Package 'bst'

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Type Package

Title Gradient Boosting

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Description Functional gradient descent algorithm for a variety of convex and non-convex loss functions, for both classical and robust regression and classification problems. See Wang (2011) <doi:10.2202/1557-4679.1304>, Wang (2012) <doi:10.3414/ME11-02-0020>, Wang (2018) <doi:10.1080/10618600.2018.1424635>, Wang (2018) <doi:10.1214/18-EJS1404>.

Imports rpart, methods, foreach, doParallel, gbm

Suggests hdi, pROC, R.rsp, knitr, gdata

VignetteBuilder R.rsp, knitr

License GPL (>= 2)

LazyLoad yes

NeedsCompilation no

Repository CRAN

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Contents

`bst` *Boosting for Classification and Regression*

Description

Gradient boosting for optimizing loss functions with componentwise linear, smoothing splines, tree models as base learners.

Usage

```
bst(x, y, cost = 0.5, family = c("gaussian", "hinge", "hinge2", "binom", "expo",
"poisson", "tgaussianDC", "thingeDC", "tbinomDC", "binomdDC", "texpoDC", "tpoissonDC",
 "huber", "thuberDC", "clossR", "clossRMM", "closs", "gloss", "qloss", "clossMM",
"glossMM", "qlossMM", "lar"), ctrl = bst_control(), control.tree = list(maxdepth = 1),
learner = c("ls", "sm", "tree"))
## S3 method for class 'bst'
print(x, ...)
## S3 method for class 'bst'
predict(object, newdata=NULL, newy=NULL, mstop=NULL,
type=c("response", "all.res", "class", "loss", "error"), ...)
## S3 method for class 'bst'
plot(x, type = c("step", "norm"),...)
## S3 method for class 'bst'
coef(object, which=object$ctrl$mstop, ...)
## S3 method for class 'bst'
fpartial(object, mstop=NULL, newdata=NULL)
```

Arguments

`x`	a data frame containing the variables in the model.
`y`	vector of responses. `y` must be in {1, -1} for `family` = "hinge".
`cost`	price to pay for false positive, 0 < `cost` < 1; price of false negative is 1-`cost`.

family	A variety of loss functions. family = "hinge" for hinge loss and family="gaussian" for squared error loss. Implementing the negative gradient corresponding to the loss function to be minimized. For hinge loss, +1/-1 binary responses is used.
ctrl	an object of class bst_control.
type	type of prediction or plot, see predict, plot
control.tree	control parameters of rpart.
learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
object	class of bst.
newdata	new data for prediction with the same number of columns as x.
newy	new response.
mstop	boosting iteration for prediction.
which	at which boosting mstop to extract coefficients.
...	additional arguments.

Details

Boosting algorithms for classification and regression problems. In a classification problem, suppose f is a classifier for a response y. A cost-sensitive or weighted loss function is

$$L(y, f, cost) = l(y, f, cost) \max(0, (1 - yf))$$

For family="hinge",

$$l(y, f, cost) = 1 - cost, if\ y = +1; \quad cost, if\ y = -1$$

For family="hinge2", l(y,f,cost)= 1, if y = +1 and f > 0 ; = 1-cost, if y = +1 and f < 0; = cost, if y = -1 and f > 0; = 1, if y = -1 and f < 0.

For twin boosting if twinboost=TRUE, there are two types of adaptive boosting if learner="ls": for twintype=1, weights are based on coefficients in the first round of boosting; for twintype=2, weights are based on predictions in the first round of boosting. See Buehlmann and Hothorn (2010).

Value

An object of class bst with print, coef, plot and predict methods are available for linear models. For nonlinear models, methods print and predict are available.

x, y, cost, family, learner, control.tree, maxdepth	These are input variables and parameters
ctrl	the input ctrl with possible updated fk if family="thingeDC", "tbinomDC", "binomdDC"
yhat	predicted function estimates
ens	a list of length mstop. Each element is a fitted model to the pseudo residuals, defined as negative gradient of loss function at the current estimated function
ml.fit	the last element of ens
ensemble	a vector of length mstop. Each element is the variable selected in each boosting step when applicable
xselect	selected variables in mstop
coef	estimated coefficients in each iteration. Used internally only

Author(s)

Zhu Wang

References

Zhu Wang (2011), HingeBoost: ROC-Based Boost for Classification and Variable Selection. *The International Journal of Biostatistics*, **7**(1), Article 13.

Peter Buehlmann and Torsten Hothorn (2010), Twin Boosting: improved feature selection and prediction, *Statistics and Computing*, **20**, 119-138.

See Also

`cv.bst` for cross-validated stopping iteration. Furthermore see `bst_control`

Examples

```
x <- matrix(rnorm(100*5),ncol=5)
c <- 2*x[,1]
p <- exp(c)/(exp(c)+exp(-c))
y <- rbinom(100,1,p)
y[y != 1] <- -1
x <- as.data.frame(x)
dat.m <- bst(x, y, ctrl = bst_control(mstop=50), family = "hinge", learner = "ls")
predict(dat.m)
dat.m1 <- bst(x, y, ctrl = bst_control(twinboost=TRUE,
coefir=coef(dat.m), xselect.init = dat.m$xselect, mstop=50))
dat.m2 <- rbst(x, y, ctrl = bst_control(mstop=50, s=0, trace=TRUE),
rfamily = "thinge", learner = "ls")
predict(dat.m2)
```

---

bst.sel *Function to select number of predictors*

Description

Function to determine the first q predictors in the boosting path, or perform (10-fold) cross-validation and determine the optimal set of parameters

Usage

```
bst.sel(x, y, q, type=c("firstq", "cv"), ...)
```

Arguments

x	Design matrix (without intercept).
y	Continuous response vector for linear regression
q	Maximum number of predictors that should be selected if `type="firstq"`.

type	if type="firstq", return the first q predictors in the boosting path. if type="cv", perform (10-fold) cross-validation and determine the optimal set of parameters
...	Further arguments to be passed to bst, cv.bst.

