

# Package ‘caustests’

May 8, 2026

**Type** Package

**Title** Multiple Granger Causality Tests for Time Series and Panel Data

**Version** 1.1.1

**Description** Comprehensive suite of Granger causality tests for time series and panel data. For time series: Toda-Yamamoto (1995) <[doi:10.1016/0304-4076\(94\)01616-8](https://doi.org/10.1016/0304-4076(94)01616-8)>, Fourier-based tests with single frequency (Enders and Jones, 2016) <[doi:10.1515/snde-2014-0101](https://doi.org/10.1515/snde-2014-0101)> and cumulative frequencies (Nazlioglu et al., 2019) <[doi:10.1080/1540496X.2018.1434072](https://doi.org/10.1080/1540496X.2018.1434072)>, quantile causality tests (Cai et al., 2023) <[doi:10.1016/j.frl.2023.104327](https://doi.org/10.1016/j.frl.2023.104327)>, and Bootstrap Fourier Granger Causality in Quantiles (Cheng et al., 2021) <[doi:10.1007/s12076-020-00263-0](https://doi.org/10.1007/s12076-020-00263-0)>. For panel data: Panel Fourier Toda-Yamamoto (Yilanci and Gorus, 2020) <[doi:10.1007/s11356-020-10092-9](https://doi.org/10.1007/s11356-020-10092-9)> and Panel Quantile Causality tests (Wang and Nguyen, 2022) <[doi:10.1080/1331677X.2021.1952089](https://doi.org/10.1080/1331677X.2021.1952089)>, as well as Group-Mean and Pooled Fully Modified OLS estimators for panel cointegrating polynomial regressions (Wagner and Reichold, 2023) <[doi:10.1080/07474938.2023.2178141](https://doi.org/10.1080/07474938.2023.2178141)>. All tests include bootstrap inference for robust p-values.

**License** GPL-3

**URL** <https://github.com/muhammedalkhalaf/caustests>

**BugReports** <https://github.com/muhammedalkhalaf/caustests/issues>

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**Imports** stats, quantreg

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**RoxygenNote** 7.3.3

**NeedsCompilation** no

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caustests	<i>Multiple Granger Causality Tests</i>
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## Description

Performs various Granger causality tests including Toda-Yamamoto, Fourier-based tests (single and cumulative frequency), and quantile causality tests with bootstrap inference.

## Usage

```
caustests(
  data,
  test,
  pmax = 8,
  ic = 1,
  nboot = 1000,
  kmax = 3,
  dmax = NULL,
  quantiles = seq(0.1, 0.9, 0.1),
  verbose = TRUE
)
```

**Arguments**

<code>data</code>	A data frame or matrix with time series variables (columns).
<code>test</code>	Integer 1-7 specifying the test type: <ul style="list-style-type: none"> <li>• 1: Toda-Yamamoto (1995)</li> <li>• 2: Single Fourier Granger (Enders &amp; Jones, 2016)</li> <li>• 3: Single Fourier Toda-Yamamoto (Nazlioglu et al., 2016)</li> <li>• 4: Cumulative Fourier Granger (Enders &amp; Jones, 2019)</li> <li>• 5: Cumulative Fourier Toda-Yamamoto (Nazlioglu et al., 2019)</li> <li>• 6: Quantile Toda-Yamamoto (Cai et al., 2023)</li> <li>• 7: Bootstrap Fourier Granger Causality in Quantiles (Cheng et al., 2021)</li> </ul>
<code>pmax</code>	Maximum lag order for model selection (default: 8).
<code>ic</code>	Information criterion: 1 for AIC, 2 for SBC/BIC (default: 1).
<code>nboot</code>	Number of bootstrap replications (default: 1000).
<code>kmax</code>	Maximum Fourier frequency (default: 3, used for tests 2-5, 7).
<code>dmax</code>	Extra lags for Toda-Yamamoto augmentation. If NULL, automatically set to 0 for tests 2, 4 (differences) and 1 for tests 1, 3, 5, 6, 7 (levels).
<code>quantiles</code>	Numeric vector of quantiles for tests 6-7 (default: seq(0.1, 0.9, 0.1)).
<code>verbose</code>	Logical; print progress messages (default: TRUE).

**Details**

The package implements seven Granger causality tests:

**Test 1: Toda-Yamamoto (1995)** Standard Granger causality in levels using VAR with extra lags equal to the maximum integration order (`dmax`). This approach is robust to unknown integration and cointegration properties.

