

Package ‘ambit’

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 acf_Exp

Autocorrelation function of the exponential trawl function

Description

This function computes the autocorrelation function associated with the exponential trawl function.

Usage

```
acf_Exp(x, lambda)
```

Arguments

x	The argument (lag) at which the autocorrelation function associated with the exponential trawl function will be evaluated
lambda	parameter in the exponential trawl

Details

The trawl function is parametrised by the parameter $\lambda > 0$ as follows:

$$g(x) = e^{\lambda x}, \text{ for } x \leq 0.$$

Its autocorrelation function is given by:

$$r(x) = e^{-\lambda x}, \text{ for } x \geq 0.$$

Value

The autocorrelation function of the exponential trawl function evaluated at x

Examples

```
acf_Exp(1, 0.1)
```

acf_LM

Autocorrelation function of the long memory trawl function

Description

This function computes the autocorrelation function associated with the long memory trawl function.

Usage

```
acf_LM(x, alpha, H)
```

Arguments

x	The argument (lag) at which the autocorrelation function associated with the long memory trawl function will be evaluated
alpha	parameter in the long memory trawl
H	parameter in the long memory trawl

Details

The trawl function is parametrised by the two parameters $H > 1$ and $\alpha > 0$ as follows:

$$g(x) = (1 - x/\alpha)^{-H}, \text{ for } x \leq 0.$$

Its autocorrelation function is given by

$$r(x) = (1 + x/\alpha)^{(1-H)}, \text{ for } x \geq 0.$$

Value

The autocorrelation function of the long memory trawl function evaluated at x

Examples

```
acf_LM(1, 0.3, 1.5)
```

```
acf_supIG
```

Autocorrelation function of the supIG trawl function

Description

This function computes the autocorrelation function associated with the supIG trawl function.

Usage

```
acf_supIG(x, delta, gamma)
```

Arguments

x	The argument (lag) at which the autocorrelation function associated with the supIG trawl function will be evaluated
delta	parameter in the supIG trawl
gamma	parameter in the supIG trawl

Details

The trawl function is parametrised by the two parameters $\delta \geq 0$ and $\gamma \geq 0$ as follows:

$$g(x) = (1 - 2x\gamma^{-2})^{-1/2} \exp(\delta\gamma(1 - (1 - 2x\gamma^{-2})^{1/2})), \text{ for } x \leq 0.$$

It is assumed that δ and γ are not simultaneously equal to zero. Its autocorrelation function is given by:

$$r(x) = \exp(\delta\gamma(1 - \sqrt{1 + 2x/\gamma^2})), \text{ for } x \geq 0.$$

Value

The autocorrelation function of the supIG trawl function evaluated at x

Examples

```
acf_supIG(1,0.3,0.1)
```

AddSlices_Rcpp	<i>Add slices and return vector of the sums of slices</i>
----------------	---

Description

Add slices and return vector of the sums of slices

Usage

```
AddSlices_Rcpp(slicematrix)
```

Arguments

slicematrix A matrix of slices.

Value

Returns the vector of the sums of the slices

AddWeightedSlices_Rcpp	<i>Add slices and return vector of the weighted sums of slices</i>
------------------------	--

Description

Add slices and return vector of the weighted sums of slices

Usage

```
AddWeightedSlices_Rcpp(slicematrix, weightvector)
```

Arguments

slicematrix A matrix of slices.
weightvector A vector of weights.

Value

Returns the vector of the weighted sums of the slices

asymptotic_variance	<i>Computing the true asymptotic variance in the CLT of the trawl estimation</i>
---------------------	--

Description

This function computes the theoretical asymptotic variance appearing in the CLT of the trawl process for a given trawl function and fourth cumulant.

Usage

```
asymptotic_variance(t, c4, varlevyseed = 1, trawlfct, trawlfct_par)
```

Arguments

t	Time point at which the asymptotic variance is computed
c4	The fourth cumulant of the Levy seed of the trawl process
varlevyseed	The variance of the Levy seed of the trawl process, the default is 1
trawlfct	The trawl function for which the asymptotic variance will be computed (Exp, supIG or LM)
trawlfct_par	The parameter vector of the trawl function (Exp: lambda, supIG: delta, gamma, LM: alpha, H)

Details

As derived in Sauri and Veraart (2022), the asymptotic variance in the central limit theorem for the trawl function estimation is given by

$$\sigma_a^2(t) = c_4(L')a(t) + 2\left\{\int_0^\infty a(s)^2 ds + \int_0^t a(t-s)a(t+s) ds - \int_t^\infty a(s-t)a(t+s) ds\right\},$$

for $t > 0$. The integrals in the above formula are approximated numerically.

Value

The function returns $\sigma_a^2(t)$.

Examples

```
#Compute the asymptotic variance at time t for an exponential trawl with
#parameter 2; here we assume that the fourth cumulant equals 1.
av<-asymptotic_variance(t=1, c4=1, varlevyseed=1, trawlfct="Exp", trawlfct_par=2)
#Print the av
av$v
#Print the four components of the asymptotic variance separately
av$v1
av$v2
av$v3
```

```

av$v4

#Note that v=v1+v2+v3+v4
av$v
av$v1+av$v2+av$v3+av$v4

```

asymptotic_variance_est

Estimating the asymptotic variance in the trawl function CLT

Description

This function estimates the asymptotic variance which appears in the CLT for the trawl function estimation.

Usage

```
asymptotic_variance_est(t, c4, varlevyseed = 1, Delta, avector, N = NULL)
```

Arguments

t	The time point at which to compute the asymptotic variance
c4	The fourth cumulant of the Levy seed of the trawl process
varlevyseed	The variance of the Levy seed of the trawl process, the default is 1
Delta	The width Delta of the observation grid
avector	The vector $(\hat{a}(0), \hat{a}(\Delta_n), \dots, \hat{a}((n-1)\Delta_n))$
N	The optional parameter to specify the upper bound N_n in the computations of the estimators

Details

As derived in Sauri and Veraart (2022), the estimated asymptotic variance is given by

$$\hat{\sigma}_a^2(t) = \hat{v}_1(t) + \hat{v}_2(t) + \hat{v}_3(t) + \hat{v}_4(t),$$

where

$$\hat{v}_1(t) := \widehat{c_4(L')\hat{a}(t)} = RQ_n \hat{a}(t) / \hat{a}(0),$$

for

$$RQ_n := \frac{1}{\sqrt{2n\Delta_n}} \sum_{k=0}^{n-2} (X_{(k+1)\Delta_n} - X_{k\Delta_n})^4,$$

and

$$\hat{v}_2(t) := 2 \sum_{l=0}^{N_n} \hat{a}^2(l\Delta_n) \Delta_n,$$

$$\hat{v}_3(t) := 2 \sum_{l=0}^{\min\{i, n-1-i\}} \hat{a}((i-l)\Delta_n) \hat{a}((i+l)\Delta_n) \Delta_n,$$

$$\hat{v}_4(t) := -2 \sum_{l=i}^{N_n-i} \hat{a}((l-i)\Delta_n) \hat{a}((i+l)\Delta_n) \Delta_n.$$

Value

The estimated asymptotic variance $\hat{v} = \hat{\sigma}_a^2(t)$ and its components $\hat{v}_1, \hat{v}_2, \hat{v}_3, \hat{v}_4$.

