
                                         numRep = 5, verbose = FALSE,
                                         saveHistory = FALSE, PM)

afm <- archetypoids_func_multiv(3, Xs, huge = 200, ArchObj = lass, PM)
str(afm)

## End(Not run)

```

archetypoids_func_multiv_robust

Archetypoid algorithm with the functional multivariate robust Frobenius norm

Description

Archetypoid algorithm with the functional multivariate robust Frobenius norm to be used with functional data.

Usage

```
archetypoids_func_multiv_robust(numArchoid, data, huge = 200, ArchObj, PM, prob)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the stepArchetypesRawData_func function.

PM	Penalty matrix obtained with eval.penalty .
prob	Probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[archetypoids](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, ,1] <- as.matrix(hgtm)
data.array[, ,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
```

```

temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, , 1])), nvars))
X[, , 1] <- t(temp_fd$coef[, , 1])
X[, , 2] <- t(temp_fd$coef[, , 2])

# Standardize the variables:
Xs <- X
Xs[, , 1] <- scale(X[, , 1])
Xs[, , 2] <- scale(X[, , 2])

lass <- stepArchetypesRawData_func_multiv_robust(data = Xs, numArch = 3,
                                                numRep = 5, verbose = FALSE,
                                                saveHistory = FALSE, PM, prob = 0.8,
                                                nbasis, nvars)

afmr <- archetypoids_func_multiv_robust(3, Xs, huge = 200, ArchObj = lass, PM, 0.8)
str(afmr)

## End(Not run)

```

archetypoids_func_robust

Archetypoid algorithm with the functional robust Frobenius norm

Description

Archetypoid algorithm with the functional robust Frobenius norm to be used with functional data.

Usage

```
archetypoids_func_robust(numArchoid, data, huge = 200, ArchObj, PM, prob)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the stepArchetypesRawData_func_robust function.
PM	Penalty matrix obtained with eval.penalty .
prob	Probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[archetypoids](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)
# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

lass <- stepArchetypesRawData_funct_robust(data = data_archs, numArch = 3,
                                          numRep = 5, verbose = FALSE,
                                          saveHistory = FALSE, PM, prob = 0.8)

afr <- archetypoids_funct_robust(3, data_archs, huge = 200, ArchObj = lass, PM, 0.8)
str(afr)

## End(Not run)
```

archetypoids_norm_frob

Archetypoid algorithm with the Frobenius norm

Description

This function is the same as [archetypoids](#) but the 2-norm is replaced by the Frobenius norm. Thus, the comparison with the robust archetypoids can be directly made.

Usage

```
archetypoids_norm_frob(numArchoid, data, huge = 200, ArchObj)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the stepArchetypesRawData_norm_frob function.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

- Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>
- Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>
- Vinue, G., Epifanio, I., and Alemany, S., Archetypoids: a new approach to define representative archetypal data, 2015. *Computational Statistics and Data Analysis* **87**, 102-115, <https://doi.org/10.1016/j.csda.2015.01.018>
- Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, <https://doi.org/10.18637/jss.v077.i06>

See Also

[archetypoids](#)

Examples

```
data(mtcars)
data <- mtcars

k <- 3
numRep <- 2
huge <- 200

lass <- stepArchetypesRawData_norm_frob(data = data, numArch = k,
                                       numRep = numRep, verbose = FALSE)

res <- archetypoids_norm_frob(k, data, huge, ArchObj = lass)
str(res)
res$cases
res$rss
```

archetypoids_robust *Archetypoid algorithm with the robust Frobenius norm*

Description

Robust version of the archetypoid algorithm with the Frobenius form.

Usage

```
archetypoids_robust(numArchoid, data, huge = 200, ArchObj, prob)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the stepArchetypesRawData_robust function.
prob	Probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.

- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[archetypoids_norm_frob](#)

Examples

```
data(mtcars)
data <- mtcars

k <- 3
numRep <- 2
huge <- 200

lass <- stepArchetypesRawData_robust(data = data, numArch = k,
                                   numRep = numRep, verbose = FALSE,
                                   saveHistory = FALSE, prob = 0.8)

res <- archetypoids_robust(k, data, huge, ArchObj = lass, 0.8)
str(res)
res$cases
res$rss
```

bisquare_function *Bisquare function*

Description

This function belongs to the bisquare family of loss functions. The bisquare family can better cope with extreme outliers.

Usage

```
bisquare_function(resid, prob, ...)
```

Arguments

resid	Vector of residuals, computed from the $m \times n$ residuals data matrix.
prob	Probability with values in $[0,1]$.
...	Additional possible arguments.

Value

Vector of real numbers.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
resid <- c(2.47, 11.85)
bisquare_function(resid, 0.8)
```

do_ada

Run the whole classical archetypoid analysis with the Frobenius norm

Description

This function executes the entire procedure involved in the archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_ada(subset, numArchoid, numRep, huge, compare = FALSE,
       vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
       outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
       method = "adjbox", prob)
```

Arguments

subset	Data to obtain archetypes. In ADALARA this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
compare	Boolean argument to compute the robust residual sum of squares to compare these results with the ones provided by do_ada_robust .
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.
prob	If compare=TRUE, probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_rob: If compare=TRUE, this is the residual sum of squares using the robust Frobenius norm. Otherwise, NULL.
- resid: Vector with the residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>

Vinue, G., Epifanio, I., and Alemany, S., Archetypoids: a new approach to define representative archetypal data, 2015. *Computational Statistics and Data Analysis* **87**, 102-115, <https://doi.org/10.1016/j.csda.2015.01.018>

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, <https://doi.org/10.18637/jss.v077.i06>

See Also

[stepArchetypesRawData_norm_frob](#), [archetypoids_norm_frob](#)

Examples