Details

Function to determine the first q predictors in the boosting path, or perform (10-fold) cross-validation and determine the optimal set of parameters. This may be used for p-value calculation. See below.

Value

Vector of selected predictors.

Author(s)

Zhu Wang

Examples

```
## Not run:
x <- matrix(rnorm(100*100), nrow = 100, ncol = 100)
y <- x[,1] * 2 + x[,2] * 2.5 + rnorm(100)
sel <- bst.sel(x, y, q=10)
library("hdi")
fit.multi <- hdi(x, y, method = "multi.split",
model.selector =bst.sel,
args.model.selector=list(type="firstq", q=10))
fit.multi
fit.multi$pval[1:10] ## the first 10 p-values
fit.multi <- hdi(x, y, method = "multi.split",
model.selector =bst.sel,
args.model.selector=list(type="cv"))
fit.multi
fit.multi$pval[1:10] ## the first 10 p-values

## End(Not run)
```

---

bst_control *Control Parameters for Boosting*

Description

Specification of the number of boosting iterations, step size and other parameters for boosting algorithms.

Usage

```
bst_control(mstop = 50, nu = 0.1, twinboost = FALSE, twintype=1, threshold=c("standard",
"adaptive"), f.init = NULL, coefir = NULL, xselect.init = NULL, center = FALSE,
trace = FALSE, numsample = 50, df = 4, s = NULL, sh = NULL, q = NULL, qh = NULL,
fk = NULL, start=FALSE, iter = 10, intercept = FALSE, trun=FALSE)
```

Arguments

mstop	an integer giving the number of boosting iterations.
nu	a small number (between 0 and 1) defining the step size or shrinkage parameter.
twinboost	a logical value: TRUE for twin boosting.
twintype	for twinboost=TRUE only. For learner="ls", if twintype=1, twin boosting with weights from magnitude of coefficients in the first round of boosting. If twintype=2, weights are correlations between predicted values in the first round of boosting and current predicted values. For learners not componentwise least squares, twintype=2.
threshold	if threshold="adaptive", the estimated function ctrl$fk is updated in every boosting step. Otherwise, no update for ctrl$fk in boosting steps. Only used in robust nonconvex loss function.
f.init	the estimate from the first round of twin boosting. Only useful when twinboost=TRUE and learner="sm" or "tree".
coefir	the estimated coefficients from the first round of twin boosting. Only useful when twinboost=TRUE and learner="ls".
xselect.init	the variable selected from the first round of twin boosting. Only useful when twinboost=TRUE.
center	a logical value: TRUE to center covariates with mean.
trace	a logical value for printout of more details of information during the fitting process.
numsample	number of random sample variable selected in the first round of twin boosting. This is potentially useful in the future implementation.
df	degree of freedom used in smoothing splines.
s, q	nonconvex loss tuning parameter s or frequency q of outliers for robust regression and classification. If s is missing but q is available, s may be computed as the 1-q quantile of robust loss values using conventional software.
sh, qh	threshold value or frequency qh of outliers for Huber regression family="huber" or family="rhuberDC". For family="huber", if sh is not provided, sh is then updated adaptively with the median of y-yhat where yhat is the estimated y in the last boosting iteration. For family="rhuberDC", if sh is missing but qh is available, sh may be computed as the 1-qh quantile of robust loss values using conventional software.
fk	predicted values at an iteration in the MM algorithm
start	a logical value, if start=TRUE and fk is a vector of values, then bst iterations begin with fk. Otherwise, bst iterations begin with the default values. This can be useful, for instance, in rbst for the MM boosting algorithm.
iter	number of iteration in the MM algorithm
intercept	logical value, if TRUE, estimation of intercept with linear predictor model
trun	logical value, if TRUE, predicted value in each boosting iteration is truncated at -1, 1, for family="closs" in bst and rfamily="closs" in rbst

Details

Objects to specify parameters of the boosting algorithms implemented in bst, via the ctrl argument. The s value is for robust nonconvex loss where smaller s value is more robust to outliers with family="closs", "tbinom", "thinge", "tbinomd", and larger s value more robust with family="clossR", "gloss", "qloss".

For family="closs", if s=2, the loss is similar to the square loss; if s=1, the loss function is an approximation of the hinge loss; for smaller values, the loss function approaches the 0-1 loss function if s<1, the loss function is a nonconvex function of the margin.

The default value of s is -1 if family="thinge", -log(3) if family="tbinom", and 4 if family="binomd". If trun=TRUE, boosting classifiers can produce real values in [-1, 1] indicating their confidence in [-1, 1]-valued classification. cf. R. E. Schapire and Y. Singer. Improved boosting algorithms using confidence-rated predictions. In Proceedings of the Eleventh Annual Conference on Computational Learning Theory, pages 80-91, 1998.

Value

An object of class bst_control, a list. Note fk may be updated for robust boosting.

See Also

bst

---

cv.bst *Cross-Validation for Boosting*

Description

Cross-validated estimation of the empirical risk/error for boosting parameter selection.

