

# Package ‘bate’

May 7, 2026

**Title** Computes Bias-Adjusted Treatment Effect

**Version** 0.1.0

**Description** Compute bounds for the treatment effect after adjusting for the presence of omitted variables in linear econometric models, according to the method of Basu (2022) <doi:10.48550/arXiv.2203.12431>. You supply the data, identify the outcome and treatment variables and additional regressors. The main functions will compute bounds for the bias-adjusted treatment effect. Many plot functions allow easy visualization of results.

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**VignetteBuilder** knitr

**URL** <https://github.com/dbasu-umass/bate/>,  
<https://rpubs.com/dbasu/bate/>

**NeedsCompilation** no

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collect_par	<i>Collect parameters from the short, intermediate and auxiliary regressions</i>
-------------	--

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## Description

Collect parameters from the short, intermediate and auxiliary regressions

## Usage

```
collect_par(data, outcome, treatment, control, other_regressors = NULL)
```

## Arguments

data	A data frame.
outcome	The name of the outcome variable (must be present in the data frame).
treatment	The name of the treatment variable (must be present in the data frame).
control	Control variables to be added to the intermediate regression.
other_regressors	Subset of control variables to be added in the short regression (default is NULL).

**Value**

A data frame with the following columns:

beta0	Treatment effect in the short regression
R0	R-squared in the short regression
betatilde	Treatment effect in the intermediate regression
Rtilde	R-squared in the intermediate regression
sigmay	Standard deviation of outcome variable
sigmax	Standard deviation of treatment variable
taux	Standard deviation of residual in auxiliary regression

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Collect parameters from the short, intermediate and auxiliary regressions
parameters <- collect_par(
  data = NLSY_IQ, outcome = "iq_std",
  treatment = "BF_months",
  control = c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
  other_regressors = c("sex", "age"))

## See results
(parameters)
```

---

cplotbias

*Create contour plot of bias*

---

**Description**

Create contour plot of bias

**Usage**

```
cplotbias(data)
```

**Arguments**

data            A data frame that is the output from the "ovbias" function.

**Value**

A plot object created with ggplot

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Collect parameters from the short, intermediate and auxiliary regressions
parameters <- collect_par(
  data = NLSY_IQ, outcome = "iq_std",
  treatment = "BF_months",
  control = c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
  other_regressors = c("sex", "age"))

## Set limits for the bounded box
Rlow <- parameters$Rtilde
Rhigh <- 0.61
deltalow <- 0.01
deltahigh <- 0.99
e <- 0.01

## Not run:
## Compute bias and bias-adjusted treatment effect
OVB <- ovbias(
  parameters = parameters,
  deltalow=deltalow,
  deltahigh=deltahigh, Rhigh=Rhigh,
  e=e)

## Contour Plot of bias over the bounded box
p2 <- cplotbias(OVB$Data)
print(p2)

## End(Not run)
```

---

delfplot

*Plot graph of function  $\delta=f(R_{max})$* 


---

**Description**

Plot graph of function  $\delta=f(R_{max})$

**Usage**

```
delfplot(parameters)
```

**Arguments**

parameters      A vector of parameters that is generated after estimating the short, intermediate and auxiliary regressions.

**Value**

A plot object created with ggplot

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Collect parameters from the short, intermediate and auxiliary regressions
parameters <- collect_par(
  data = NLSY_IQ, outcome = "iq_std",
  treatment = "BF_months",
  control = c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
  other_regressors = c("sex", "age"))

## Set limits for the bounded box
Rlow <- parameters$Rtilde
Rhigh <- 0.61
deltalow <- 0.01
deltahigh <- 0.99
e <- 0.01

## Oster's method: Plot of delta = f(Rmax)
p4 <- delfplot(parameters = parameters)
print(p4)
```

---

dplotbate

*Histogram of bias adjusted treatment effect*

---

**Description**

Histogram of bias adjusted treatment effect

**Usage**