Examples

```
##Simulate a trawl process
##Determine the sampling grid
my_n <- 1000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(123)
#Simulate the trawl process
Poi_data <- sim_weighted_trawl(my_n, my_delta,
                              "Exp", my_lambda, "Poi", my_v)$path

#Estimate the trawl function
my_lag <- 100+1
trawl <- nonpar_trawlest(Poi_data, my_delta, lag=my_lag)$a_hat

#Estimate the fourth cumulant of the trawl process
c4_est <- c4est(Poi_data, my_delta)

asymptotic_variance_est(t=1, c4=c4_est, varlevyseed=1,
                        Delta=my_delta, avector=trawl)$v
```

c4est

Estimating the fourth cumulant of the trawl process

Description

This function estimates the fourth cumulant of the trawl process.

Usage

```
c4est(data, Delta)
```

Arguments

data The data set used to estimate the fourth cumulant
Delta The width Delta of the observation grid

Details

According to Sauri and Veraart (2022), estimator based on $X_0, X_{\Delta_n}, \dots, X_{(n-1)\Delta_n}$ is given by

$$\hat{c}_4(L') = RQ_n / \hat{a}(0),$$

where

$$RQ_n := \frac{1}{\sqrt{2n\Delta_n}} \sum_{k=0}^{n-2} (X_{(k+1)\Delta_n} - X_{k\Delta_n})^4,$$

and

$$\hat{a}(0) = \frac{1}{2\Delta_n n} \sum_{k=0}^{n-2} (X_{(k+1)\Delta_n} - X_{k\Delta_n})^2.$$

Value

The function returns the estimated fourth cumulant of the Levy seed: $\hat{c}_4(L')$.

Examples

```
##Simulate a trawl process
##Determine the sampling grid
my_n <- 1000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(123)
#Simulate the trawl process
Poi_data<-ambit::sim_weighted_trawl(my_n, my_delta, "Exp", my_lambda, "Poi", my_v)$path

#Estimate the fourth cumulant of the trawl process
c4est(Poi_data, my_delta)
```

discrete_fourier_sin_cos
discrete_fourier_sin_cos

Description

discrete_fourier_sin_cos

Usage

discrete_fourier_sin_cos(x, a, b, tau)

Arguments

x	argument for which the acf will be computed (this can be a vector)
a	vector of coefficients a ₀ ,...a _n
b	vector of coefficients b ₁ ,...b _n
tau	period of function

Details

Computes the Fourier approximation of a function using the sin-cos representation for given coefficients a₀,...a_n, b₁, ...b_n and rounds the values to a grid of width 1

Value

Fourier approximation or vector of Fourier approximations evaluated in x

fit_exp_periodic_trawl
Fits an exponential periodic trawl function to equidistant time series data

Description

Fits an exponential periodic trawl function to equidistant time series data

Usage

```
fit_exp_periodic_trawl(
  x,
  m = 1,
  tau,
  GMMlag = 50,
  Delta = 1,
  plotacf = FALSE,
  lags = 100
)
```

Arguments

x	vector of equidistant time series data
m	the order of the Fourier approximation of the periodic function
tau	the period, if not provided it will be estimated
GMMlag	lag length used in the GMM estimation, the default is 50
Delta	interval length of the time grid used in the time series, the default is 1
plotacf	binary variable specifying whether or not the empirical and fitted autocorrelation function should be plotted
lags	number of lags to be used in the plot of the autocorrelation function

Details

The trawl function is parametrised by the parameter $\lambda > 0$ as follows:

$$g(x) = e^{\lambda x}, \text{ for } x \leq 0.$$

The parameter τ is estimated using the smoothed periodogram, the parameter λ is estimated by GMM.

Value

lambda: the parameter λ in the exponential trawl, tau: the period τ , a: the vector of the Fourier coefficients, b: the vector of the Fourier coefficients.

fit_exp_sin_trawl	<i>Fits an exponential trawl function to equidistant time series data</i>
-------------------	---

Description

Fits an exponential trawl function to equidistant time series data

Usage

```
fit_exp_sin_trawl(x, GMMlag = 10, Delta = 1, plotacf = FALSE, lags = 100)
```

Arguments

x	vector of equidistant time series data
GMMlag	lag length used in the GMM estimation, the default is 10
Delta	interval length of the time grid used in the time series, the default is 1
plotacf	binary variable specifying whether or not the empirical and fitted autocorrelation function should be plotted
lags	number of lags to be used in the plot of the autocorrelation function

Details

The trawl function is parametrised by the parameter $\lambda > 0$ as follows:

$$g(x) = e^{\lambda x}, \text{ for } x \leq 0.$$

The Lebesgue measure of the corresponding trawl set is given by $1/\lambda$. Both parameters λ and τ are estimated by GMM.

Value

lambda: the memory parameter λ in the exponential trawl

fit_exp_sin_trawl_periodfixed

Fits an exponential trawl function to equidistant time series data

Description

Fits an exponential trawl function to equidistant time series data

Usage

```
fit_exp_sin_trawl_periodfixed(
  x,
  tau = 1,
  GMMlag,
  Delta = 1,
  plotacf = FALSE,
  lags = 100
)
```

Arguments

x	vector of equidistant time series data
tau	period in the sine function, the default is 1
GMMlag	lag length used in the GMM estimation, the default is tau
Delta	interval length of the time grid used in the time series, the default is 1
plotacf	binary variable specifying whether or not the empirical and fitted autocorrelation function should be plotted
lags	number of lags to be used in the plot of the autocorrelation function

Details

The trawl function is parametrised by the parameter $\lambda > 0$ as follows:

$$g(x) = e^{\lambda x}, \text{ for } x \leq 0.$$

The Lebesgue measure of the corresponding trawl set is given by $1/\lambda$.