```

library(Anthropometry)
data(mtcars)
#data <- as.matrix(mtcars)
data <- mtcars

k <- 3
numRep <- 2
huge <- 200

preproc <- preprocessing(data, stand = TRUE, percAccomm = 1)
suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_ada <- do_ada(preproc$data, k, numRep, huge, FALSE, method = "adjbox")
str(res_ada)

res_ada1 <- do_ada(preproc$data, k, numRep, huge, FALSE,
  vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
  outl_degree = c("outl_strong", "outl_semi_strong",
    "outl_moderate"), method = "toler")
str(res_ada1)

res_ada2 <- do_ada(preproc$data, k, numRep, huge, TRUE, method = "adjbox", prob = 0.8)
str(res_ada2)

```

do_ada_robust	<i>Run the whole robust archetypoid analysis with the robust Frobenius norm</i>
---------------	---

Description

This function executes the entire procedure involved in the robust archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the robust archetypal algorithm and finally, the optimal vector of robust archetypoids is returned.

Usage

```

do_ada_robust(subset, numArchoid, numRep, huge, prob, compare = FALSE,
  vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
  outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
  method = "adjbox")

```

Arguments

subset	Data to obtain archetypes. In ADALARA this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.

numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
compare	Boolean argument to compute the non-robust residual sum of squares to compare these results with the ones provided by <code>do_ada</code> .
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_non_rob: If compare=TRUE, this is the residual sum of squares using the non-robust Frobenius norm. Otherwise, NULL.
- resid Vector of residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[stepArchetypesRawData_robust](#), [archetypoids_robust](#)

Examples

```
## Not run:
library(Anthropometry)
data(mtcars)
#data <- as.matrix(mtcars)
data <- mtcars

k <- 3
```

```

numRep <- 2
huge <- 200

preproc <- preprocessing(data, stand = TRUE, percAccomm = 1)
suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_ada_rob <- do_ada_robust(preproc$data, k, numRep, huge, 0.8,
                           FALSE, method = "adjbox")

str(res_ada_rob)

res_ada_rob1 <- do_ada_robust(preproc$data, k, numRep, huge, 0.8,
                             FALSE, vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
                             outl_degree = c("outl_strong", "outl_semi_strong",
                                              "outl_moderate"),
                             method = "toler")

str(res_ada_rob1)

## End(Not run)

```

do_alphas_rss

Alphas and RSS of every set of archetypoids

Description

In the ADALARA algorithm, every time that a set of archetypoids is computed using a sample of the data, the alpha coefficients and the associated residual sum of squares (RSS) for the entire data set must be computed.

Usage

```
do_alphas_rss(data, subset, huge, k_subset, rand_obs, alphas_subset,
              type_alg = "ada", PM, prob)
```

Arguments

data	Data matrix with all the observations.
subset	Data matrix with a sample of the data observations.
huge	Penalization added to solve the convex least squares problems.
k_subset	Archetypoids obtained from subset.
rand_obs	Sample observations that form subset.
alphas_subset	Alpha coefficients related to k_subset.
type_alg	String. Options are 'ada' for the non-robust multivariate adalara algorithm, 'ada_rob' for the robust multivariate adalara algorithm, 'fada' for the non-robust fda fadalara algorithm and 'fada_rob' for the robust fda fadalara algorithm.
PM	Penalty matrix obtained with eval.penalty . Needed when type_alg = 'fada' or type_alg = 'fada_rob'.
prob	Probability with values in [0,1]. Needed when type_alg = 'ada_rob' or type_alg = 'fada_rob'.

Value

A list with the following elements:

- rss Real number of the residual sum of squares.
- resid_rss Matrix with the residuals.
- alphas Matrix with the alpha values.

Author(s)

Guillermo Vinue

See Also

[archetypoids_norm_frob](#)

Examples

```
data(mtcars)
data <- mtcars
n <- nrow(data)
m <- 10

k <- 3
numRep <- 2
huge <- 200

suppressWarnings(RNGversion("3.5.0"))
set.seed(1)
rand_obs_si <- sample(1:n, size = m)

si <- data[rand_obs_si,]
ada_si <- do_ada(si, k, numRep, huge, FALSE)

k_si <- ada_si$cases
alphas_si <- ada_si$alphas
colnames(alphas_si) <- rownames(si)

rss_si <- do_alphas_rss(data, si, huge, k_si, rand_obs_si, alphas_si, "ada")
str(rss_si)
```

do_alphas_rss_multiv *Alphas and RSS of every set of multivariate archetypoids*

Description

In the ADALARA algorithm, every time that a set of archetypoids is computed using a sample of the data, the alpha coefficients and the associated residual sum of squares (RSS) for the entire data set must be computed.

Usage

```
do_alphas_rss_multiv(data, subset, huge, k_subset, rand_obs, alphas_subset,
                    type_alg = "ada", PM, prob, nbasis, nvars)
```

Arguments

data	Data matrix with all the observations.
subset	Data matrix with a sample of the data observations.
huge	Penalization added to solve the convex least squares problems.
k_subset	Archetypoids obtained from subset.
rand_obs	Sample observations that form subset.
alphas_subset	Alpha coefficients related to k_subset.
type_alg	String. Options are 'ada' for the non-robust multivariate adalara algorithm, 'ada_rob' for the robust multivariate adalara algorithm, 'fada' for the non-robust fda fadalara algorithm and 'fada_rob' for the robust fda fadalara algorithm.
PM	Penalty matrix obtained with eval.penalty . Needed when type_alg = 'fada' or type_alg = 'fada_rob'.
prob	Probability with values in [0,1]. Needed when type_alg = 'ada_rob' or type_alg = 'fada_rob'.
nbasis	Number of basis.
nvars	Number of variables.

Value

A list with the following elements:

- rss Real number of the residual sum of squares.
- resid_rss Matrix with the residuals.
- alphas Matrix with the alpha values.

Author(s)

Guillermo Vinue

See Also

[archetypoids_norm_frob](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]
```

```

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, ,1] <- as.matrix(hgtm)
data.array[, ,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, ,1])), nvars))
X[, ,1] <- t(temp_fd$coef[, ,1])
X[, ,2] <- t(temp_fd$coef[, ,2])

# Standardize the variables:
Xs <- X
Xs[, ,1] <- scale(X[, ,1])
Xs[, ,2] <- scale(X[, ,2])
# We have to give names to the dimensions to know the
# observations that were identified as archetypoids.
dimnames(Xs) <- list(paste("Obs", 1:dim(hgtm)[2], sep = ""),
                    1:nbasis,
                    c("boys", "girls"))

n <- dim(Xs)[1]
# Number of archetypoids:
k <- 3
numRep <- 20
huge <- 200

# Size of the random sample of observations:
m <- 15
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N
prob <- 0.75
data_alg <- Xs

nbasis <- dim(data_alg)[2] # number of basis.
nvars <- dim(data_alg)[3] # number of variables.
n <- nrow(data_alg)

suppressWarnings(RNGversion("3.5.0"))
set.seed(1)
rand_obs_si <- sample(1:n, size = m)