```
dplotbate(data)
```

**Arguments**

`data`                    A data frame that is the output from the "ovbias" function.

**Value**

A plot object created with ggplot

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Collect parameters from the short, intermediate and auxiliary regressions
parameters <- collect_par(
  data = NLSY_IQ, outcome = "iq_std",
  treatment = "BF_months",
  control = c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
  other_regressors = c("sex", "age"))

## Set limits for the bounded box
Rlow <- parameters$Rtilde
Rhigh <- 0.61
deltalow <- 0.01
deltahigh <- 0.99
e <- 0.01

## Not run:
## Compute bias and bias-adjusted treatment effect
OVB <- ovbias(
  parameters = parameters,
  deltalow=deltalow,
  deltahigh=deltahigh, Rhigh=Rhigh,
  e=e)

## Histogram and density Plot of bstar distribution
p3 <- dplotbate(OVB$Data)
print(p3)

## End(Not run)
```

**Description**

Extend border of bounded box by +/- e

**Usage**

expand\_border(parameters, deltalow, deltahigh, Rlow, Rhigh, e)

**Arguments**

- parameters      A vector of parameters (real numbers) that is generated by estimating the short, intermediate and auxiliary regressions.
- deltalow        The lower limit of delta.
- deltahigh       The upper limit of delta.
- Rlow            The lower limit of Rmax.
- Rhigh           The upper limit of Rmax.
- e                The step size.

**Value**

Data frame.

---

get_border	<i>Identify all border points in a region</i>
------------	---

---

**Description**

Identify all border points in a region

**Usage**

get\_border(region, e)

**Arguments**

- region          A data frame containing the x and y coordinates of the region.
- e                The step size of the grid in the x and y directions.

**Value**

A data frame containing the x and y coordinates of the border points of the region.

---

`mycubic`*Compute roots of the cubic equation*

---

**Description**

Compute roots of the cubic equation

**Usage**

```
mycubic(parameters, mydelta, Rmax)
```

**Arguments**

<code>parameters</code>	A vector of parameters (real numbers) that is generated by estimating the short, intermediate and auxiliary regressions.
<code>mydelta</code>	Value of delta (real number).
<code>Rmax</code>	Value of Rmax (real number).

**Value**

A vector containing the three roots of the cubic equation defined by the parameters, delta and Rmax.

---

`mydisc`*Evaluates discriminant of the cubic equation*

---

**Description**

Evaluates discriminant of the cubic equation

**Usage**

```
mydisc(parameters, mydelta, Rmax)
```

**Arguments**

<code>parameters</code>	A vector of parameters (real numbers) that is generated by estimating the short, intermediate and auxiliary regressions.
<code>mydelta</code>	The value of delta (real number).
<code>Rmax</code>	The value of Rmax (real number)

**Value**

Returns a value of 0 or 1; 0 (if discriminant is positive) and 1 (if discriminant is nonpositive)

---

NLSY\_BW

*NLSY Birth Weight.*

---

### Description

NLSY data to analyse the effect of maternal behaviour on children's birth weight. Natality detail files are from 2001 and 2002. Data is from the NLSY Children and Young Adults panel.

### Usage

NLSY\_BW

### Format

A data frame with 7686 observations on 13 variables:

birth\_wt birth weight, grams

BF\_months months of breast feeding

mom\_drink\_preg\_all did the mother drink at all during pregnancy

lbw\_preterm low birth weight + preterm

age age of child

female child female

black mother black

motherAge age of mother

motherEDU years of schooling of mother

mom\_married is the mother married?

income annual income of mother

sex years of schooling of mother

race race of mother

gesweek gestation week

any\_smoke did the mother smoke at all during pregnancy

Source: <https://drive.google.com/file/d/101W9dP8F3B1DnAZGBegpoqCfysUrn7Uc/view?usp=sharing>

### Examples

```
## Load data set
data("NLSY_BW")
## See names of variables
names(NLSY_BW)
```

---

NLSY\_IQ

*NLSY IQ.*

---

### Description

NLSY data to analyse the effect of maternal behaviour on children's IQ score. Natality detail files are from 2001 and 2002. Data is from the NLSY Children and Young Adults panel.