Value

lambda: the memory parameter λ in the exponential trawl

fit_exp_sin_trawl_periodogram

Fits an exponential trawl function to equidistant time series data

Description

Fits an exponential trawl function to equidistant time series data

Usage

```
fit_exp_sin_trawl_periodogram(
  x,
  GMMlag = 10,
  Delta = 1,
  plotacf = FALSE,
  lags = 100
)
```

Arguments

x	vector of equidistant time series data
GMMlag	lag length used in the GMM estimation, the default is 10
Delta	interval length of the time grid used in the time series, the default is 1
plotacf	binary variable specifying whether or not the empirical and fitted autocorrelation function should be plotted
lags	number of lags to be used in the plot of the autocorrelation function

Details

The trawl function is parametrised by the parameter $\lambda > 0$ as follows:

$$g(x) = e^{\lambda x}, \text{ for } x \leq 0.$$

The Lebesgue measure of the corresponding trawl set is given by $1/\lambda$. The period parameter is estimated using the smoothed periodogram and the trawl parameter is estimated using GMM.

Value

lambda: the memory parameter λ in the exponential trawl

fit_LM_periodic_trawl *Fits a supGamma periodic trawl function to equidistant time series data*

Description

Fits a supGamma periodic trawl function to equidistant time series data

Usage

```
fit_LM_periodic_trawl(
  x,
  m = 1,
  tau,
  GMMlag = 50,
  Delta = 1,
  plotacf = FALSE,
  lags = 100
)
```

Arguments

x	vector of equidistant time series data
m	the order of the Fourier approximation of the periodic function
tau	the period, if not provided it will be estimated
GMMlag	lag length used in the GMM estimation, the default is 50
Delta	interval length of the time grid used in the time series, the default is 1
plotacf	binary variable specifying whether or not the empirical and fitted autocorrelation function should be plotted
lags	number of lags to be used in the plot of the autocorrelation function

Details

The trawl function is parametrised by the parameter $\lambda > 0$ as follows:

$$g(x) = (1 + x/\alpha)^H, \text{ for } x \leq 0.$$

The parameter τ is estimated using the smoothed periodogram, the other parameters are estimated by GMM.

Value

alpha: the parameter α in the supGamma trawl, H: the parameter H in the supGamma trawl, tau: the period τ , a: the vector of the Fourier coefficients, b: the vector of the Fourier coefficients.

fit_LM_sin_trawl	<i>Fits a LM periodic trawl function to equidistant time series data</i>
------------------	--

Description

Fits a LM periodic trawl function to equidistant time series data

Usage

```
fit_LM_sin_trawl(x, GMMlag = 10, Delta = 1, plotacf = FALSE, lags = 100)
```

Arguments

x	vector of equidistant time series data
GMMlag	lag length used in the GMM estimation, the default is 10
Delta	interval length of the time grid used in the time series, the default is 1
plotacf	binary variable specifying whether or not the empirical and fitted autocorrelation function should be plotted
lags	number of lags to be used in the plot of the autocorrelation function

Details

The trawl function is parametrised by the parameter $\lambda > 0$ as follows:

$$g(x) = e^{\lambda x}, \text{ for } x \leq 0.$$

The Lebesgue measure of the corresponding trawl set is given by $1/\lambda$. Both parameters λ and τ are estimated by GMM.

Value

lambda: the memory parameter λ in the exponential trawl

fourier_sin_cos *fourier_sin_cos*

Description

fourier_sin_cos

Usage

fourier_sin_cos(x, a, b, tau)

Arguments

x	argument for which the acf will be computed (this can be a vector)
a	vector of coefficients a ₀ ,...a _n
b	vector of coefficients b ₁ ,...b _n
tau	period of function

Details

Computes the Fourier approximation of a function using the sin-cos representation for given coefficients a₀,...a_n, b₁, ...b_n

Value

Fourier approximation or vector of Fourier approximations evaluated in x

kernel_generic_trawl_acf
kernel_generic_trawl_acf

Description

kernel_generic_trawl_acf

Usage

kernel_generic_trawl_acf(p, g, x)

Arguments

p	kernel function to be used in the weighted trawl process
g	trawl function
x	argument for which the acf will be computed (this can be a vector)

Details

We numerically approximate the acf for a given periodic function p and a given trawl function g

Value

acf or vector of acfs evaluated in x

Examples

```
my_p <- function(x){sin(x)}
my_g <- function(x){exp(-x)}
kernel_generic_trawl_acf(my_p, my_g, 1)

kernel_generic_trawl_acf(my_p, my_g, c(1,2,3,4))
```

kernel_generic_trawl_acf_incrtol
kernel_generic_trawl_acf_incrtol

Description

kernel_generic_trawl_acf_incrtol

Usage

```
kernel_generic_trawl_acf_incrtol(p, g, x)
```

Arguments

p	kernel function to be used in the weighted trawl process
g	trawl function
x	argument for which the acf will be computed (this can be a vector)

Details

We numerically approximate the acf for a given periodic function p and a given trawl function g . We allow for an increased tolerance level in the integral computations.

Value

acf or vector of acfs evaluated in x

`kernel_trawl_acf` *kernel_trawl_acf*

Description

`kernel_trawl_acf`

Usage

`kernel_trawl_acf(p, trawlfct, trawlfct_par, x)`

Arguments

<code>p</code>	kernel function to be used in the weighted trawl process
<code>trawlfct</code>	the trawl function used (Exp, supIG or LM)
<code>trawlfct_par</code>	parameter vector of trawl function
<code>x</code>	argument for which the acf will be computed (this can be a vector)

Details

We numerically approximate the acf for a given periodic function `p` and a given trawl function `g`

Value

acf or vector of acfs evaluated in `x`

`kernel_trawl_acf_exp_periodic`
kernel_trawl_acf_exp_periodic

Description

`kernel_trawl_acf_exp_periodic`

Usage

`kernel_trawl_acf_exp_periodic(x, lambda, a, b, tau)`

Arguments

<code>x</code>	argument for which the acf will be computed (this can be a vector)
<code>lambda</code>	parameter in the trawl function
<code>a</code>	vector of Fourier coefficients
<code>b</code>	vector of Fourier coefficients
<code>tau</code>	period in the sine function

Details

We compute the acf of a weighted trawl process with exponential trawl function and periodic function

