

Package ‘alqrfe’

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Title Adaptive Lasso Quantile Regression with Fixed Effects

Version 1.3

Description

Quantile regression with fixed effects solves longitudinal data, considering the individual intercepts as fixed effects. The parametric set of this type of problem used to be huge. Thus penalized methods such as Lasso are currently applied. Adaptive Lasso presents oracle properties, which include Gaussianity and correct model selection. Bayesian information criteria (BIC) estimates the optimal tuning parameter lambda. Plot tools are also available.

License GPL (>= 2)

Depends R (>= 4.4.0)

Imports Rcpp (>= 1.0.5), MASS (>= 7.3-49), stats

LinkingTo Rcpp, RcppArmadillo

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Config/testthat/edition 3

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clean_data	<i>Clean missings</i>
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Description

Clean missings

Usage

```
clean_data(y, x, id)
```

Arguments

y	Numeric vector, outcome.
x	Numeric matrix, covariates
id	Numeric vector, identifies the unit to which the observation belongs.

Value

list with the same objects y, x, id, but without missings.

Examples

```
n = 10
m = 4
d = 3
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)
x[1,3] = NA
clean_data(y=y, x=x, id=subj)
```

mqr *multiple penalized quantile regression*

Description

Estimate QR for several taus

Usage

```
mqr(x, y, subj, tau = 1:9/10, method = "qr", ngrid = 20, inf = 1e-08, digt = 4)
```

Arguments

x	Numeric matrix, covariates
y	Numeric vector, outcome.
subj	Numeric vector, identifies the unit to which the observation belongs.
tau	Numeric vector, identifies the percentiles.
method	Factor, "qr" quantile regression, "qrfe" quantile regression with fixed effects, "lqrfe" Lasso quantile regression with fixed effects, "alqr" adaptive Lasso quantile regression with fixed effects.
ngrid	Numeric scalar greater than one, number of BIC to test.
inf	Numeric scalar, internal value, small value.
digt	Numeric scalar, internal value greater than one, define "zero" coefficient.

Value

Beta Numeric array, with three dimensions: 1) tau, 2) coef., lower bound, upper bound, 3) exploratory variables.

Examples

```
n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)
```

```
Beta = mqr(x,y,subj,tau=1:9/10, method="qr", ngrid = 10)
Beta
```

mqr_alpha

*multiple penalized quantile regression - alpha***Description**

Estimate QR intercepts for several taus

Usage

```
mqr_alpha(
  x,
  y,
  subj,
  tau = 1:9/10,
  method = "qr",
  ngrid = 20,
  inf = 1e-08,
  digt = 4
)
```

Arguments

x	Numeric matrix, covariates
y	Numeric vector, outcome.
subj	Numeric vector, identifies the unit to which the observation belongs.
tau	Numeric vector, identifies the percentiles.
method	Factor, "qr" quantile regression, "qrfe" quantile regression with fixed effects, "lqrfe" Lasso quantile regression with fixed effects, "alqr" adaptive Lasso quantile regression with fixed effects.
ngrid	Numeric scalar greater than one, number of BIC to test.
inf	Numeric scalar, internal value, small value.
digt	Numeric scalar, internal value greater than one, define "zero" coefficient.

Value

Alpha Numeric array, with three dimensions: 1) tau, 2) coef., lower bound, upper bound, 3) exploratory variables.

Examples

```
n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
```

```

subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)

Alpha = mqr(x,y,subj,tau=1:9/10, method="qr", ngrid = 10)
Alpha

```

plot_alpha

plot multiple penalized quantile regression - alpha

Description

plot QR intercepts for several taus

Usage

```

plot_alpha(
  Beta,
  tau = 1:9/10,
  D,
  ylab = expression(alpha[1]),
  col = 2,
  lwd = 1,
  lty = 2,
  pch = 1,
  cex.axis = 1,
  cex.lab = 1,
  main = ""
)

```

Arguments

Beta	Numeric array, with three dimensions: 1) tau, 2) coef., lower bound, upper bound, 3) exploratory variables.
tau	Numeric vector, identifies the percentiles.
D	intercept's number.
ylab	y legend
col	color.
lwd	line width.
lty	line type.
pch	point character.
cex.axis	cex axis length.
cex.lab	cex axis length.
main	title.