### Usage

NLSY\_IQ

### Format

A data frame with 6514 observations on 13 variables:

iq\_std standardized IQ score, PIAT score

BF\_months months of breast feeding

mom\_drink\_preg\_all did mother drink at all during pregnancy

lbw\_preterm low birth weight + preterm

age age of child

female child female

black mother black

motherAge age of mother

motherEDU years of schooling of mother

mom\_married is the mother married?

income annual income of mother

sex child sex

race race of mother

Source: <https://drive.google.com/file/d/101W9dP8F3B1DnAZGBegpoqCfysUrn7Uc/view?usp=sharing>

### Examples

```
## Load data set
data("NLSY_IQ")
## See names of variables
names(NLSY_IQ)
```

---

osterbds	<i>Computes identified set according to Oster (2019)</i>
----------	--

---

**Description**

Computes identified set according to Oster (2019)

**Usage**

```
osterbds(parameters, Rmax)
```

**Arguments**

parameters	A vector of parameters that is generated after estimating the short, intermediate and auxiliary regressions.
Rmax	A real number which lies between $R_{\text{tilde}}$ (R-squared for the intermediate regression) and 1.

**Value**

A data frame with three columns:

Discriminant	The value of the discriminant of the quadratic equation that is solved to generate the identified set
Interval1	The interval formed with the first root of the quadratic equation
Interval2	The interval formed with the first root of the quadratic equation

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Collect parameters from the short, intermediate and auxiliary regressions
parameters <- collect_par(
  data = NLSY_IQ, outcome = "iq_std",
  treatment = "BF_months",
  control = c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
  other_regressors = c("sex", "age"))

## Oster's method: bounding sets when Rmax=0.61
osterbds(parameters = parameters, Rmax=0.61)
```

---

osterdelstar	<i>Computes delta* according to Oster (2019)</i>
--------------	--

---

**Description**

Computes delta\* according to Oster (2019)

**Usage**

```
osterdelstar(parameters, Rmax)
```

**Arguments**

parameters	A vector of parameters that is generated after estimating the short, intermediate and auxiliary regressions.
Rmax	A real number that lies between Rtilde (R-squared for the intermediate regression) and 1.

**Value**

A data frame with three columns:

delstar	The value of delta for the chosen value of Rmax
discontinuity	Indicates whether the point of discontinuity is within the interval formed by Rtilde and 1
slope	Slope of the function, $\text{delta} = f(\text{Rmax})$

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Collect parameters from the short, intermediate and auxiliary regressions
parameters <- collect_par(
  data = NLSY_IQ, outcome = "iq_std",
  treatment = "BF_months",
  control = c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
  other_regressors = c("sex", "age"))

## Oster's method: delta* (for Rmax=0.61)
osterdelstar(parameters = parameters, Rmax=0.61)
```

---

ovbias	<i>Compute bias adjusted treatment effect taking parameter vector as input.</i>
--------	---

---

**Description**

Compute bias adjusted treatment effect taking parameter vector as input.

**Usage**

```
ovbias(parameters, deltalow, deltahigh, Rhigh, e)
```

**Arguments**

parameters	A vector of parameters (real numbers) that is generated by estimating the short, intermediate and auxiliary regressions.
deltalow	The lower limit of delta.
deltahigh	The upper limit of delta.
Rhigh	The upper limit of Rmax.
e	The step size.