Usage

```
cv.bst(x,y,K=10,cost=0.5,family=c("gaussian", "hinge", "hinge2", "binom", "expo",
"poisson", "tgaussianDC", "thingeDC", "tbinomDC", "binomdDC", "texpoDC", "tpoissonDC",
"clossR", "closs", "gloss", "qloss", "lar"), learner = c("ls", "sm", "tree"),
ctrl = bst_control(), type = c("loss", "error"),
plot.it = TRUE, main = NULL, se = TRUE, n.cores=2, ...)
```

Arguments

x	a data frame containing the variables in the model.
y	vector of responses. y must be in {1, -1} for binary classifications.
K	K-fold cross-validation
cost	price to pay for false positive, 0 < cost < 1; price of false negative is 1-cost.
family	family = "hinge" for hinge loss and family="gaussian" for squared error loss.

learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
ctrl	an object of class bst_control.
type	cross-validation criteria. For type="loss", loss function values and type="error" is misclassification error.
plot.it	a logical value, to plot the estimated loss or error with cross validation if TRUE.
main	title of plot
se	a logical value, to plot with standard errors.
n.cores	The number of CPU cores to use. The cross-validation loop will attempt to send different CV folds off to different cores.
...	additional arguments.

Value

object with

residmat	empirical risks in each cross-validation at boosting iterations
mstop	boosting iteration steps at which CV curve should be computed.
cv	The CV curve at each value of mstop
cv.error	The standard error of the CV curve
family	loss function types

...

See Also

bst

Examples

```
## Not run:
x <- matrix(rnorm(100*5),ncol=5)
c <- 2*x[,1]
p <- exp(c)/(exp(c)+exp(-c))
y <- rbinom(100,1,p)
y[y != 1] <- -1
x <- as.data.frame(x)
cv.bst(x, y, ctrl = bst_control(mstop=50), family = "hinge", learner = "ls", type="loss")
cv.bst(x, y, ctrl = bst_control(mstop=50), family = "hinge", learner = "ls", type="error")
dat.m <- bst(x, y, ctrl = bst_control(mstop=50), family = "hinge", learner = "ls")
dat.m1 <- cv.bst(x, y, ctrl = bst_control(twinboost=TRUE, coefir=coef(dat.m),
xselect.init = dat.m$xselect, mstop=50), family = "hinge", learner="ls")

## End(Not run)
```

cv.mada *Cross-Validation for one-vs-all AdaBoost with multi-class problem*

Description

Cross-validated estimation of the empirical misclassification error for boosting parameter selection.

Usage

```
cv.mada(x, y, balance=FALSE, K=10, nu=0.1, mstop=200, interaction.depth=1,
trace=FALSE, plot.it = TRUE, se = TRUE, ...)
```

Arguments

x	a data matrix containing the variables in the model.
y	vector of multi class responses. y must be an integer vector from 1 to C for C class problem.
balance	logical value. If TRUE, The K parts were roughly balanced, ensuring that the classes were distributed proportionally among each of the K parts.
K	K-fold cross-validation
nu	a small number (between 0 and 1) defining the step size or shrinkage parameter.
mstop	number of boosting iteration.
interaction.depth	used in gbm to specify the depth of trees.
trace	if TRUE, iteration results printed out.
plot.it	a logical value, to plot the cross-validation error if TRUE.
se	a logical value, to plot with 1 standard deviation curves.
...	additional arguments.

Value

object with

residmat	empirical risks in each cross-validation at boosting iterations
fraction	abscissa values at which CV curve should be computed.
cv	The CV curve at each value of fraction
cv.error	The standard error of the CV curve

...

See Also

mada

`cv.mbst` *Cross-Validation for Multi-class Boosting*

Description

Cross-validated estimation of the empirical multi-class loss for boosting parameter selection.

Usage

```
cv.mbst(x, y, balance=FALSE, K = 10, cost = NULL,
family = c("hinge","hinge2","thingeDC", "closs", "clossMM"),
learner = c("tree", "ls", "sm"), ctrl = bst_control(),
type = c("loss","error"), plot.it = TRUE, se = TRUE, n.cores=2, ...)
```

Arguments

`x`	a data frame containing the variables in the model.
`y`	vector of responses. `y` must be integers from 1 to C for C class problem.
`balance`	logical value. If TRUE, The K parts were roughly balanced, ensuring that the classes were distributed proportionally among each of the K parts.
`K`	K-fold cross-validation
`cost`	price to pay for false positive, 0 < `cost` < 1; price of false negative is 1-`cost`.
`family`	`family` = "hinge" for hinge loss. "hinge2" is a different hinge loss
`learner`	a character specifying the component-wise base learner to be used: `ls` linear models, `sm` smoothing splines, `tree` regression trees.
`ctrl`	an object of class `bst_control`.
`type`	for `family="hinge"`, `type="loss"` is hinge risk. For `family="thingeDC"`, `type="loss"`
`plot.it`	a logical value, to plot the estimated risks if `TRUE`.
`se`	a logical value, to plot with standard errors.
`n.cores`	The number of CPU cores to use. The cross-validation loop will attempt to send different CV folds off to different cores.
`...`	additional arguments.

Value

object with

`residmat`	empirical risks in each cross-validation at boosting iterations
`fraction`	abscissa values at which CV curve should be computed.
`cv`	The CV curve at each value of fraction
`cv.error`	The standard error of the CV curve

...

See Also

mbst

---

cv.mhingebst *Cross-Validation for Multi-class Hinge Boosting*

Description

Cross-validated estimation of the empirical multi-class hinge loss for boosting parameter selection.

Usage

```
cv.mhingebst(x, y, balance=FALSE, K = 10, cost = NULL, family = "hinge",
learner = c("tree", "ls", "sm"), ctrl = bst_control(),
type = c("loss","error"), plot.it = TRUE, main = NULL, se = TRUE, n.cores=2, ...)
```

Arguments

x	a data frame containing the variables in the model.
y	vector of responses. y must be integers from 1 to C for C class problem.
balance	logical value. If TRUE, The K parts were roughly balanced, ensuring that the classes were distributed proportionally among each of the K parts.
K	K-fold cross-validation
cost	price to pay for false positive, 0 < cost < 1; price of false negative is 1-cost.
family	family = "hinge" for hinge loss.