```

```

si <- apply(data_alg, 2:3, function(x) x[rand_obs_si])

fada_si <- do_fada_multiv_robust(si, k, numRep, huge, 0.8, FALSE, PM)

k_si <- fada_si$cases
alphas_si <- fada_si$alphas
colnames(alphas_si) <- rownames(si)

rss_si <- do_alphas_rss_multiv(data_alg, si, huge, k_si, rand_obs_si, alphas_si,
                             "fada_rob", PM, 0.8, nbasis, nvars)

str(rss_si)

## End(Not run)

```

do_clean

*Cleaning outliers***Description**

Cleaning of the most remarkable outliers. This improves the performance of the archetypoid algorithm since it is not affected by spurious points.

Usage

```
do_clean(data, num_pts, range = 1.5, out_perc = 80)
```

Arguments

data	Data frame with (temporal) points in the rows and observations in the columns.
num_pts	Number of temporal points.
range	Same parameter as in function boxplot . A value of 1.5 is enough to detect amplitude and shift outliers, while a value of 3 is needed to detect isolated outliers.
out_perc	Minimum number of temporal points (in percentage) to consider the observation as an outlier. Needed when range=1.5.

Value

Numeric vector with the outliers.

Author(s)

Irene Epifanio

See Also

[boxplot](#)

Examples

```
data(mtcars)
data <- mtcars
num_pts <- ncol(data)
do_clean(t(data), num_pts, 1.5, 80)
```

`do_clean_multiv`*Cleaning multivariate functional outliers*

Description

Cleaning of the most remarkable multivariate functional outliers. This improves the performance of the archetypoid algorithm since it is not affected by spurious points.

Usage

```
do_clean_multiv(data, num_pts, range = 1.5, out_perc = 80, nbasis, nvars)
```

Arguments

<code>data</code>	Data frame with (temporal) points in the rows and observations in the columns.
<code>num_pts</code>	Number of temporal points.
<code>range</code>	Same parameter as in function boxplot . A value of 1.5 is enough to detect amplitude and shift outliers, while a value of 3 is needed to detect isolated outliers.
<code>out_perc</code>	Minimum number of temporal points (in percentage) to consider the observation as an outlier. Needed when <code>range=1.5</code> .
<code>nbasis</code>	Number of basis.
<code>nvars</code>	Number of variables.

Value

List with the outliers for each variable.

Author(s)

Irene Epifanio

See Also

[boxplot](#)

Examples

```

## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, ,1])), nvars))
X[, ,1] <- t(temp_fd$coef[, ,1])
X[, ,2] <- t(temp_fd$coef[, ,2])

# Standardize the variables:
Xs <- X
Xs[, ,1] <- scale(X[, ,1])
Xs[, ,2] <- scale(X[, ,2])

x1 <- t(Xs[, ,1])
for (i in 2:nvars) {
  x12 <- t(Xs[, ,i])
  x1 <- rbind(x1, x12)
}
data_all <- t(x1)

num_pts <- ncol(data_all) / nvars
range <- 3
out1 <- do_clean_multiv(t(data_all), num_pts, range, out_perc, nbasis, nvars)
out1

## End(Not run)

```

do_fada *Run the whole functional archetypoid analysis with the Frobenius norm*

Description

This function executes the entire procedure involved in the functional archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the functional archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_fada(subset, numArchoid, numRep, huge, compare = FALSE, PM,
        vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
        outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
        method = "adjbox", prob)
```

Arguments

subset	Data to obtain archetypes. In fadalaria this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
compare	Boolean argument to compute the robust residual sum of squares to compare these results with the ones provided by do_fada_robust .
PM	Penalty matrix obtained with eval.penalty .
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.
prob	If compare=TRUE, probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_rob: If compare_robust=TRUE, this is the residual sum of squares using the robust Frobenius norm. Otherwise, NULL.
- resid: Vector of residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>

See Also

[stepArchetypesRawData_funcnt](#), [archetypoids_funcnt](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)

# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada <- do_fada(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
                  compare = FALSE, PM = PM, method = "adjbox")
str(res_fada)

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada1 <- do_fada(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
                  compare = FALSE, PM = PM,
                  vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
                  outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
                  method = "toler")
str(res_fada1)

res_fada2 <- do_fada(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
                  compare = TRUE, PM = PM, method = "adjbox", prob = 0.8)
str(res_fada2)

## End(Not run)
```

do_fada_multiv	<i>Run the whole archetypoid analysis with the functional multivariate Frobenius norm</i>
----------------	---