**Value**

List with three elements:

Data	Data frame containing the bias ( $\$bias$ ) and bias-adjusted treatment effect ( $\$bstar$ ) for each point on the grid
bias_Distribution	Quantiles (2.5,5.0,50,95,97.5) of the empirical distribution of bias
bstar_Distribution	Quantiles (2.5,5.0,50,95,97.5) of the empirical distribution of the bias-adjusted treatment effect

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Collect parameters from the short, intermediate and auxiliary regressions
parameters <- collect_par(
  data = NLSY_IQ, outcome = "iq_std",
  treatment = "BF_months",
  control = c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
```

```

other_regressors = c("sex","age"))

## Set limits for the bounded box
Rlow <- parameters$Rtilde
Rhigh <- 0.61
deltalow <- 0.01
deltahigh <- 0.99
e <- 0.01

## Not run:
## Compute bias and bias-adjusted treatment effect
OVB <- ovbias(
  parameters = parameters,
  deltalow=deltalow,
  deltahigh=deltahigh, Rhigh=Rhigh,
  e=e)

## Default quantiles of bias
(OVB$bias_Distribution)

## Chosen quantiles of bias
quantile(OVB$Data$bias, c(0.01,0.05,0.1,0.9,0.95,0.975))

## Default quantiles of bias-adjusted treatment effect
(OVB$bstar_Distribution)

## Chosen quantiles of bias-adjusted treatment effect
quantile(OVB$Data$bstar, c(0.01,0.05,0.1,0.9,0.95,0.975))

## End(Not run)

```

---

ovbias_lm	<i>Compute bias adjusted treatment effect taking three lm objects as input.</i>
-----------	---

---

### Description

Compute bias adjusted treatment effect taking three lm objects as input.

### Usage

```
ovbias_lm(lm_shrt, lm_int, lm_aux, deltalow, deltahigh, Rhigh, e)
```

### Arguments

lm_shrt	lm object corresponding to the short regression
lm_int	lm object corresponding to the intermediate regression
lm_aux	lm object corresponding to the auxiliary regression

deltalow	The lower limit of delta
deltahigh	The upper limit of delta
Rhigh	The upper limit of Rmax
e	The step size

### Value

List with three elements:

Data	Data frame containing the bias and bias-adjusted treatment effect for each point on the grid
bias_Distribution	Quantiles (2.5,5.0,50,95,97.5) of the empirical distribution of bias
bstar_Distribution	Quantiles (2.5,5.0,50,95,97.5) of the empirical distribution of the bias-adjusted treatment effect

### Examples

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Short regression
reg_s <- lm(iq_std ~ BF_months + factor(age) + sex, data = NLSY_IQ)

## Intermediate regression
reg_i <- lm(iq_std ~ BF_months +
  factor(age) + sex + income + motherAge +
  motherEDU + mom_married + factor(race),
  data = NLSY_IQ)

## Auxiliary regression
reg_a <- lm(BF_months ~ factor(age) +
  sex + income + motherAge + motherEDU +
  mom_married + factor(race), data = NLSY_IQ)

## Set limits for the bounded box
Rlow <- summary(reg_i)$r.squared
Rhigh <- 0.61
deltalow <- 0.01
deltahigh <- 0.99
e <- 0.01

## Not run:
## Compute bias and bias-adjusted treatment effect
ovb_lm <- ovbias_lm(lm_shrt = reg_s, lm_int = reg_i,
```

```
lm_aux = reg_a, deltalow=deltalow, deltahigh=deltahigh,
Rhigh=Rhigh, e=e)

## Default quantiles of bias
ovb_lm$bias_Distribution

# Default quantiles of bias-adjusted treatment effect
ovb_lm$bstar_Distribution

## End(Not run)
```

---

ovbias\_par

---

*Compute bias adjusted treatment effect taking data frame as input.*


---

### Description

Compute bias adjusted treatment effect taking data frame as input.

### Usage

```
ovbias_par(
  data,
  outcome,
  treatment,
  control,
  other_regressors = NULL,
  deltalow,
  deltahigh,
  Rhigh,
  e
)
```

### Arguments

data	Data frame.
outcome	Outcome variable.
treatment	Treatment variable.
control	Control variables to add in the intermediate regression.
other_regressors	Subset of control variables to add in the short regression (default is NULL).
deltalow	The lower limit of delta.
deltahigh	The upper limit of delta.
Rhigh	The upper limit of Rmax.
e	The step size.