Implementing the negative gradient corresponding to the loss function to be minimized.

learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
ctrl	an object of class bst_control.
type	for family="hinge", type="loss" is hinge risk.
plot.it	a logical value, to plot the estimated loss or error with cross validation if TRUE.
main	title of plot
se	a logical value, to plot with standard errors.
n.cores	The number of CPU cores to use. The cross-validation loop will attempt to send different CV folds off to different cores.
...	additional arguments.

Value

object with

residmat	empirical risks in each cross-validation at boosting iterations
fraction	abscissa values at which CV curve should be computed.
cv	The CV curve at each value of fraction
cv.error	The standard error of the CV curve

...

See Also

mhingebst

---

cv.mhingeova *Cross-Validation for one-vs-all HingeBoost with multi-class problem*

Description

Cross-validated estimation of the empirical misclassification error for boosting parameter selection.

Usage

```
cv.mhingeova(x, y, balance=FALSE, K=10, cost = NULL, nu=0.1,
learner=c("tree", "ls", "sm"), maxdepth=1, m1=200, twinboost = FALSE,
m2=200, trace=FALSE, plot.it = TRUE, se = TRUE, ...)
```

Arguments

x	a data frame containing the variables in the model.
y	vector of multi class responses. y must be an integer vector from 1 to C for C class problem.
balance	logical value. If TRUE, The K parts were roughly balanced, ensuring that the classes were distributed proportionally among each of the K parts.
K	K-fold cross-validation
cost	price to pay for false positive, 0 < cost < 1; price of false negative is 1-cost.
nu	a small number (between 0 and 1) defining the step size or shrinkage parameter.
learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
maxdepth	tree depth used in learner=tree
m1	number of boosting iteration
twinboost	logical: twin boosting?
m2	number of twin boosting iteration

trace	if TRUE, iteration results printed out
plot.it	a logical value, to plot the estimated risks if TRUE.
se	a logical value, to plot with standard errors.
...	additional arguments.

Value

object with

residmat	empirical risks in each cross-validation at boosting iterations
fraction	abscissa values at which CV curve should be computed.
cv	The CV curve at each value of fraction
cv.error	The standard error of the CV curve

...

Note

The functions for balanced cross validation were from R package pmar.

See Also

mhingeova

---

cv.rbst *Cross-Validation for Nonconvex Loss Boosting*

Description

Cross-validated estimation of the empirical risk/error, can be used for tuning parameter selection.

Usage

```
cv.rbst(x, y, K = 10, cost = 0.5, rfamily = c("tgaussian", "thuber", "thinge",
"tbinom", "binomd", "texpo", "tpoisson", "clossR", "closs", "gloss", "qloss"),
learner = c("ls", "sm", "tree"), ctrl = bst_control(), type = c("loss", "error"),
plot.it = TRUE, main = NULL, se = TRUE, n.cores=2,...)
```

Arguments

x	a data frame containing the variables in the model.
y	vector of responses. y must be in {1, -1} for binary classification
K	K-fold cross-validation
cost	price to pay for false positive, 0 < cost < 1; price of false negative is 1-cost.
rfamily	nonconvex loss function types.

learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
ctrl	an object of class bst_control.
type	cross-validation criteria. For type="loss", loss function values and type="error" is misclassification error.
plot.it	a logical value, to plot the estimated loss or error with cross validation if TRUE.
main	title of plot
se	a logical value, to plot with standard errors.
n.cores	The number of CPU cores to use. The cross-validation loop will attempt to send different CV folds off to different cores.
...	additional arguments.

Value

object with

residmat	empirical risks in each cross-validation at boosting iterations
mstop	boosting iteration steps at which CV curve should be computed.
cv	The CV curve at each value of mstop
cv.error	The standard error of the CV curve
rfamily	nonconvex loss function types.

...

Author(s)

Zhu Wang

See Also

rbst

Examples

```
## Not run:
x <- matrix(rnorm(100*5),ncol=5)
c <- 2*x[,1]
p <- exp(c)/(exp(c)+exp(-c))
y <- rbinom(100,1,p)
y[y != 1] <- -1
x <- as.data.frame(x)
cv.rbst(x, y, ctrl = bst_control(mstop=50), rfamily = "thinge", learner = "ls", type="lose")
cv.rbst(x, y, ctrl = bst_control(mstop=50), rfamily = "thinge", learner = "ls", type="error")
dat.m <- rbst(x, y, ctrl = bst_control(mstop=50), rfamily = "thinge", learner = "ls")
dat.m1 <- cv.rbst(x, y, ctrl = bst_control(twinboost=TRUE, coefir=coef(dat.m),
xselect.init = dat.m$xselect, mstop=50), family = "thinge", learner="ls")

## End(Not run)
```

cv.rmbst *Cross-Validation for Nonconvex Multi-class Loss Boosting*

Description

Cross-validated estimation of the empirical multi-class loss, can be used for tuning parameter selection.

Usage

```
cv.rmbst(x, y, balance=FALSE, K = 10, cost = NULL, rfamily = c("thinge", "closs"),
learner = c("tree", "ls", "sm"), ctrl = bst_control(), type = c("loss","error"),
plot.it = TRUE, main = NULL, se = TRUE, n.cores=2, ...)
```

Arguments

x	a data frame containing the variables in the model.
y	vector of responses. y must be integers from 1 to C for C class problem.
balance	logical value. If TRUE, The K parts were roughly balanced, ensuring that the classes were distributed proportionally among each of the K parts.
K	K-fold cross-validation
cost	price to pay for false positive, 0 < cost < 1; price of false negative is 1-cost.
rfamily	rfamily = "thinge" for truncated multi-class hinge loss.