Description

This function executes the entire procedure involved in the functional archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the functional archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_fada_multiv(subset, numArchoid, numRep, huge, compare = FALSE, PM,
               method = "adjbox", prob)
```

Arguments

subset	Data to obtain archetypes. In fadalaria this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
compare	Boolean argument to compute the robust residual sum of squares to compare these results with the ones provided by do_fada_robust .
PM	Penalty matrix obtained with eval.penalty .
method	Method to compute the outliers. So far the only option allowed is 'adjbox' for using adjusted boxplots for skewed distributions. The use of tolerance intervals might also be explored in the future for the multivariate case.
prob	If compare=TRUE, probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_rob: If compare_robust=TRUE, this is the residual sum of squares using the robust Frobenius norm. Otherwise, NULL.
- resid: Vector of residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>

See Also

[stepArchetypesRawData_funct_multiv](#), [archetypoids_funct_multiv](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, ,1] <- as.matrix(hgtm)
data.array[, ,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, ,1])), nvars))
X[, ,1] <- t(temp_fd$coef[, ,1])
X[, ,2] <- t(temp_fd$coef[, ,2])

# Standardize the variables:
Xs <- X
Xs[, ,1] <- scale(X[, ,1])
Xs[, ,2] <- scale(X[, ,2])

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada <- do_fada_multiv(subset = Xs, numArchoid = 3, numRep = 5, huge = 200,
                          compare = FALSE, PM = PM, method = "adjbox")
str(res_fada)

## End(Not run)
```

do_fada_multiv_robust *Run the whole archetypoid analysis with the functional multivariate robust Frobenius norm*

Description

This function executes the entire procedure involved in the functional archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the functional archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_fada_multiv_robust(subset, numArchoid, numRep, huge, prob, compare = FALSE, PM,
                      method = "adjbox")
```

Arguments

subset	Data to obtain archetypes. In fadalaria this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization to solve the convex least squares problem, see archetypoids .
prob	Probability with values in [0,1].
compare	Boolean argument to compute the non-robust residual sum of squares to compare these results with the ones provided by do_fada .
PM	Penalty matrix obtained with eval.penalty .
method	Method to compute the outliers. So far the only option allowed is 'adjbox' for using adjusted boxplots for skewed distributions. The use of tolerance intervals might also be explored in the future for the multivariate case.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_non_rob: If compare=TRUE, this is the residual sum of squares using the non-robust Frobenius norm. Otherwise, NULL.
- resid Vector of residuals.
- outliers: Outliers.
- local_rel_imp Matrix with the local (casewise) relative importance (in percentage) of each variable for the outlier identification. Only for the multivariate case. It is relative to the outlier observation itself. The other observations are not considered for computing this importance. This procedure works because the functional variables are in the same scale, after standardizing. Otherwise, it couldn't be interpreted like that.

- `margi_rel_imp` Matrix with the marginal relative importance of each variable (in percentage) for the outlier identification. Only for the multivariate case. In this case, the other points are considered, since the value of the outlier observation is compared with the remaining points.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[stepArchetypesRawData_funct_multiv_robust](#), [archetypoids_funct_multiv_robust](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, ,1] <- as.matrix(hgtm)
data.array[, ,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, ,1])), nvars))
X[, ,1] <- t(temp_fd$coef[, ,1])
X[, ,2] <- t(temp_fd$coef[, ,2])

# Standardize the variables:
Xs <- X
Xs[, ,1] <- scale(X[, ,1])
Xs[, ,2] <- scale(X[, ,2])
```

```

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada <- do_fada_multiv_robust(subset = Xs, numArchoid = 3, numRep = 5, huge = 200,
                                prob = 0.75, compare = FALSE, PM = PM, method = "adjbox")

str(res_fada)
res_fada$cases
#[1] 8 24 29
res_fada$rss
#[1] 2.301741

## End(Not run)

```

do_fada_robust	<i>Run the whole archetypoid analysis with the functional robust Frobenius norm</i>
----------------	---

Description

This function executes the entire procedure involved in the functional archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the functional archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```

do_fada_robust(subset, numArchoid, numRep, huge, prob, compare = FALSE, PM,
               vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
               outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
               method = "adjbox")

```

Arguments

subset	Data to obtain archetypes. In fadalaria this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
compare	Boolean argument to compute the non-robust residual sum of squares to compare these results with the ones provided by do_fada .
PM	Penalty matrix obtained with eval.penalty .
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_non_rob: If compare=TRUE, this is the residual sum of squares using the non-robust Frobenius norm. Otherwise, NULL.
- resid: Vector of residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[stepArchetypesRawData_func_robust](#), [archetypoids_func_robust](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)

# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada_rob <- do_fada_robust(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
                             prob = 0.75, compare = FALSE, PM = PM, method = "adjbox")
str(res_fada_rob)

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada_rob1 <- do_fada_robust(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
```

```
        prob = 0.75, compare = FALSE, PM = PM,
        vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
        outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
        method = "toler")
str(res_fada_rob1)

## End(Not run)
```

do_knno

kNN for outlier detection

Description

Ramaswamy et al. proposed the k-nearest neighbors outlier detection method (kNNo). Each point's anomaly score is the distance to its kth nearest neighbor in the data set. Then, all points are ranked based on this distance. The higher an example's score is, the more anomalous it is.

Usage

```
do_knno(data, k, top_n)
```

Arguments

data	Data observations.
k	Number of neighbors of a point that we are interested in.
top_n	Total number of outliers we are interested in.

Value

Vector of outliers.

Author(s)

Guillermo Vinue

References

Ramaswamy, S., Rastogi, R. and Shim, K. Efficient Algorithms for Mining Outliers from Large Data Sets. SIGMOD'00 Proceedings of the 2000 ACM SIGMOD international conference on Management of data, 2000, 427-438.

Examples

```
data(mtcars)
data <- as.matrix(mtcars)
outl <- do_knno(data, 3, 2)
outl
data[outl,]
```

do_outl_degree	<i>Degree of outlierness</i>
----------------	------------------------------

Description

Classification of outliers according to their degree of outlierness. They are classified using the tolerance proportion. For instance, outliers from a 95

Usage

```
do_outl_degree(vect_tol = c(0.95, 0.9, 0.85), resid_vect, alpha = 0.05,
              outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"))
```

Arguments

vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85).
resid_vect	Vector of n residuals, where n was the number of rows of the data matrix.
alpha	Significance level. Default 0.05.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate").

Value

List with the type outliers.