Value

acf or vector of acfs evaluated in x

`kernel_trawl_acf_exp_sin`
kernel_trawl_acf_exp_sin

Description

`kernel_trawl_acf_exp_sin`

Usage

`kernel_trawl_acf_exp_sin(x, lambda, tau)`

Arguments

- `x` argument for which the acf will be computed (this can be a vector)
- `lambda` parameter in the exponential trawl function
- `tau` period in the sine function

Details

We compute the acf of a weighted trawl process with exponential trawl function and periodic function given by the sine function

Value

acf or vector of acfs evaluated in x

kernel_trawl_acf_LM_periodic
kernel_trawl_acf_LM_periodic

Description

kernel_trawl_acf_LM_periodic

Usage

kernel_trawl_acf_LM_periodic(x, alpha, H, a, b, tau)

Arguments

x	argument for which the acf will be computed (this can be a vector)
alpha	parameter in the trawl function
H	parameter in the trawl function
a	vector of Fourier coefficients
b	vector of Fourier coefficients
tau	period in the sine function

Details

We compute the acf of a weighted trawl process with supGamma trawl function and periodic function

Value

acf or vector of acfs evaluated in x

LebA_est *Nonparametric estimation of the trawl set Leb(A)*

Description

This function estimates the size of the trawl set given by Leb(A).

Usage

LebA_est(data, Delta, biascor = FALSE)

Arguments

data	Data to be used in the trawl function estimation.
Delta	Width of the grid on which we observe the data
biascor	A binary variable determining whether a bias correction should be computed, the default is FALSE

Details

Estimation of the trawl function using the methodology proposed in Sauri and Veraart (2022).

Value

The estimated Lebesgue measure of the trawl set

Examples

```
##Simulate a trawl process
##Determine the sampling grid
my_n <- 5000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(1726)
#Simulate the trawl process
Poi_data<-ambit::sim_weighted_trawl(my_n, my_delta, "Exp", my_lambda, "Poi", my_v)$path

#Estimate the trawl set without bias correction
LebA1 <-LebA_est(Poi_data, my_delta)
LebA1

#Estimate the trawl set with bias correction
LebA2 <-LebA_est(Poi_data, my_delta, biascor=TRUE)
LebA2

#Note that Leb(A)=1/my_lambda for an exponential trawl
```

LebA_slice_est	<i>Nonparametric estimation of the trawl (sub-) sets $Leb(A)$, $Leb(A \text{ intersection } A_h)$, $Leb(A \text{ setdifference } A_h)$</i>
----------------	---

Description

This function estimates $Leb(A)$, $Leb(A \text{ intersection } A_h)$, $Leb(A \setminus A_h)$.

Usage

```
LebA_slice_est(
  data,
  Delta,
  h,
  biascor = FALSE,
  adjust_neg = FALSE,
  adjust_variance = FALSE
)
```

Arguments

data	Data to be used in the trawl function estimation.
Delta	Width of the grid on which we observe the data
h	Time point used in $A \text{ intersection } A_h$ and the $A \text{ setdifference } A_h$
biascor	A binary variable determining whether a bias correction should be computed, the default is FALSE
adjust_neg	A binary variable determining whether negative estimates of the trawl function should be set to 0, the default is FALSE
adjust_variance	A binary variable determining whether a variance adjustment should be used, the default is FALSE

Details

Estimation of the trawl function using the methodology proposed in Sauri and Veraart (2022).

Value

LebA
 LebAintersection
 LebAsetdifference

Examples

```

##Simulate a trawl process
##Determine the sampling grid
my_n <- 5000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(1726)
#Simulate the trawl process
Poi_data<-ambit::sim_weighted_trawl(my_n, my_delta, "Exp", my_lambda, "Poi", my_v)$path

#Estimate the trawl set and its two slices at time h=2 without bias correction
est1 <- LebA_slice_est(Poi_data, my_delta, h=2)
est1$LebA
est1$LebAintersection
est1$LebAsetdifference

#Estimate the trawl set and its two slices at time h=2 without bias correction
est2 <- LebA_slice_est(Poi_data, my_delta, h=2, biascor=TRUE)
est2$LebA
est2$LebAintersection
est2$LebAsetdifference

#Note that Leb(A)=1/my_lambda for an exponential trawl

```

LebA_slice_est_approx *Nonparametric estimation of the trawl (sub-) sets Leb(A), Leb(A intersection A_h), Leb(A setdifference A_h)*

Description

This function estimates Leb(A), Leb(A intersection A_h), Leb(A \ A_h).

Usage

```
LebA_slice_est_approx(esttrawl, Delta, h, adjust_neg = FALSE)
```

Arguments

esttrawl	Vector containing estimated trawl function.
Delta	Width of the grid on which we observe the data

h	Time point used in A intersection A_h and the setdifference A setdifference A_h
adjust_neg	A binary variable determining whether negative estimates of the trawl function should be set to 0, the default is FALSE

Details

Estimation of the trawl function using the methodology proposed in Sauri and Veraart (2022).

Value

LebA
 LebAintersection
 LebAsetdifference

Examples

```
##Simulate a trawl process
##Determine the sampling grid
my_n <- 5000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(1726)
#Simulate the trawl process
Poi_data<-ambit::sim_weighted_trawl(my_n, my_delta, "Exp", my_lambda, "Poi", my_v)$path

#Estimate the trawl set and its two slices at time h=2 without bias correction
est1 <- LebA_slice_est(Poi_data, my_delta, h=2)
est1$LebA
est1$LebAintersection
est1$LebAsetdifference

#Estimate the trawl set and its two slices at time h=2 without bias correction
est2 <- LebA_slice_est(Poi_data, my_delta, h=2, biascor=TRUE)
est2$LebA
est2$LebAintersection
est2$LebAsetdifference

#Note that Leb(A)=1/my_lambda for an exponential trawl
```

 LebA_slice_ratio_est_acfbased

Nonparametric estimation of the ratios $Leb(A \cap A_h)/Leb(A)$, $Leb(A \setminus A_h)/Leb(A)$

Description

This function estimates the ratios $Leb(A \cap A_h)/Leb(A)$, $Leb(A \setminus A_h)/Leb(A)$.

Usage

```
LebA_slice_ratio_est_acfbased(data, Delta, h)
```

Arguments

data	Data to be used in the trawl function estimation.
Delta	Width of the grid on which we observe the data
h	Time point used in $A \cap A_h$ and the setdifference $A \setminus A_h$

Details

Estimation of the trawl function using the methodology proposed in Sauri and Veraart (2022) which is based on the empirical acf.