Implementing the negative gradient corresponding to the loss function to be minimized.

learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
ctrl	an object of class bst_control.
type	loss value or misclassification error.
plot.it	a logical value, to plot the estimated loss or error with cross validation if TRUE.
main	title of plot
se	a logical value, to plot with standard errors.
n.cores	The number of CPU cores to use. The cross-validation loop will attempt to send different CV folds off to different cores.
...	additional arguments.

Value

object with

residmat	empirical risks in each cross-validation at boosting iterations
fraction	abscissa values at which CV curve should be computed.
cv	The CV curve at each value of fraction
cv.error	The standard error of the CV curve

...

Author(s)

Zhu Wang

See Also

rmbst

---

ex1data *Generating Three-class Data with 50 Predictors*

Description

Randomly generate data for a three-class model.

Usage

```
ex1data(n.data, p=50)
```

Arguments

n.data	number of data samples.
p	number of predictors.

Details

The data is generated based on Example 1 described in Wang (2012).

Value

A list with n.data by p predictor matrix x, three-class response y and conditional probabilities.

Author(s)

Zhu Wang

References

Zhu Wang (2012), Multi-class HingeBoost: Method and Application to the Classification of Cancer Types Using Gene Expression Data. *Methods of Information in Medicine*, **51**(2), 162–7.

Examples

```
## Not run:
dat <- ex1data(100, p=5)
mhingebst(x=dat$x, y=dat$y)

## End(Not run)
```

loss *Internal Function*

Description

Internal Function

mada *Multi-class AdaBoost*

Description

One-vs-all multi-class AdaBoost

Usage

```
mada(xtr, ytr, xte=NULL, yte=NULL, mstop=50, nu=0.1, interaction.depth=1)
```

Arguments

`xtr`	training data matrix containing the predictor variables in the model.
`ytr`	training vector of responses. `ytr` must be integers from 1 to C, for C class problem.
`xte`	test data matrix containing the predictor variables in the model.
`yte`	test vector of responses. `yte` must be integers from 1 to C, for C class problem.
`mstop`	number of boosting iteration.
`nu`	a small number (between 0 and 1) defining the step size or shrinkage parameter.
`interaction.depth`	used in gbm to specify the depth of trees.

Details

For a C-class problem (C > 2), each class is separately compared against all other classes with AdaBoost, and C functions are estimated to represent confidence for each class. The classification rule is to assign the class with the largest estimate.

Value

A list contains variable selected `xselect` and training and testing error `err.tr`, `err.te`.

Author(s)

Zhu Wang

See Also

cv.mada for cross-validated stopping iteration.

Examples

```
data(iris)
mada(xtr=iris[,-5], ytr=iris[,5])
```

---

mbst *Boosting for Multi-Classification*

Description

Gradient boosting for optimizing multi-class loss functions with componentwise linear, smoothing splines, tree models as base learners.

Usage

```
mbst(x, y, cost = NULL, family = c("hinge", "hinge2", "thingeDC", "closs", "clossMM"),
ctrl = bst_control(), control.tree=list(fixed.depth=TRUE,
n.term.node=6, maxdepth = 1), learner = c("ls", "sm", "tree"))
## S3 method for class 'mbst'
print(x, ...)
## S3 method for class 'mbst'
predict(object, newdata=NULL, newy=NULL, mstop=NULL,
type=c("response", "class", "loss", "error"), ...)
## S3 method for class 'mbst'
fpartial(object, mstop=NULL, newdata=NULL)
```

Arguments

x	a data frame containing the variables in the model.
y	vector of responses. y must be 1, 2, ..., k for a k classification problem
cost	price to pay for false positive, 0 < cost < 1; price of false negative is 1-cost.
family	family = "hinge" for hinge loss, family="hinge2" for hinge loss but the response is not recoded (see details). family="thingeDC" for DCB loss function, see rmbst.
ctrl	an object of class bst_control.
control.tree	control parameters of rpart.
learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
type	in predict a character indicating whether the response, all responses across the boosting iterations, classes, loss or classification errors should be predicted in case of hinge problems. in plot, plot of boosting iteration or L_1 norm.

object	class of mbst.
newdata	new data for prediction with the same number of columns as x.
newy	new response.
mstop	boosting iteration for prediction.
...	additional arguments.

Details

A linear or nonlinear classifier is fitted using a boosting algorithm for multi-class responses. This function is different from mhingebst on how to deal with zero-to-sum constraint and loss functions. If family="hinge", the loss function is the same as in mhingebst but the boosting algorithm is different. If family="hinge2", the loss function is different from family="hinge": the response is not recoded as in Wang (2012). In this case, the loss function is

$$\sum I(y_i \neq j)(f_j + 1)_+.$$

family="thingeDC" for robust loss function used in the DCB algorithm.

Value

An object of class mbst with print, coef, plot and predict methods are available for linear models. For nonlinear models, methods print and predict are available.

x, y, cost, family, learner, control.tree, maxdepth	These are input variables and parameters
ctrl	the input ctrl with possible updated fk if family="thingeDC"
yhat	predicted function estimates
ens	a list of length mstop. Each element is a fitted model to the pseudo residuals, defined as negative gradient of loss function at the current estimated function
ml.fit	the last element of ens
ensemble	a vector of length mstop. Each element is the variable selected in each boosting step when applicable
xselect	selected variables in mstop
coef	estimated coefficients in each iteration. Used internally only

Author(s)

Zhu Wang

References

Zhu Wang (2011), HingeBoost: ROC-Based Boost for Classification and Variable Selection. *The International Journal of Biostatistics*, **7**(1), Article 13.