Author(s)

Guillermo Vinue

See Also

[outl_toler](#)

Examples

```
do_outl_degree(0.95, 1:100, 0.05, "outl_strong")
```

fadalara	<i>Functional parallel archetypoid algorithm for large applications (FADALARA)</i>
----------	--

Description

The FADALARA algorithm is based on the CLARA clustering algorithm. This is the parallel version of the algorithm. It allows to detect anomalies (outliers). In the univariate case, there are two different methods to detect them: the adjusted boxplot (default and most reliable option) and tolerance intervals. In the multivariate case, only adjusted boxplots are used. If needed, tolerance intervals allow to define a degree of outlierness.

Usage

```
fadalara(data, N, m, numArchoid, numRep, huge, prob, type_alg = "fada",
         compare = FALSE, PM, vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
         outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
         method = "adjbox", multiv, frame)
```

Arguments

data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric. The data must have row names so that the algorithm can identify the archetypoids in every sample.
N	Number of samples.
m	Sample size of each sample.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
type_alg	String. Options are 'fada' for the non-robust fadalara algorithm, whereas 'fada_rob' is for the robust fadalara algorithm.
compare	Boolean argument to compute the robust residual sum of squares if type_alg = "fada" and the non-robust if type_alg = "fada_rob".
PM	Penalty matrix obtained with eval.penalty .
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals. The tolerance intervals are only computed in the univariate case, i.e., method='toler' only valid if multiv=FALSE.

multiv	Multivariate (TRUE) or univariate (FALSE) algorithm.
frame	Boolean value to indicate whether the frame is computed (Mair et al., 2017) or not. The frame is made up of a subset of extreme points, so the archetypoids are only computed on the frame. Low frame densities are obtained when only small portions of the data were extreme. However, high frame densities reduce this speed-up.

Value

A list with the following elements:

- cases Vector of archetypoids.
- rss Optimal residual sum of squares.
- outliers: Outliers.
- alphas: Matrix with the alpha coefficients.
- local_rel_imp Matrix with the local (casewise) relative importance (in percentage) of each variable for the outlier identification. Only for the multivariate case. It is relative to the outlier observation itself. The other observations are not considered for computing this importance. This procedure works because the functional variables are in the same scale, after standardizing. Otherwise, it couldn't be interpreted like that.
- margi_rel_imp Matrix with the marginal relative importance of each variable (in percentage) for the outlier identification. Only for the multivariate case. In this case, the other points are considered, since the value of the outlier observation is compared with the remaining points.

Author(s)

Guillermo Vinue, Irene Epifanio

References

- Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>
- Hubert, M. and Vandervieren, E., An adjusted boxplot for skewed distributions, 2008. *Computational Statistics and Data Analysis* **52(12)**, 5186-5201, <https://doi.org/10.1016/j.csda.2007.11.008>
- Kaufman, L. and Rousseeuw, P.J., Clustering Large Data Sets, 1986. *Pattern Recognition in Practice*, 425-437.
- Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.
- Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[do_fada](#), [do_fada_robust](#)

Examples

```

## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, , 1] <- as.matrix(hgtm)
data.array[, , 2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, , 1])), nvars))
X[, , 1] <- t(temp_fd$coef[, , 1])
X[, , 2] <- t(temp_fd$coef[, , 2])

# Standardize the variables:
Xs <- X
Xs[, , 1] <- scale(X[, , 1])
Xs[, , 2] <- scale(X[, , 2])
# We have to give names to the dimensions to know the
# observations that were identified as archetypoids.
dimnames(Xs) <- list(paste("Obs", 1:dim(hgtm)[2], sep = ""),
                    1:nbasis,
                    c("boys", "girls"))

n <- dim(Xs)[1]
# Number of archetypoids:
k <- 3
numRep <- 20
huge <- 200

# Size of the random sample of observations:
m <- 15
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N
prob <- 0.75
data_alg <- Xs

```

```

# Parallel:
# Prepare parallelization (including the seed for reproducibility):
library(doParallel)
no_cores <- detectCores() - 1
no_cores
cl <- makeCluster(no_cores)
registerDoParallel(cl)
clusterSetRNGStream(cl, iced = 2018)
res_fl <- fadalara(data = data_alg, N = N, m = m, numArchoid = k, numRep = numRep,
                 huge = huge, prob = prob, type_alg = "fada_rob", compare = FALSE,
                 PM = PM, method = "adjbox", multiv = TRUE, frame = FALSE) # frame = TRUE
stopCluster(cl)

res_fl_copy <- res_fl
res_fl <- res_fl[which.min(unlist(sapply(res_fl, function(x) x[2])))[[1]]]
str(res_fl)
res_fl$cases
res_fl$rss
as.vector(res_fl$outliers)

## End(Not run)

```

fadalara_no_parallel	<i>Functional non-parallel archetypoid algorithm for large applications (FADALARA)</i>
----------------------	--

Description

The FADALARA algorithm is based on the CLARA clustering algorithm. This is the non-parallel version of the algorithm. It allows to detect anomalies (outliers). In the univariate case, there are two different methods to detect them: the adjusted boxplot (default and most reliable option) and tolerance intervals. In the multivariate case, only adjusted boxplots are used. If needed, tolerance intervals allow to define a degree of outlierness.

Usage

```

fadalara_no_parallel(data, seed, N, m, numArchoid, numRep, huge, prob, type_alg = "fada",
                    compare = FALSE, verbose = TRUE, PM, vect_tol = c(0.95, 0.9, 0.85),
                    alpha = 0.05, outl_degree = c("outl_strong", "outl_semi_strong",
                    "outl_moderate"), method = "adjbox", multiv, frame)

```

Arguments

data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable (temporal point). All variables are numeric. The data must have row names so that the algorithm can identify the archetypoids in every sample.
------	--

seed	Integer value to set the seed. This ensures reproducibility.
N	Number of samples.
m	Sample size of each sample.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
type_alg	String. Options are 'fada' for the non-robust fadalara algorithm, whereas 'fada_rob' is for the robust fadalara algorithm.
compare	Boolean argument to compute the robust residual sum of squares if type_alg = "fada" and the non-robust if type_alg = "fada_rob".
verbose	Display progress? Default TRUE.
PM	Penalty matrix obtained with eval.penalty .
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals. The tolerance intervals are only computed in the univariate case, i.e., method='toler' only valid if multiv = FALSE.
multiv	Multivariate (TRUE) or univariate (FALSE) algorithm.
frame	Boolean value to indicate whether the frame is computed (Mair et al., 2017) or not. The frame is made up of a subset of extreme points, so the archetypoids are only computed on the frame. Low frame densities are obtained when only small portions of the data were extreme. However, high frame densities reduce this speed-up.