**Value**

List with three elements:

Data	Data frame containing the bias and bias-adjusted treatment effect for each point on the grid
bias_Distribution	Quantiles (2.5,5.0,50,95,97.5) of the empirical distribution of bias
bstar_Distribution	Quantiles (2.5,5.0,50,95,97.5) of the empirical distribution of the bias-adjusted treatment effect

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set parameters for bounded box
Rhigh <- 0.61
deltalow <- 0.01
deltahigh <- 0.99
e <- 0.01

## Not run:
## Compute bias and bias-adjusted treatment effect
OVB_par <- ovbias_par(data=NLSY_IQ,
  outcome="iq_std", treatment="BF_months",
  control=c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
  other_regressors = c("sex", "age"), deltalow=deltalow,
  deltahigh=deltahigh, Rhigh=Rhigh, e=e)

## Default quantiles of bias
OVB_par$bias_Distribution

# Default quantiles of bias-adjusted treatment effect
OVB_par$bstar_Distribution

## End(Not run)
```

---

partocoef

*Returns coefficients of the cubic equation*

---

**Description**

Returns coefficients of the cubic equation

**Usage**

```
partocoef(parameters, mydelta, Rmax)
```

**Arguments**

parameters	A vector of parameters (real numbers) that is generated by estimating the short, intermediate and auxiliary regressions.
mydelta	The value of delta (real number)
Rmax	The value of Rmax (real number)

**Value**

A data frame with the coefficients of the cubic equation.

---

selectroot	<i>Select root of the cubic based on the root of a nearest point</i>
------------	--

---

**Description**

Select root of the cubic based on the root of a nearest point

**Usage**

```
selectroot(parameters, mydelta, Rmax, closest_bias)
```

**Arguments**

parameters	A vector of parameters (real numbers) that is generated by estimating the short, intermediate and auxiliary regressions.
mydelta	The value of delta (real number).
Rmax	The value of Rmax (real number).
closest_bias	The value of bias at the nearest point.

**Value**

Data frame

---

split_nurr	<i>Split a region into two parts</i>
------------	--------------------------------------

---

**Description**

Split a region into two parts

**Usage**

```
split_nurr(region1, region2, epsilon, parameters, e)
```

**Arguments**

region1	Data frame with coordinates for region 1
region2	Data frame with coordinates for region 2
epsilon	Closest distance
parameters	A vector of parameters (real numbers) that is generated by estimating the short, intermediate and auxiliary regressions.
e	The step size of the grid in the x and y directions.

**Value**

List, where first element is region within epsilon distance of region 1 and second element which is region which is not within epsilon distance of region 1.

---

urrplot	<i>Region plot to demarcate URR and NURR for the bounded box</i>
---------	--

---

**Description**

Region plot to demarcate URR and NURR for the bounded box

**Usage**

```
urrplot(parameters, deltalow, deltahigh, Rlow, Rhigh, e)
```

**Arguments**

parameters	A vector of parameters (real numbers) that is generated by estimating the short, intermediate and auxiliary regressions.
deltalow	The lower limit for delta.
deltahigh	The upper limit for delta.
Rlow	The lower limit for Rmax.
Rhigh	The upper limit for Rmax.
e	The step size of the grid in the x and y directions.

**Value**

A plot object created by ggplot

**Examples**

```
## Load data set
data("NLSY_IQ")

## Set age and race as factor variables
NLSY_IQ$age <- factor(NLSY_IQ$age)
NLSY_IQ$race <- factor(NLSY_IQ$race)

## Collect parameters from the short, intermediate and auxiliary regressions
parameters <- collect_par(
  data = NLSY_IQ, outcome = "iq_std",
  treatment = "BF_months",
  control = c("age", "sex", "income", "motherAge", "motherEDU", "mom_married", "race"),
  other_regressors = c("sex", "age"))

## Set limits for the bounded box
Rlow <- parameters$Rtilde
Rhigh <- 0.61
deltalow <- 0.01
deltahigh <- 0.99
e <- 0.01

## Create region plot for bounded box
p1 <- urrplot(parameters, deltalow, deltahigh, Rlow, Rhigh, e=e)

## See plot
print(p1)
```

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