Zhu Wang (2012), Multi-class HingeBoost: Method and Application to the Classification of Cancer Types Using Gene Expression Data. *Methods of Information in Medicine*, **51**(2), 162–7.

See Also

cv.mbst for cross-validated stopping iteration. Furthermore see bst_control

Examples

```
x <- matrix(rnorm(100*5),ncol=5)
c <- quantile(x[,1], prob=c(0.33, 0.67))
y <- rep(1, 100)
y[x[,1] > c[1] & x[,1] < c[2] ] <- 2
y[x[,1] > c[2]] <- 3
x <- as.data.frame(x)
dat.m <- mbst(x, y, ctrl = bst_control(mstop=50), family = "hinge", learner = "ls")
predict(dat.m)
dat.m1 <- mbst(x, y, ctrl = bst_control(twinboost=TRUE,
f.init=predict(dat.m), xselect.init = dat.m$xselect, mstop=50))
dat.m2 <- rmbst(x, y, ctrl = bst_control(mstop=50, s=1, trace=TRUE),
rfamily = "thinge", learner = "ls")
predict(dat.m2)
```

---

mhingebst *Boosting for Multi-class Classification*

Description

Gradient boosting for optimizing multi-class hinge loss functions with componentwise linear least squares, smoothing splines and trees as base learners.

Usage

```
mhingebst(x, y, cost = NULL, family = c("hinge"), ctrl = bst_control(),
control.tree = list(fixed.depth=TRUE, n.term.node=6, maxdepth = 1),
learner = c("ls", "sm", "tree"))
## S3 method for class 'mhingebst'
print(x, ...)
## S3 method for class 'mhingebst'
predict(object, newdata=NULL, newy=NULL, mstop=NULL,
type=c("response", "class", "loss", "error"), ...)
## S3 method for class 'mhingebst'
fpartial(object, mstop=NULL, newdata=NULL)
```

Arguments

x	a data frame containing the variables in the model.
y	vector of responses. y must be in {1, -1} for family = "hinge".
cost	equal costs for now and unequal costs will be implemented in the future.
family	family = "hinge" for multi-class hinge loss.
ctrl	an object of class bst_control.

control.tree	control parameters of rpart.
learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
type	in predict a character indicating whether the response, classes, loss or classification errors should be predicted in case of hinge
object	class of mhingebst.
newdata	new data for prediction with the same number of columns as x.
newy	new response.
mstop	boosting iteration for prediction.
...	additional arguments.

Details

A linear or nonlinear classifier is fitted using a boosting algorithm based on component-wise base learners for multi-class responses.

Value

An object of class mhingebst with print and predict methods being available for fitted models.

Author(s)

Zhu Wang

References

Zhu Wang (2011), HingeBoost: ROC-Based Boost for Classification and Variable Selection. *The International Journal of Biostatistics*, **7**(1), Article 13.

Zhu Wang (2012), Multi-class HingeBoost: Method and Application to the Classification of Cancer Types Using Gene Expression Data. *Methods of Information in Medicine*, **51**(2), 162–7.

See Also

cv.mhingebst for cross-validated stopping iteration. Furthermore see bst_control

Examples

```
## Not run:
dat <- ex1data(100, p=5)
res <- mhingebst(x=dat$x, y=dat$y)

## End(Not run)
```

`mhingeova` *Multi-class HingeBoost*

Description

Multi-class algorithm with one-vs-all binary HingeBoost which optimizes the hinge loss functions with componentwise linear, smoothing splines, tree models as base learners.

Usage

```
mhingeova(xtr, ytr, xte=NULL, yte=NULL, cost = NULL, nu=0.1,
learner=c("tree", "ls", "sm"), maxdepth=1, m1=200, twinboost = FALSE, m2=200)
## S3 method for class 'mhingeova'
print(x, ...)
```

Arguments

`xtr`	training data containing the predictor variables.
`ytr`	vector of training data responses. `ytr` must be in {1,2,...,k}.
`xte`	test data containing the predictor variables.
`yte`	vector of test data responses. `yte` must be in {1,2,...,k}.
`cost`	default is NULL for equal cost; otherwise a numeric vector indicating price to pay for false positive, 0 < `cost` < 1; price of false negative is 1-`cost`.
`nu`	a small number (between 0 and 1) defining the step size or shrinkage parameter.
`learner`	a character specifying the component-wise base learner to be used: `ls` linear models, `sm` smoothing splines, `tree` regression trees.
`maxdepth`	tree depth used in `learner=tree`
`m1`	number of boosting iteration
`twinboost`	logical: twin boosting?
`m2`	number of twin boosting iteration
`x`	class of `mhingeova`.
`...`	additional arguments.

Details

For a C-class problem (C > 2), each class is separately compared against all other classes with HingeBoost, and C functions are estimated to represent confidence for each class. The classification rule is to assign the class with the largest estimate. A linear or nonlinear multi-class HingeBoost classifier is fitted using a boosting algorithm based on one-against component-wise base learners for +1/-1 responses, with possible cost-sensitive hinge loss function.

Value

An object of class `mhingeova` with `print` method being available.

Author(s)

Zhu Wang

References

Zhu Wang (2011), HingeBoost: ROC-Based Boost for Classification and Variable Selection. *The International Journal of Biostatistics*, **7**(1), Article 13.

Zhu Wang (2012), Multi-class HingeBoost: Method and Application to the Classification of Cancer Types Using Gene Expression Data. *Methods of Information in Medicine*, **51**(2), 162–7.

See Also

`bst` for HingeBoost binary classification. Furthermore see `cv.bst` for stopping iteration selection by cross-validation, and `bst_control` for control parameters.