Value

A list with the following elements:

- cases Vector of archetypoids.
- rss Optimal residual sum of squares.
- outliers: Vector of outliers.
- alphas: Matrix with the alpha coefficients.
- local_rel_imp Matrix with the local (casewise) relative importance (in percentage) of each variable for the outlier identification. Only for the multivariate case. It is relative to the outlier observation itself. The other observations are not considered for computing this importance. This procedure works because the functional variables are in the same scale, after standardizing. Otherwise, it couldn't be interpreted like that.
- margi_rel_imp Matrix with the marginal relative importance of each variable (in percentage) for the outlier identification. Only for the multivariate case. In this case, the other points are considered, since the value of the outlier observation is compared with the remaining points.

Author(s)

Guillermo Vinue, Irene Epifanio

References

- Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>
- Hubert, M. and Vandervieren, E., An adjusted boxplot for skewed distributions, 2008. *Computational Statistics and Data Analysis* **52(12)**, 5186-5201, <https://doi.org/10.1016/j.csda.2007.11.008>
- Kaufman, L. and Rousseeuw, P.J., Clustering Large Data Sets, 1986. *Pattern Recognition in Practice*, 425-437.
- Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.
- Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[fadalara](#)

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, ,1] <- as.matrix(hgtm)
data.array[, ,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, ,1])), nvars))
```

```

X[,1] <- t(temp_fd$coef[,1])
X[,2] <- t(temp_fd$coef[,2])

# Standardize the variables:
Xs <- X
Xs[,1] <- scale(X[,1])
Xs[,2] <- scale(X[,2])
# We have to give names to the dimensions to know the
# observations that were identified as archetypoids.
dimnames(Xs) <- list(paste("Obs", 1:dim(hgtm)[2], sep = ""),
                    1:nbasis,
                    c("boys", "girls"))

n <- dim(Xs)[1]
# Number of archetypoids:
k <- 3
numRep <- 20
huge <- 200

# Size of the random sample of observations:
m <- 15
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N
prob <- 0.75
data_alg <- Xs

seed <- 2018
res_fl <- fadalara_no_parallel(data = data_alg, seed = seed, N = N, m = m,
                              numArchoid = k, numRep = numRep, huge = huge,
                              prob = prob, type_alg = "fada_rob", compare = FALSE,
                              verbose = TRUE, PM = PM, method = "adjbox", multiv = TRUE,
                              frame = FALSE) # frame = TRUE

str(res_fl)
res_fl$cases
res_fl$rss
as.vector(res_fl$outliers)

## End(Not run)

```

frame_in_r

Compute archetypes frame

Description

Computing the frame with the approach by Mair et al. (2017).

Usage

```
frame_in_r(X)
```

Arguments

`X` Data frame.

Value

Vector with the observations that belong to the frame.

Author(s)

Sebastian Mair, code kindly provided by him.

References

Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.

Examples

```
## Not run:  
X <- mtcars  
q <- frame_in_r(X)  
H <- X[q,]  
q  
  
## End(Not run)
```

frobenius_norm

Frobenius norm

Description

Computes the Frobenius norm.

Usage

```
frobenius_norm(m)
```

Arguments

`m` Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p -dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>

Vinue, G., Epifanio, I., and Alemany, S., Archetypoids: a new approach to define representative archetypal data, 2015. *Computational Statistics and Data Analysis* **87**, 102-115, <https://doi.org/10.1016/j.csda.2015.01.018>

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, <https://doi.org/10.18637/jss.v077.i06>

Examples

```
mat <- matrix(1:4, nrow = 2)
frobienius_norm(mat)
```

frobienius_norm_funct *Functional Frobenius norm*

Description

Computes the functional Frobenius norm.

Usage

```
frobienius_norm_funct(m, PM)
```

Arguments

<code>m</code>	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
<code>PM</code>	Penalty matrix obtained with eval.penalty .

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p -dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>

Examples

```
library(fda)
mat <- matrix(1:9, nrow = 3)
fbasis <- create.fourier.basis(rangeval = c(1, 32), nbasis = 3)
PM <- eval.penalty(fbasis)
frobenius_norm_funct(mat, PM)
```

frobenius_norm_funct_multiv

Functional multivariate Frobenius norm

Description

Computes the functional multivariate Frobenius norm.

Usage

```
frobenius_norm_funct_multiv(m, PM)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
PM	Penalty matrix obtained with <code>eval.penalty</code> .

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p -dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>

Examples

```
mat <- matrix(1:400, ncol = 20)
PM <- matrix(1:100, ncol = 10)
frobienus_norm_funct_multiv(mat, PM)
```

frobienus_norm_funct_multiv_robust

Functional multivariate robust Frobenius norm

Description

Computes the functional multivariate robust Frobenius norm.

Usage

```
frobienus_norm_funct_multiv_robust(m, PM, prob, nbasis, nvars)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
PM	Penalty matrix obtained with eval.penalty .
prob	Probability with values in [0,1].
nbasis	Number of basis.
nvars	Number of variables.

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
mat <- matrix(1:400, ncol = 20)
PM <- matrix(1:100, ncol = 10)
frobenius_norm_funct_multiv_robust(mat, PM, 0.8, 10, 2)
```

frobenius_norm_funct_robust

Functional robust Frobenius norm

Description

Computes the functional robust Frobenius norm.

Usage

```
frobenius_norm_funct_robust(m, PM, prob)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
PM	Penalty matrix obtained with eval.penalty .
prob	Probability with values in [0,1].

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
library(fda)
mat <- matrix(1:9, nrow = 3)
fbasis <- create.fourier.basis(rangeval = c(1, 32), nbasis = 3)
PM <- eval.penalty(fbasis)
frobienius_norm_funct_robust(mat, PM, 0.8)
```

frobienius_norm_robust *Robust Frobenius norm*

Description

Computes the robust Frobenius norm.