**Tests 2-3: Single Fourier Frequency** Incorporate a single Fourier frequency to capture smooth structural breaks. Test 2 uses first differences, Test 3 uses levels (Toda-Yamamoto style).

**Tests 4-5: Cumulative Fourier Frequency** Use cumulative Fourier frequencies (1 to `k`) for more flexible break patterns. Test 4 uses first differences, Test 5 uses levels.

**Test 6: Quantile Toda-Yamamoto** Extends Toda-Yamamoto to quantile regression, allowing causality analysis across different quantiles of the conditional distribution.

**Test 7: Bootstrap Fourier Granger Causality in Quantiles (BFGC-Q)** Combines Fourier flexibility with quantile regression for robust inference under structural breaks and across quantiles.

**Value**

An object of class "caustests" containing:

<code>results</code>	Data frame with test results for each direction
<code>test</code>	Test number used
<code>test_name</code>	Name of the test
<code>pmax</code>	Maximum lag considered

ic	Information criterion used
nboot	Number of bootstrap replications
kmax	Maximum Fourier frequency
dmax	Augmentation lags
quantiles	Quantiles used (for tests 6-7)
quantile_results	Detailed quantile results (for tests 6-7)

## References

- Toda, H. Y., & Yamamoto, T. (1995). Statistical inference in vector autoregressions with possibly integrated processes. *Journal of Econometrics*, 66(1-2), 225-250. doi:10.1016/03044076(94)016168
- Enders, W., & Jones, P. (2016). Grain prices, oil prices, and multiple smooth breaks in a VAR. *Studies in Nonlinear Dynamics & Econometrics*, 20(4), 399-419. doi:10.1515/snde20140101
- Nazlioglu, S., Gormus, N. A., & Soytas, U. (2016). Oil prices and real estate investment trusts (REITs): Gradual-shift causality and volatility transmission analysis. *Energy Economics*, 60, 168-175. doi:10.1016/j.eneco.2016.09.009
- Nazlioglu, S., Soytas, U., & Gormus, N. A. (2019). Oil prices and monetary policy in emerging markets: Structural shifts in causal linkages. *Emerging Markets Finance and Trade*, 55(1), 105-117. doi:10.1080/1540496X.2018.1434072
- Cai, Y., Chang, T., Xiang, Y., & Chang, H. L. (2023). Testing Granger causality in quantiles between the stock and the foreign exchange markets of Japan. *Finance Research Letters*, 58, 104327. doi:10.1016/j.frl.2023.104327
- Cheng, S. C., Hsueh, H. P., Ranjbar, O., Wang, M. C., & Chang, T. (2021). Bootstrap Fourier Granger causality test in quantiles and the asymmetric causal relationship between CO2 emissions and economic growth. *Letters in Spatial and Resource Sciences*, 14, 31-49. doi:10.1007/s12076-020002630

## Examples

```
# Load example data
data(caustests_data)

# Test 1: Toda-Yamamoto test
result1 <- caustests(caustests_data, test = 1, nboot = 199)
print(result1)
summary(result1)

# Test 3: Single Fourier Toda-Yamamoto
result3 <- caustests(caustests_data, test = 3, kmax = 2, nboot = 199)
print(result3)

# Test 6: Quantile causality (fewer quantiles for speed)
result6 <- caustests(caustests_data, test = 6,
                    quantiles = c(0.25, 0.50, 0.75), nboot = 199)
print(result6)
```

---

`caustests_data`*Example Time Series Dataset for Causality Tests*

---

**Description**

A simulated dataset containing three time series variables for demonstrating Granger causality tests. The data includes one dependent variable (Y) and two potential causal variables (X1, X2) with known causal relationships.

**Usage**`caustests_data`**Format**

A data frame with 200 observations and 3 variables:

**Y** Dependent variable, generated as AR(2) plus causal effects from X1

**X1** First explanatory variable, AR(1) process

**X2** Second explanatory variable, independent AR(1) process

**Details**

The data generating process is:

- X1 and X2 are independent AR(1) processes
- Y depends on its own lags plus lagged values of X1 (but not X2)
- This creates a true causal relationship from X1 to Y
- There is no true causality from X2 to Y or from Y to X1/X2

This allows users to verify that the causality tests correctly identify the causal direction  $X1 \Rightarrow Y$  while finding no significant causality in other directions (with appropriate sample sizes and test settings).