Value

LebAintersection_ratio: $LebA \cap A_h / LebA$
 LebAsetdifference_ratio: $LebA \setminus A_h / LebA$

Examples

```
##Simulate a trawl process
##Determine the sampling grid
my_n <- 5000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(1726)
#Simulate the trawl process
Poi_data<-ambit::sim_weighted_trawl(my_n, my_delta, "Exp", my_lambda, "Poi", my_v)$path
```

```
#Estimate the trawl set and its two slices at time h=0.5
est <- LebA_slice_ratio_est_acfbased(Poi_data, my_delta, h=0.5)
#Print the ratio LebAintersection/LebA
est$LebAintersection_ratio
#Print the ratio LebAsetdifference/LebA
est$LebAsetdifference_ratio
```

my_mae

my_mse

Description

Returns the mean absolute error between two vectors

Usage

```
my_mae(x, y)
```

Arguments

x	vector
y	vector

Value

Mean absolute error between the two vectors x and y

Examples

```
#Simulate two vectors of i.i.d.~standard normal data
set.seed(456)
x <- rnorm(100)
y <- rnorm(100)
#Compute the mean absolute error between both vectors
my_mae(x,y)
```

my_mse	<i>my_mse</i>
--------	---------------

Description

Returns the mean squared error between two vectors

Usage

```
my_mse(x, y)
```

Arguments

x	vector
y	vector

Value

Mean square error between the two vectors x and y

Examples

```
#Simulate two vectors of i.i.d.~standard normal data
set.seed(456)
x <- rnorm(100)
y <- rnorm(100)
#Compute the mean squared error between both vectors
my_mse(x,y)
```

my_results	<i>my_results</i>
------------	-------------------

Description

Returns summary statistics

Usage

```
my_results(x, sd = 1, digits = 3, reduced_percentiles = FALSE)
```

Arguments

x	Numeric vector of data values
sd	Optional parameter giving the standard deviation of the normal distribution used for computing the coverage probabilities. Default is 1.
digits	Optional parameter specifying to how many digits the results should be rounded. Default is 3.
reduced_percentiles	Optional logical parameter specifying whether only the upper three levels of 90. Default is FALSE.

Details

This function returns the sample mean, sample standard deviation and the coverage probabilities at levels 75 (or just 90 standard normal quantiles. Coverage probability is calculated as the proportion of $|x|$ values that fall within the specified quantile range.

Value

A numeric vector containing:

- Sample mean
- Sample standard deviation
- Coverage probabilities at the specified levels

When `reduced_percentiles=FALSE`: returns 8 values (mean, sd, 6 coverage levels) When `reduced_percentiles=TRUE`: returns 5 values (mean, sd, 3 coverage levels)

Examples

```
#Simulate i.i.d.~standard normal data
set.seed(456)
data <- rnorm(10000)
#Display the sample mean, standard deviation and coverage probabilities:
my_results(data)
```

nonpar_trawlest *Nonparametric estimation of the trawl function*

Description

This function implements the nonparametric trawl estimation proposed in Sauri and Veraart (2022).

Usage

```
nonpar_trawlest(data, Delta, lag = 100)
```

Arguments

data	Data to be used in the trawl function estimation.
Delta	Width of the grid on which we observe the data
lag	The lag until which the trawl function should be estimated

Details

Estimation of the trawl function using the methodology proposed in Sauri and Veraart (2022). Suppose the data is observed on the grid $0, \Delta, 2\Delta, \dots, (n-1)\Delta$. Given the path contained in data, the function returns the lag-dimensional vector

$$(\hat{a}(0), \hat{a}(\Delta), \dots, \hat{a}((lag - 1)\Delta)).$$

In the case when $lag=n$, the $n-1$ dimensional vector

$$(\hat{a}(0), \hat{a}(\Delta), \dots, \hat{a}((n - 2)\Delta))$$

is returned.

Value

ahat Returns the lag-dimensional vector $(\hat{a}(0), \hat{a}(\Delta), \dots, \hat{a}((lag - 1)\Delta))$. Here, $\hat{a}(0)$ is estimated based on the realised variance estimator.

a0_alt Returns the alternative estimator of $a(0)$ using the same methodology as the one used for $t>0$. Note that this is not the recommended estimator to use, but can be used for comparison purposes.

Examples

```
##Simulate a trawl process
##Determine the sampling grid
my_n <- 5000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(1726)
#Simulate the trawl process
Poi_data<-ambit::sim_weighted_trawl(my_n, my_delta, "Exp", my_lambda, "Poi", my_v)$path

#Estimate the trawl function
my_lag <- 100+1
PoiEx_trawl <- nonpar_trawlest(Poi_data, my_delta, lag=my_lag)$a_hat

#Plot the estimated trawl function and superimpose the true one
```

```

l_seq <- seq(from = 0, to = (my_lag-1), by = 1)
esttrawlfcct.data <- base::data.frame(l=l_seq[1:31],
                                     value=PoiEx_trawl[1:31])
p1 <- ggplot2::ggplot(esttrawlfcct.data, ggplot2::aes(x=l,y=value))+
  ggplot2::geom_point(size=3)+
  ggplot2::geom_function(fun = function(x) acf_Exp(x*my_delta,my_lambda), colour="red", size=1.5)+
  ggplot2::xlab("l")+
  ggplot2::ylab(latex2exp::TeX("$\\hat{a}(\\cdot)$ for Poisson trawl process"))
p1

```

rq

*Computing the scaled realised quarticity***Description**

This function computes the scaled realised quarticity of a time series for a given width of the observation grid.

Usage

```
rq(data, Delta)
```

Arguments

data	The data set used to compute the scaled realised quarticity
Delta	The width Delta of the observation grid

Details

According to Sauri and Veraart (2022), the scaled realised quarticity for $X_0, X_{\Delta_n}, \dots, X_{(n-1)\Delta_n}$ is given by

$$RQ_n := \frac{1}{\sqrt{2n\Delta_n}} \sum_{k=0}^{n-2} (X_{(k+1)\Delta_n} - X_{k\Delta_n})^4.$$

Value

The function returns the scaled realised quarticity RQ_n .