Examples

```

n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)

Beta = mqr_alpha(x,y,subj,tau=1:9/10, method="qr", ngrid = 10)
plot_alpha(Beta,tau=1:9/10,D=1)

```

plot_taus

plot multiple penalized quantile regression

Description

plot QR for several taus

Usage

```

plot_taus(
  Beta,
  tau = 1:9/10,
  D,
  col = 2,
  lwd = 1,
  lty = 2,
  pch = 1,
  cex.axis = 1,
  cex.lab = 1,
  main = ""
)

```

Arguments

Beta	Numeric array, with three dimensions: 1) tau, 2) coef., lower bound, upper bound, 3) exploratory variables.
tau	Numeric vector, identifies the percentiles.
D	covariate's number.
col	color.

lwd	line width.
lty	line type.
pch	point character.
cex.axis	cex axis length.
cex.lab	cex axis length.
main	title.

Examples

```

n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)

Beta = mqr(x,y,subj,tau=1:9/10, method="qr", ngrid = 10)
plot_taus(Beta,tau=1:9/10,D=1)

```

qr

quantile regression

Description

Estimate quantile regression parameters for any quantile.

Remarks:

1. If the first column of 'x' is entirely equal to 1, then the first element of 'beta' represents the common intercept. Otherwise, there is no default common intercept (unlike the default behavior in 'lm').
2. If there is a common intercept and 'method' is "qrfe", "lqrfe" or "alqrfe", a 'sum-to-zero constraint' is applied on the 'alpha' parameters:

$$\sum_{i=1}^n \alpha_i = 0$$

This follows the approach in Danilevicz (2025).

Usage

```
qr(x, y, subj, tau = 0.5, method = "qrfe", ngrid = 20, inf = 1e-08, digit = 4)
```

Arguments

x	Numeric matrix, covariates
y	Numeric vector, outcome.
subj	Numeric vector, identifies the unit to which the observation belongs.
tau	Numeric, identifies the percentile.
method	Factor, "qr" quantile regression, "qrfe" quantile regression with fixed effects, "lqrfe" Lasso quantile regression with fixed effects, "alqrfe" adaptive Lasso quantile regression with fixed effects.
ngrid	Numeric scalar greater than one, number of BIC to test.
inf	Numeric scalar, internal value, small value.
digtl	Numeric scalar, internal value greater than one, define "zero" coefficient.

Value

alpha	Numeric vector, intercepts' coefficients.
beta	Numeric vector, exploratory variables' coefficients.
lambda	Numeric, estimated lambda.
res	Numeric vector, percentile residuals.
tau	Numeric scalar, the percentile.
penalty	Numeric scalar, indicate the chosen effect.
sig2_alpha	Numeric vector, intercepts' standard errors.
sig2_beta	Numeric vector, exploratory variables' standard errors.
Tab_alpha	Data.frame, intercepts' summary.
Tab_beta	Data.frame, exploratory variables' summary.
Mat_alpha	Numeric matrix, intercepts' summary.
Mat_beta	Numeric matrix, exploratory variables' summary.
method	Factor, method applied.

References

- Danilevicz, I.M., Bondon, P., Reisen, V.A. (2025) "Adaptive LASSO Quantile Regression with Fixed Effects", *Appl. Math. Model.*, xx (xx), <doi:10.1016/j.apm.2025.116600>
- Danilevicz, I.M., Reisen, V.A., Bondon, P. (2024) "Expectile and M-quantile regression for panel data", *Stat. Comput.*, 34 (97), <doi:10.1007/s11222-024-10396-7>
- Koenker, R. (2004) "Quantile regression for longitudinal data", *J. Multivar. Anal.*, 91(1): 74-89, <doi:10.1016/j.jmva.2004.05.006>

Examples

```
# Example 1
n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)
m1 = qr(x,y,subj,tau=0.75, method="qrfe")
m1
m2 = qr(x,y,subj,tau=0.3, method="lqrfe", ngrid = 10)
m2

# Example 2, from MASS package
Rabbit = MASS::Rabbit
Rabbit$Treatment = ifelse(Rabbit$Treatment=="Control",0,1)
Rabbit$Animal = ifelse(Rabbit$Animal == "R1",1,ifelse(Rabbit$Animal == "R2",2,
ifelse(Rabbit$Animal == "R3",3,ifelse(Rabbit$Animal == "R4",4,5))))
X = matrix(cbind(Rabbit$Dose,Rabbit$Treatment), ncol=2)
m3 = qr(x=X, y=Rabbit$BPchange, subj=Rabbit$Animal,tau=0.5, method="alqrfe", ngrid = 10)
m3
```

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