Examples

```
## Not run:
dat1 <- read.table("http://archive.ics.uci.edu/ml/machine-learning-databases/
thyroid-disease/ann-train.data")
dat2 <- read.table("http://archive.ics.uci.edu/ml/machine-learning-databases/
thyroid-disease/ann-test.data")
res <- mhingeova(xtr=dat1[,-22], ytr=dat1[,22], xte=dat2[,-22], yte=dat2[,22],
cost=c(2/3, 0.5, 0.5), nu=0.5, learner="ls", m1=100, K=5, cv1=FALSE,
twinboost=TRUE, m2= 200, cv2=FALSE)
res <- mhingeova(xtr=dat1[,-22], ytr=dat1[,22], xte=dat2[,-22], yte=dat2[,22],
cost=c(2/3, 0.5, 0.5), nu=0.5, learner="ls", m1=100, K=5, cv1=FALSE,
twinboost=TRUE, m2= 200, cv2=TRUE)

## End(Not run)
```

---

nsel *Find Number of Variables In Multi-class Boosting Iterations*

Description

Find Number of Variables In Multi-class Boosting Iterations

Usage

```
nsel(object, mstop)
```

Arguments

`object`	an object of `mhingebst`, `mbst`, or `rmbst`
`mstop`	boosting iteration number

Value

a vector of length mstop indicating number of variables selected in each boosting iteration

Author(s)

Zhu Wang

---

rbst *Robust Boosting for Robust Loss Functions*

Description

MM (majorization/minimization) algorithm based gradient boosting for optimizing nonconvex robust loss functions with componentwise linear, smoothing splines, tree models as base learners.

Usage

```
rbst(x, y, cost = 0.5, rfamily = c("tgaussian", "thuber","thinge", "tbinom", "binomd",
"texpo", "tpoisson", "clossR", "closs", "gloss", "qloss"), ctrl=bst_control(),
control.tree=list(maxdepth = 1), learner=c("ls","sm","tree"),del=1e-10)
```

Arguments

x	a data frame containing the variables in the model.
y	vector of responses. y must be in {1, -1} for classification.
cost	price to pay for false positive, 0 < cost < 1; price of false negative is 1-cost.
rfamily	robust loss function, see details.
ctrl	an object of class bst_control.
control.tree	control parameters of rpart.
learner	a character specifying the component-wise base learner to be used: ls linear models, sm smoothing splines, tree regression trees.
del	convergency criteria

Details

An MM algorithm operates by creating a convex surrogate function that majorizes the nonconvex objective function. When the surrogate function is minimized with gradient boosting algorithm, the desired objective function is decreased. The MM algorithm contains difference of convex (DC) algorithm for rfamily=c("tgaussian", "thuber","thinge", "tbinom", "binomd", "texpo", "tpoisson") and quadratic majorization boosting algorithm (QMBA) for rfamily=c("clossR", "closs", "gloss", "qloss").

rfamily = "tgaussian" for truncated square error loss, "thuber" for truncated Huber loss, "thinge" for truncated hinge loss, "tbinom" for truncated logistic loss, "binomd" for logistic difference loss, "texpo" for truncated exponential loss, "tpoisson" for truncated Poisson loss, "clossR" for C-loss in regression, "closs" for C-loss in classification, "gloss" for G-loss, "qloss" for Q-loss.

s must be a numeric value to be specified in bst_control. For rfamily="thinge", "tbinom", "texpo" s < 0. For rfamily="binomd", "tpoisson", "closs", "qloss", "clossR" , s > 0 and for rfamily="gloss", s > 1. Some suggested s values: "thinge"= -1, "tbinom"= -log(3), "binomd"= log(4), "texpo"= log(0.5), "closs"=1, "gloss"=1.5, "qloss"=2, "clossR"=1.

Value

An object of class bst with print, coef, plot and predict methods are available for linear models. For nonlinear models, methods print and predict are available.

x, y, cost, rfamily, learner, control.tree, maxdepth
: These are input variables and parameters

ctrl
: the input ctrl with possible updated fk if family="tgaussian", "thingeDC", "tbinomDC", "binomdDC" or "tpoisson".

yhat
: predicted function estimates

ens
: a list of length mstop. Each element is a fitted model to the pseudo residuals, defined as negative gradient of loss function at the current estimated function

ml.fit
: the last element of ens

ensemble
: a vector of length mstop. Each element is the variable selected in each boosting step when applicable

xselect
: selected variables in mstop

coef
: estimated coefficients in mstop

Author(s)

Zhu Wang

References

Zhu Wang (2018), Quadratic Majorization for Nonconvex Loss with Applications to the Boosting Algorithm, *Journal of Computational and Graphical Statistics*, **27**(3), 491-502, doi: 10.1080/10618600.2018.1424635

Zhu Wang (2018), Robust boosting with truncated loss functions, *Electronic Journal of Statistics*, **12**(1), 599-650, doi: 10.1214/18EJS1404

See Also

cv.rbst for cross-validated stopping iteration. Furthermore see bst_control

Examples

```
x <- matrix(rnorm(100*5),ncol=5)
c <- 2*x[,1]
p <- exp(c)/(exp(c)+exp(-c))
y <- rbinom(100,1,p)
y[y != 1] <- -1
y[1:10] <- -y[1:10]
x <- as.data.frame(x)
```

```
dat.m <- bst(x, y, ctrl = bst_control(mstop=50), family = "hinge", learner = "ls")
predict(dat.m)
dat.m1 <- bst(x, y, ctrl = bst_control(twinboost=TRUE,
coefir=coef(dat.m), xselect.init = dat.m$xselect, mstop=50))
dat.m2 <- rbst(x, y, ctrl = bst_control(mstop=50, s=0, trace=TRUE),
rfamily = "thinge", learner = "ls")
predict(dat.m2)
```

`rbstpath` *Robust Boosting Path for Nonconvex Loss Functions*

Description

Gradient boosting path for optimizing robust loss functions with componentwise linear, smoothing splines, tree models as base learners. See details below before use.