Examples

```

##Simulate a trawl process
##Determine the sampling grid
my_n <- 1000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter

```

```

#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(123)
#Simulate the trawl process
Poi_data<-ambit::sim_weighted_trawl(my_n, my_delta, "Exp", my_lambda, "Poi", my_v)$path

#Compute the scaled realised quarticity
rq(Poi_data, my_delta)

```

sim_weighted_trawl *Simulation of a weighted trawl process*

Description

This function simulates a weighted trawl process for various choices of the trawl function and the marginal distribution.

Usage

```

sim_weighted_trawl(
  n,
  Delta,
  trawlfct,
  trawlfct_par,
  distr,
  distr_par,
  kernelfct = NULL
)

```

Arguments

n	number of grid points to be simulated (excluding the starting value)
Delta	grid-width
trawlfct	the trawl function a used in the simulation (Exp, supIG or LM)
trawlfct_par	parameter vector of trawl function (Exp: lambda, supIG: delta, gamma, LM: alpha, H)
distr	marginal distribution. Choose from "Gamma" (Gamma), "Gauss" (Gaussian), "Cauchy" (Cauchy), "NIG" (Normal Inverse Gaussian), "Poi" (Poisson), "NegBin" (Negative Binomial)
distr_par	parameters of the marginal distribution: (Gamma: shape, scale; Gauss: mu, sigma (i.e. the second parameter is the standard deviation, not the variance); Cauchy: l, s; NIG: alpha, beta, delta, mu; Poi: v, NegBin: m, theta)
kernelfct	the kernel function p used in the ambit process

Details

This functions simulates a sample path from a weighted trawl process given by

$$Y_t = \int_{(-\infty, t] \times (-\infty, \infty)} p(t-s) I_{(0, a(t-s))}(x) L(dx, ds),$$

for $t \geq 0$, and returns $Y_0, Y_\Delta, \dots, Y_{n\Delta}$.

Value

path Simulated path
 slice_sizes slice sizes used
 S_matrix Matrix of all slices
 kernelweights kernel weights used

Examples

```
#Simulation of a Gaussian trawl process with exponential trawl function
n<-2000
Delta<-0.1
trawlfct="Exp"
trawlfct_par <-0.5
distr<-"Gauss"
distr_par<-c(0,1) #mean 0, std 1
set.seed(233)
path <- sim_weighted_trawl(n, Delta, trawlfct, trawlfct_par, distr, distr_par)$path
#Plot the path
library(ggplot2)
df <- data.frame(time = seq(0,n,1), value=path)
p <- ggplot(df, aes(x=time, y=path))+
  geom_line()+
  xlab("t")+
  ylab("Trawl process")
p
```

sim_weighted_trawl_gen

Simulation of a weighted trawl process with generic trawl function

Description

This function simulates a weighted trawl process for a generic trawl function and various choices the marginal distribution. The specific trawl function to be used can be supplied directly by the user.

Usage

```
sim_weighted_trawl_gen(
  n,
  Delta,
  trawlfct_gen,
  distr,
  distr_par,
  kernelfct = NULL
)
```

Arguments

n	number of grid points to be simulated (excluding the starting value)
Delta	grid-width
trawlfct_gen	the trawl function a used in the simulation
distr	marginal distribution. Choose from "Gamma" (Gamma), "Gauss" (Gaussian), "Cauchy" (Cauchy), "NIG" (Normal Inverse Gaussian), Poi" (Poisson), "NegBin" (Negative Binomial)
distr_par	parameters of the marginal distribution: (Gamma: shape, scale; Gauss: mu, sigma (i.e. the second parameter is the standard deviation, not the variance); Cauchy: l, s; NIG: alpha, beta, delta, mu; Poi: v, NegBin: m, theta)
kernelfct	the kernel function p used in the ambit process

Details

This functions simulates a sample path from a weighted trawl process given by

$$Y_t = \int_{(-\infty, t] \times (-\infty, \infty)} p(t-s) I_{(0, a(t-s))}(x) L(dx, ds),$$

for $t \geq 0$, and returns $Y_0, Y_\Delta, \dots, Y_{n\Delta}$. The user needs to ensure that trawlfct_gen is a monotonic function.

Value

path Simulated path
 slice_sizes slice sizes used
 S_matrix Matrix of all slices
 kernelweights kernel weights used

Examples

```
#Simulation of a Gaussian trawl process with exponential trawl function
n<-2000
Delta<-0.1

trawlfct_par <-0.5
```

```
distr<-"Gauss"
distr_par<-c(0,1) #mean 0, std 1
set.seed(233)

a <- function(x){exp(-trawlfct_par*x)}
path <- sim_weighted_trawl_gen(n, Delta, a,
                              distr, distr_par)$path

#Plot the path
library(ggplot2)
df <- data.frame(time = seq(0,n,1), value=path)
p <- ggplot(df, aes(x=time, y=path))+
  geom_line()+
  xlab("t")+
  ylab("Trawl process")
p
```

test_asymnorm	<i>Computing the infeasible test statistic from the trawl function estimation CLT</i>
---------------	---

Description

This function computes the infeasible test statistic appearing in the CLT for the trawl function estimation.

Usage

```
test_asymnorm(ahat, n, Delta, k, c4, varlevyseed = 1, trawlfct, trawlfct_par)
```

Arguments

ahat	The term $\hat{a}(k\Delta_n)$ in the CLT
n	The number n of observations in the sample
Delta	The width Delta of the observation grid
k	The time point in $0, 1, \dots, n - 1$; the test statistic will be computed for the time point $k * \Delta_n$.
c4	The fourth cumulant of the Levy seed of the trawl process
varlevyseed	The variance of the Levy seed of the trawl process, the default is 1
trawlfct	The trawl function for which the asymptotic variance will be computed (Exp, supIG or LM)
trawlfct_par	The parameter vector of the trawl function (Exp: lambda, supIG: delta, gamma, LM: alpha, H)

Details

As derived in Sauri and Veraart (2022), the infeasible test statistic is given by

$$\frac{\sqrt{n\Delta_n}}{\sqrt{\sigma_a^2(k\Delta_n)}} (\hat{a}(k\Delta_n) - a(k\Delta_n)),$$

for $k \in \{0, 1, \dots, n - 1\}$.

Value

The function returns the infeasible test statistic specified above.

Examples

```
test_asymnorm(ahat=0.9, n=5000, Delta=0.1, k=1, c4=1, varlevyseed=1,
             trawlfct="Exp", trawlfct_par=0.1)
```

test_asymnorm_est	<i>Computing the feasible statistic of the trawl function CLT</i>
-------------------	---

Description

This function computes the feasible statistics associated with the CLT for the trawl function estimation.