Usage

```
frobienius_norm_robust(m, prob)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
prob	Probability with values in [0,1].

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
mat <- matrix(1:4, nrow = 2)
frobenius_norm_robust(mat, 0.8)
```

int_prod_mat

Interior product between matrices

Description

Helper function to compute the Frobenius norm.

Usage

```
int_prod_mat(m)
```

Arguments

m Data matrix.

Value

Data matrix.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
mat <- matrix(1:4, nrow = 2)
int_prod_mat(mat)
```

int_prod_mat_funct *Interior product between matrices for FDA*

Description

Helper function to compute the Frobenius norm in the functional data analysis (FDA) scenario.

Usage

```
int_prod_mat_funct(m, PM)
```

Arguments

m	Data matrix.
PM	Penalty matrix obtained with eval.penalty .

Value

Data matrix.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
library(fda)
mat <- matrix(1:9, nrow = 3)
fbasis <- create.fourier.basis(rangeval = c(1, 32), nbasis = 3)
PM <- eval.penalty(fbasis)
int_prod_mat_funct(mat, PM)
```

int_prod_mat_sq *Squared interior product between matrices*

Description

Helper function to compute the robust Frobenius norm.

Usage

```
int_prod_mat_sq(m)
```

Arguments

m Data matrix.

Value

Data matrix.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
mat <- matrix(1:4, nrow = 2)
int_prod_mat_sq(mat)
```

int_prod_mat_sq_funct *Squared interior product between matrices for FDA*

Description

Helper function to compute the robust Frobenius norm in the functional data analysis (FDA) scenario.

Usage

```
int_prod_mat_sq_funct(m, PM)
```

Arguments

m Data matrix.
PM Penalty matrix obtained with `eval.penalty`.

Value

Data matrix.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
library(fda)
mat <- matrix(1:9, nrow = 3)
fbasis <- create.fourier.basis(rangeval = c(1, 32), nbasis = 3)
PM <- eval.penalty(fbasis)
int_prod_mat_sq_funct(mat, PM)
```

outl_toler	<i>Tolerance outliers</i>
------------	---------------------------

Description

Outliers according to a tolerance interval. This function is used by the archetypoid algorithms to identify the outliers. See the function `nptol.int` in package `tolerance`.

Usage

```
outl_toler(p_tol = 0.95, resid_vect, alpha = 0.05)
```

Arguments

p_tol The proportion of observations to be covered by this tolerance interval.
resid_vect Vector of n residuals, where n was the number of rows of the data matrix.
alpha Significance level.

Value

Vector with the outliers.

Author(s)

Guillermo Vinue

References

Young, D., tolerance: An R package for estimating tolerance intervals, 2010. *Journal of Statistical Software*, **36(5)**, 1-39, <https://doi.org/10.18637/jss.v036.i05>

See Also

[adalara](#), [fadalara](#), [do_outl_degree](#)

Examples

```
outl_toler(0.95, 1:100, 0.05)
```

stepArchetypesRawData_func

Archetype algorithm to raw data with the functional Frobenius norm

Description

This is a slight modification of [stepArchetypesRawData](#) to use the functional archetype algorithm with the Frobenius norm.

Usage

```
stepArchetypesRawData_func(data, numArch, numRep = 3,  
                           verbose = TRUE, saveHistory = FALSE, PM)
```

Arguments

<code>data</code>	Data to obtain archetypes.
<code>numArch</code>	Number of archetypes to compute, from 1 to numArch.
<code>numRep</code>	For each numArch, run the archetype algorithm numRep times.
<code>verbose</code>	If TRUE, the progress during execution is shown.
<code>saveHistory</code>	Save execution steps.
<code>PM</code>	Penalty matrix obtained with eval.penalty .

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

- Cutler, A. and Breiman, L., Archetypal Analysis. *Technometrics*, 1994, **36(4)**, 338-347, <https://doi.org/10.2307/1269949>
- Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>
- Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)
# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

lass <- stepArchetypesRawData_funct(data = data_archs, numArch = 3,
                                   numRep = 5, verbose = FALSE,
                                   saveHistory = FALSE, PM)

str(lass)
length(lass[[1]])
class(lass[[1]])
class(lass[[1]][[5]])

## End(Not run)
```

```
stepArchetypesRawData_funct_multiv
```

*Archetype algorithm to raw data with the functional multivariate
Frobenius norm*

Description

This is a slight modification of [stepArchetypesRawData](#) to use the functional archetype algorithm with the multivariate Frobenius norm.

Usage

```
stepArchetypesRawData_funct_multiv(data, numArch, numRep = 3,
                                   verbose = TRUE, saveHistory = FALSE, PM)
```

Arguments

data	Data to obtain archetypes.
numArch	Number of archetypes to compute, from 1 to numArch.
numRep	For each numArch, run the archetype algorithm numRep times.
verbose	If TRUE, the progress during execution is shown.
saveHistory	Save execution steps.
PM	Penalty matrix obtained with <code>eval.penalty</code> .

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

- Cutler, A. and Breiman, L., Archetypal Analysis. *Technometrics*, 1994, **36(4)**, 338-347, <https://doi.org/10.2307/1269949>
- Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>
- Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, ,1] <- as.matrix(hgtm)
data.array[, ,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
```

```

temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[, , 1])), nvars))
X[, , 1] <- t(temp_fd$coef[, , 1])
X[, , 2] <- t(temp_fd$coef[, , 2])

# Standardize the variables:
Xs <- X
Xs[, , 1] <- scale(X[, , 1])
Xs[, , 2] <- scale(X[, , 2])

lass <- stepArchetypesRawData_func_multiv(data = Xs, numArch = 3,
                                         numRep = 5, verbose = FALSE,
                                         saveHistory = FALSE, PM)

str(lass)
length(lass[[1]])
class(lass[[1]])
class(lass[[1]][[5]])

## End(Not run)

```

```
stepArchetypesRawData_func_multiv_robust
```

Archetype algorithm to raw data with the functional multivariate robust Frobenius norm

Description

This is a slight modification of [stepArchetypesRawData](#) to use the functional archetype algorithm with the multivariate Frobenius norm.