Usage

```
rbstpath(x, y, rmstop=seq(40, 400, by=20), ctrl=bst_control(), del=1e-16, ...)
```

Arguments

`x`	a data frame containing the variables in the model.
`y`	vector of responses. `y` must be in {1, -1}.
`rmstop`	vector of boosting iterations
`ctrl`	an object of class `bst_control`.
`del`	convergency criteria
`...`	arguments passed to `rbst`

Details

This function invokes `rbst` with `mstop` being each element of vector `rmstop`. It can provide different paths. Thus `rmstop` serves as another hyper-parameter. However, the most important hyper-parameter is the loss truncation point or the point determines the level of nonconvexity. This is an experimental function and may not be needed in practice.

Value

A length `rmstop` vector of lists with each element being an object of class `rbst`.

Author(s)

Zhu Wang

See Also

`rbst`

Examples

```
x <- matrix(rnorm(100*5),ncol=5)
c <- 2*x[,1]
p <- exp(c)/(exp(c)+exp(-c))
y <- rbinom(100,1,p)
y[y != 1] <- -1
y[1:10] <- -y[1:10]
x <- as.data.frame(x)
dat.m <- bst(x, y, ctrl = bst_control(mstop=50), family = "hinge", learner = "ls")
predict(dat.m)
dat.m1 <- bst(x, y, ctrl = bst_control(twinboost=TRUE,
coefir=coef(dat.m), xselect.init = dat.m$xselect, mstop=50))
dat.m2 <- rbst(x, y, ctrl = bst_control(mstop=50, s=0, trace=TRUE),
rfamily = "thinge", learner = "ls")
predict(dat.m2)
rmstop <- seq(10, 40, by=10)
dat.m3 <- rbstpath(x, y, rmstop, ctrl=bst_control(s=0), rfamily = "thinge", learner = "ls")
```

`rmbst` *Robust Boosting for Multi-class Robust Loss Functions*

Description

MM (majorization/minimization) based gradient boosting for optimizing nonconvex robust loss functions with componentwise linear, smoothing splines, tree models as base learners.

Usage

```
rmbst(x, y, cost = 0.5, rfamily = c("thinge", "closs"), ctrl=bst_control(),
control.tree=list(maxdepth = 1),learner=c("ls","sm","tree"),del=1e-10)
```

Arguments

`x`	a data frame containing the variables in the model.
`y`	vector of responses. `y` must be in {1, 2, ..., k}.
`cost`	price to pay for false positive, 0 < `cost` < 1; price of false negative is 1-`cost`.
`rfamily`	`family` = "thinge" is currently implemented.
`ctrl`	an object of class `bst_control`.
`control.tree`	control parameters of rpart.
`learner`	a character specifying the component-wise base learner to be used: `ls` linear models, `sm` smoothing splines, `tree` regression trees.
`del`	convergency criteria

Details

An MM algorithm operates by creating a convex surrogate function that majorizes the nonconvex objective function. When the surrogate function is minimized with gradient boosting algorithm, the desired objective function is decreased. The MM algorithm contains difference of convex (DC) for `rfamily="thinge"`, and quadratic majorization boosting algorithm (QMBA) for `rfamily="closs"`.

Value

An object of class `bst` with `print`, `coef`, `plot` and `predict` methods are available for linear models. For nonlinear models, methods `print` and `predict` are available.

`x`, `y`, `cost`, `rfamily`, `learner`, `control.tree`, `maxdepth`
: These are input variables and parameters

`ctrl`
: the input `ctrl` with possible updated `fk` if `type="adaptive"`

`yhat`
: predicted function estimates

`ens`
: a list of length `mstop`. Each element is a fitted model to the pseudo residuals, defined as negative gradient of loss function at the current estimated function

`ml.fit`
: the last element of `ens`

`ensemble`
: a vector of length `mstop`. Each element is the variable selected in each boosting step when applicable

`xselect`
: selected variables in `mstop`

`coef`
: estimated coefficients in `mstop`

Author(s)

Zhu Wang

References

Zhu Wang (2018), Quadratic Majorization for Nonconvex Loss with Applications to the Boosting Algorithm, *Journal of Computational and Graphical Statistics*, **27**(3), 491-502, doi: 10.1080/10618600.2018.1424635

Zhu Wang (2018), Robust boosting with truncated loss functions, *Electronic Journal of Statistics*, **12**(1), 599-650, doi: 10.1214/18EJS1404

See Also

`cv.rmbst` for cross-validated stopping iteration. Furthermore see `bst_control`

Examples

```
x <- matrix(rnorm(100*5),ncol=5)
c <- quantile(x[,1], prob=c(0.33, 0.67))
y <- rep(1, 100)
y[x[,1] > c[1] & x[,1] < c[2] ] <- 2
y[x[,1] > c[2]] <- 3
```

```
x <- as.data.frame(x)
x <- as.data.frame(x)
dat.m <- mbst(x, y, ctrl = bst_control(mstop=50), family = "hinge", learner = "ls")
predict(dat.m)
dat.m1 <- mbst(x, y, ctrl = bst_control(twinboost=TRUE,
f.init=predict(dat.m), xselect.init = dat.m$xselect, mstop=50))
dat.m2 <- rmbst(x, y, ctrl = bst_control(mstop=50, s=1, trace=TRUE),
rfamily = "thinge", learner = "ls")
predict(dat.m2)
```

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