Usage

```
test_asymnorm_est(
  data,
  Delta,
  trawlfct,
  trawlfct_par,
  biascor = FALSE,
  k = NULL
)
```

Arguments

data	The data set based on observations of $X_0, X_{\Delta_n}, \dots, X_{(n-1)\Delta_n}$
Delta	The width Delta of the observation grid
trawlfct	The trawl function for which the asymptotic variance will be computed (Exp, supIG or LM)
trawlfct_par	The parameter vector of the trawl function (Exp: lambda, supIG: delta, gamma, LM: alpha, H)
biascor	A binary variable determining whether a bias correction should be computed, the default is FALSE
k	The optional parameter specifying the time point in $0, 1, \dots, n - 1$; the test statistic will be computed for the time point $k\Delta_n$.

Details

As derived in Sauri and Veraart (2022), the feasible statistic, for $t > 0$, is given by

$$T(t)_n := \frac{\sqrt{n\Delta_n}}{\sqrt{\widehat{\sigma_a^2(t)}}} (\hat{a}(t) - a(t) - bias(t)).$$

For $t = 0$, we have

$$T(t)_n := \frac{\sqrt{n\Delta_n}}{\sqrt{RQ_n}} (\hat{a}(0) - a(0) - bias(0)),$$

where

$$RQ_n := \frac{1}{\sqrt{2n\Delta_n}} \sum_{k=0}^{n-2} (X_{(k+1)\Delta_n} - X_{k\Delta_n})^4.$$

We set $bias(t) = 0$ in the case when `biascor==FALSE` and $bias(t) = 0.5 * \Delta * \hat{a}'(t)$ otherwise.

Value

The function returns the vector of the feasible statistics $(T(0)_n, T((\Delta)_n), \dots, T((n-2)\Delta_n))$ if no bias correction is required and $(T(0)_n, T((\Delta)_n), \dots, T((n-3)\Delta_n))$ if bias correction is required if `k` is not provided, otherwise it returns the value $T(k\Delta_n)_n$. If the estimated asymptotic variance is ≤ 0 , the value of the test statistic is set to 999.

Examples

```
##Simulate a trawl process
##Determine the sampling grid
my_n <- 1000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(123)
#Simulate the trawl process
Poi_data <- sim_weighted_trawl(my_n, my_delta,
                              "Exp", my_lambda, "Poi", my_v)$path

#Compute the test statistic for time t=0
##Either one can use:
test_asymnorm_est(Poi_data, my_delta,
                  trawlfct="Exp", trawlfct_par=my_lambda)[1]
#or:
test_asymnorm_est(Poi_data, my_delta,
                  trawlfct="Exp", trawlfct_par=my_lambda, k=0)
```

test_asymnorm_est_dev *Computing the feasible statistic of the trawl function CLT*

Description

This function computes the feasible test statistic appearing in the CLT for the trawl function estimation.

Usage

```
test_asymnorm_est_dev(
  ahat,
  n,
  Delta,
  k,
  c4,
  varlevyseed = 1,
  trawlfct,
  trawlfct_par,
  avector
)
```

Arguments

ahat	The estimated trawl function at time t : $\hat{a}(t)$
n	The number of observations in the data set
Delta	The width Δ of the observation grid
k	The time point in $0, 1, \dots, n - 1$; the test statistic will be computed for the time point $k * \Delta_n$.
c4	The fourth cumulant of the Levy seed of the trawl process
varlevyseed	The variance of the Levy seed of the trawl process, the default is 1
trawlfct	The trawl function for which the asymptotic variance will be computed (Exp, supIG or LM)
trawlfct_par	The parameter vector of the trawl function (Exp: lambda, supIG: delta, gamma, LM: alpha, H)
avector	The vector $(\hat{a}(0), \hat{a}(\Delta_n), \dots, \hat{a}((n - 1)\Delta_n))$

Details

As derived in Sauri and Veraart (2022), the feasible statistic is given by

$$T(k\Delta_n)_n := \frac{\sqrt{n\Delta_n}}{\sqrt{\widehat{\sigma_a^2(\Delta_n)}}} (\hat{a}(\Delta_n) - a(\Delta_n))$$

Value

The function returns the feasible statistic $T(\Delta_n)_n$ if the estimated asymptotic variance is positive and 999 otherwise.

trawl_deriv	<i>Estimating the derivative of the trawl function using the empirical derivative</i>
-------------	---

Description

This function estimates the derivative of the trawl function using the empirical derivative of the trawl function.

Usage

```
trawl_deriv(data, Delta, lag = 100)
```

Arguments

data	Numeric vector of data used to compute the derivative of the trawl function
Delta	Numeric value specifying the width Delta of the observation grid
lag	Integer specifying the lag until which the trawl function derivative should be estimated. Default is 100.

Details

This function first estimates the trawl function $\hat{a}(t)$ using [nonpar_trawlest](#), then computes the derivative using finite differences:

$$\hat{a}'(l\Delta_n) = \frac{\hat{a}((l+1)\Delta_n) - \hat{a}(l\Delta_n)}{\Delta_n},$$

for $l = 0, 1, \dots, lag - 1$.

Value

Numeric vector of length lag containing the estimated derivative values $(\hat{a}'(0), \hat{a}'(\Delta), \dots, \hat{a}'((lag-1)\Delta))$.

See Also

[nonpar_trawlest](#) for the underlying trawl function estimation

Examples

```

##Simulate a trawl process
##Determine the sampling grid
my_n <- 1000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(123)
#Simulate the trawl process
Poi_data <- sim_weighted_trawl(my_n, my_delta,
                              "Exp", my_lambda, "Poi", my_v)$path

#Estimate the trawl function
my_lag <- 100+1
trawl <- nonpar_trawlest(Poi_data, my_delta, lag=my_lag)$a_hat

#Estimate the derivative of the trawl function
trawl_deriv <- trawl_deriv(Poi_data, my_delta, lag=100)

```

trawl_deriv_mod

Estimating the derivative of the trawl function

Description

This function estimates the derivative of the trawl function using the modified version proposed in Sauri and Veraart (2022).

Usage

```
trawl_deriv_mod(data, Delta, lag = 100)
```

Arguments

data	Numeric vector of data used to compute the derivative of the trawl function
Delta	Numeric value specifying the width Delta of the observation grid
lag	Integer specifying the lag until which the trawl function derivative should be estimated. Default is 100.