Usage

```
stepArchetypesRawData_func_multiv_robust(data, numArch, numRep = 3,
                                         verbose = TRUE, saveHistory = FALSE, PM, prob, nbasis, nvars)
```

Arguments

data	Data to obtain archetypes.
numArch	Number of archetypes to compute, from 1 to numArch.
numRep	For each numArch, run the archetype algorithm numRep times.
verbose	If TRUE, the progress during execution is shown.
saveHistory	Save execution steps.
PM	Penalty matrix obtained with eval.penalty .

prob	Probability with values in [0,1].
nbasis	Number of basis.
nvars	Number of variables.

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Cutler, A. and Breiman, L., Archetypal Analysis. *Technometrics*, 1994, **36(4)**, 338-347, <https://doi.org/10.2307/1269949>

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[, ,1] <- as.matrix(hgtm)
data.array[, ,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)
```

```

X <- array(0, dim = c(dim(t(temp_fd$coefs[, , 1])), nvars))
X[, , 1] <- t(temp_fd$coef[, , 1])
X[, , 2] <- t(temp_fd$coef[, , 2])

# Standardize the variables:
Xs <- X
Xs[, , 1] <- scale(X[, , 1])
Xs[, , 2] <- scale(X[, , 2])

lass <- stepArchetypesRawData_func_multiv_robust(data = Xs, numArch = 3,
                                                numRep = 5, verbose = FALSE,
                                                saveHistory = FALSE, PM, prob = 0.8,
                                                nbasis, nvars)

str(lass)
length(lass[[1]])
class(lass[[1]])
class(lass[[1]][[5]])

## End(Not run)

```

```
stepArchetypesRawData_func_robust
```

Archetype algorithm to raw data with the functional robust Frobenius norm

Description

This is a slight modification of [stepArchetypesRawData](#) to use the functional archetype algorithm with the functional robust Frobenius norm.

Usage

```
stepArchetypesRawData_func_robust(data, numArch, numRep = 3,
                                  verbose = TRUE, saveHistory = FALSE, PM, prob)
```

Arguments

<code>data</code>	Data to obtain archetypes.
<code>numArch</code>	Number of archetypes to compute, from 1 to numArch.
<code>numRep</code>	For each numArch, run the archetype algorithm numRep times.
<code>verbose</code>	If TRUE, the progress during execution is shown.
<code>saveHistory</code>	Save execution steps.
<code>PM</code>	Penalty matrix obtained with eval.penalty .
<code>prob</code>	Probability with values in [0,1].

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Cutler, A. and Breiman, L., Archetypal Analysis. *Technometrics*, 1994, **36(4)**, 338-347, <https://doi.org/10.2307/1269949>

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, <https://doi.org/10.1016/j.csda.2016.06.007>

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)
# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

lass <- stepArchetypesRawData_func_robust(data = data_archs, numArch = 3,
                                         numRep = 5, verbose = FALSE,
                                         saveHistory = FALSE, PM, prob = 0.8)

str(lass)
length(lass[[1]])
class(lass[[1]])
class(lass[[1]][[5]])

## End(Not run)
```

`stepArchetypesRawData_norm_frob`*Archetype algorithm to raw data with the Frobenius norm*

Description

This is a slight modification of `stepArchetypesRawData` to use the archetype algorithm with the Frobenius norm.

Usage

```
stepArchetypesRawData_norm_frob(data, numArch, numRep = 3,  
                                verbose = TRUE, saveHistory = FALSE)
```

Arguments

<code>data</code>	Data to obtain archetypes.
<code>numArch</code>	Number of archetypes to compute, from 1 to <code>numArch</code> .
<code>numRep</code>	For each <code>numArch</code> , run the archetype algorithm <code>numRep</code> times.
<code>verbose</code>	If TRUE, the progress during execution is shown.
<code>saveHistory</code>	Save execution steps.

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, <https://doi.org/10.18637/jss.v030.i08>

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

Vinue, G., Epifanio, I., and Alemany, S., Archetypoids: a new approach to define representative archetypal data, 2015. *Computational Statistics and Data Analysis* **87**, 102-115, <https://doi.org/10.1016/j.csda.2015.01.018>

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, <https://doi.org/10.18637/jss.v077.i06>

See Also

[stepArchetypesRawData](#), [stepArchetypes](#)

Examples

```
data(mtcars)
data <- as.matrix(mtcars)

numArch <- 5
numRep <- 2

lass <- stepArchetypesRawData_norm_frob(data = data, numArch = 1:numArch,
                                       numRep = numRep, verbose = FALSE)

str(lass)
length(lass[[1]])
class(lass[[1]])
```

stepArchetypesRawData_robust

Archetype algorithm to raw data with the robust Frobenius norm

Description

This is a slight modification of [stepArchetypesRawData](#) to use the archetype algorithm with the robust Frobenius norm.

Usage

```
stepArchetypesRawData_robust(data, numArch, numRep = 3,
                             verbose = TRUE, saveHistory = FALSE, prob)
```

Arguments

data	Data to obtain archetypes.
numArch	Number of archetypes to compute, from 1 to numArch.
numRep	For each numArch, run the archetype algorithm numRep times.
verbose	If TRUE, the progress during execution is shown.
saveHistory	Save execution steps.
prob	Probability with values in [0,1].

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. <https://doi.org/10.1016/j.physa.2018.12.036>

See Also

[stepArchetypesRawData_norm_frob](#)

Examples

```
data(mtcars)
data <- as.matrix(mtcars)

numArch <- 5
numRep <- 2

lass <- stepArchetypesRawData_robust(data = data, numArch = 1:numArch,
                                   numRep = numRep, verbose = FALSE,
                                   saveHistory = FALSE, prob = 0.8)

str(lass)
length(lass[[1]])
class(lass[[1]])
```

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