Details

According to Sauri and Veraart (2022), the derivative of the trawl function can be estimated based on observations $X_0, X_{\Delta_n}, \dots, X_{(n-1)\Delta_n}$ by

$$\hat{a}'(t) = \frac{1}{n\Delta_n^2} \sum_{k=l+1}^{n-2} (X_{(k+1)\Delta_n} - X_{k\Delta_n})(X_{(k-l)\Delta_n} - X_{(k-l-1)\Delta_n}),$$

for $\Delta_n l \leq t < (l+1)\Delta_n$.

Value

The function returns the lag-dimensional vector $(\hat{a}'(0), \hat{a}'(\Delta), \dots, \hat{a}'((lag-1)\Delta))$.

Examples

```
##Simulate a trawl process
##Determine the sampling grid
my_n <- 1000
my_delta <- 0.1
my_t <- my_n*my_delta

###Choose the model parameter
#Exponential trawl function:
my_lambda <- 2
#Poisson marginal distribution trawl
my_v <- 1

#Set the seed
set.seed(123)
#Simulate the trawl process
Poi_data <- sim_weighted_trawl(my_n, my_delta,
                             "Exp", my_lambda, "Poi", my_v)$path

#Estimate the trawl function
my_lag <- 100+1
trawl <- nonpar_trawlest(Poi_data, my_delta, lag=my_lag)$a_hat

#Estimate the derivative of the trawl function
trawl_deriv <- trawl_deriv_mod(Poi_data, my_delta, lag=100)
```

trawl_est

Bias-corrected nonparametric estimation of the trawl function

Description

This function implements bias correction for the nonparametric trawl estimation proposed in Sauri and Veraart (2022).

Usage

```
trawl_est(data, Delta)
```

Arguments

data	Data to be used in the trawl function estimation.
Delta	Width of the grid on which we observe the data

Details

This function performs bias correction on the nonparametric trawl function estimates obtained using the methodology of Sauri and Veraart (2022). The bias correction is implemented by estimating the derivative of the trawl function and applying the correction $0.5 \times \Delta \times \hat{a}'(t)$, where $\hat{a}'(t)$ is the estimated derivative at lag t .

Suppose the data is observed on the grid $0, \Delta, 2\Delta, \dots, (n-1)\Delta$. Given the path contained in data, the function returns both the original and bias-corrected estimates of the trawl function.

The bias correction is based on the theoretical result that the leading bias term in nonparametric trawl function estimation is proportional to Δ times the derivative of the true trawl function.

Value

trawlfct Returns the original nonparametric trawl function estimate obtained from [nonpar_trawlest](#).

trawlfct_biascor Returns the bias-corrected trawl function estimate, computed as the original estimate minus the bias correction term $0.5 \times \Delta \times \hat{a}'(t)$.

See Also

[nonpar_trawlest](#), [trawl_deriv_mod](#)

Examples

```
#Simulation of a Gaussian trawl process with exponential trawl function
n<-2000
Delta<-0.5

trawlfct_par <-0.5
distr<-"Gauss"
distr_par<-c(0,1) #mean 0, std 1
set.seed(233)

a <- function(x){exp(-trawlfct_par*x)}
path <- sim_weighted_trawl_gen(n, Delta, a,
                             distr, distr_par)$path

#Plot the path
library(ggplot2)
df <- data.frame(time = seq(0,n,1), value=path)
p <- ggplot(df, aes(x=time, y=path))+
  geom_line()+
  xlab("1")+
```

```

      ylab("Trawl process")
    p

result <- trawl_est(path, Delta)

original_estimate <- result$trawlfct[1:30]
bias_corrected <- result$trawlfct_biascor[1:30]

# True exponential values for the same lags
lags <- 0:(length(original_estimate)-1)
true_vals <- a(lags * Delta)

# Plot all three
plot(lags, original_estimate,
     type = "l", col = "blue", lwd = 2,
     xlab = "Lag index", ylab = "Trawl function estimate",
     main = "Trawl function: Original vs bias-corrected vs true",
     ylim = range(c(original_estimate, bias_corrected, true_vals), na.rm = TRUE))
lines(lags, bias_corrected,
      col = "red", lwd = 2, lty = 2)
lines(lags, true_vals,
      col = "black", lwd = 2, lty = 3)

legend("topright",
      legend = c("Original", "Bias-corrected", "True exponential"),
      col = c("blue", "red", "black"),
      lty = c(1, 2, 3), lwd = 2)

```

trawl_Exp

Evaluates the exponential trawl function

Description

Evaluates the exponential trawl function

Usage

```
trawl_Exp(x, lambda)
```

Arguments

x	the argument at which the exponential trawl function will be evaluated
lambda	the parameter λ in the exponential trawl

Details

The trawl function is parametrised by parameter $\lambda > 0$ as follows:

$$g(x) = e^{\lambda x}, \text{ for } x \leq 0.$$

Value

The exponential trawl function evaluated at x

Examples

```
trawl_Exp(-1, 0.5)
```

trawl_LM

Evaluates the long memory trawl function

Description

Evaluates the long memory trawl function

Usage

```
trawl_LM(x, alpha, H)
```

Arguments

x	the argument at which the supOU/long memory trawl function will be evaluated
alpha	the parameter α in the long memory trawl
H	the parameter H in the long memory trawl

Details

The trawl function is parametrised by the two parameters $H > 1$ and $\alpha > 0$ as follows:

$$g(x) = (1 - x/\alpha)^{-H}, \text{ for } x \leq 0.$$

If $H \in (1, 2]$, then the resulting trawl process has long memory, for $H > 2$, it has short memory.

Value

the long memory trawl function evaluated at x

Examples

```
trawl_LM(-1, 0.5, 1.5)
```

trawl_supIG	<i>Evaluates the supIG trawl function</i>
-------------	---

Description

Evaluates the supIG trawl function

Usage

```
trawl_supIG(x, delta, gamma)
```

Arguments

x	the argument at which the supIG trawl function will be evaluated
delta	the parameter δ in the supIG trawl
gamma	the parameter γ in the supIG trawl

Details

The trawl function is parametrised by the two parameters $\delta \geq 0$ and $\gamma \geq 0$ as follows:

$$gd(x) = (1 - 2x\gamma^{-2})^{-1/2} \exp(\delta\gamma(1 - (1 - 2x\gamma^{-2})^{1/2})), \text{ for } x \leq 0.$$

It is assumed that δ and γ are not simultaneously equal to zero.

Value

The supIG trawl function evaluated at x

Examples

```
trawl_supIG(-1, 0.5, 0.2)
```

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