**Source**

Simulated data for package demonstration

**Examples**

```
data(caustests_data)
head(caustests_data)
summary(caustests_data)

# Check correlations
cor(caustests_data)
```

---

`grunfeld_cmg`*Example Panel Data for xtpcmg*

---

**Description**

Returns the Grunfeld (1958) balanced panel dataset for examples.

**Usage**

```
grunfeld_cmg()
```

**Value**

A data frame with columns `firm`, `year`, `invest`, and `mvalue`.

**Examples**

```
dat <- grunfeld_cmg()
head(dat)
```

---

`grunfeld_panel`*Example Panel Data for xtpcaus*

---

**Description**

Returns a small balanced panel dataset (subset of Grunfeld 1958) for use in examples and testing.

**Usage**

```
grunfeld_panel()
```

**Value**

A data frame with columns `firm`, `year`, `invest`, and `mvalue`.

**Examples**

```
dat <- grunfeld_panel()
head(dat)
```

---

plot.caustests	<i>Plot Quantile Causality Results</i>
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---

**Description**

Creates diagnostic plots for quantile causality tests (tests 6-7).

**Usage**

```
## S3 method for class 'caustests'
plot(x, which = 1, type = "both", ...)
```

**Arguments**

x	An object of class "caustests" from test 6 or 7.
which	Which direction to plot (default: 1, first direction).
type	Plot type: "wald" for Wald statistics, "pval" for p-values, or "both" (default).
...	Additional arguments passed to plot.

**Value**

Invisibly returns the plotted data.

**Examples**

```
data(caustests_data)
result <- caustests(caustests_data, test = 6,
                   quantiles = c(0.25, 0.50, 0.75), nboot = 199)
plot(result)
```

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print.xtpcaus	<i>Print Method for xtpcaus Objects</i>
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**Description**

Print Method for xtpcaus Objects

**Usage**

```
## S3 method for class 'xtpcaus'
print(x, ...)
```

**Arguments**

x                    An object of class "xtpcaus".  
 ...                  Additional arguments (ignored).

**Value**

Invisibly returns x.

---

print.xtpcmg                  *Print Method for xtpcmg Objects*

---

**Description**

Print Method for xtpcmg Objects

**Usage**

```
## S3 method for class 'xtpcmg'
print(x, ...)
```

**Arguments**

x                    An object of class "xtpcmg".  
 ...                  Additional arguments (ignored).

**Value**

Invisibly returns x.

---

summary.xtpcaus                  *Summary Method for xtpcaus Objects*

---

**Description**

Summary Method for xtpcaus Objects

**Usage**

```
## S3 method for class 'xtpcaus'
summary(object, ...)
```

**Arguments**

object                An object of class "xtpcaus".  
 ...                  Additional arguments (ignored).

**Value**

Invisibly returns object.

---

summary.xtpcmg	<i>Summary Method for xtpcmg Objects</i>
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---

**Description**

Summary Method for xtpcmg Objects

**Usage**

```
## S3 method for class 'xtpcmg'
summary(object, ...)
```

**Arguments**

object	An object of class "xtpcmg".
...	Additional arguments (ignored).

**Value**

Invisibly returns object.

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xtpcaus	<i>Panel Granger Causality Tests</i>
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---

**Description**

Tests whether x Granger-causes y in a balanced panel using either the Panel Fourier Toda-Yamamoto (PFTY) test or the Panel Quantile Causality (PQC) test.

**Usage**

```
xtpcaus(
  data,
  y,
  x,
  panel_id,
  time_id,
  test = c("pfty", "pqc"),
  pmax = 4L,
  dmax = 1L,
  nboot = 499L,
  kmax = 3L,
```

```

ic = c("aic", "bic"),
quantiles = c(0.1, 0.25, 0.5, 0.75, 0.9),
seed = -1L
)

```

### Arguments

<code>data</code>	A data frame in long format.
<code>y</code>	Character. Name of the dependent (caused) variable.
<code>x</code>	Character. Name of the independent (causing) variable.
<code>panel_id</code>	Character. Name of the panel identifier variable.
<code>time_id</code>	Character. Name of the time variable.
<code>test</code>	Character. Test type: "pfty" for Panel Fourier Toda-Yamamoto or "pqc" for Panel Quantile Causality.
<code>pmax</code>	Integer. Maximum lag order for selection. Default is 4.
<code>dmax</code>	Integer. Maximum integration order for Toda-Yamamoto augmentation. Default is 1.
<code>nboot</code>	Integer. Number of bootstrap replications. Minimum 99. Default is 499.
<code>kmax</code>	Integer. Maximum Fourier frequency (PFTY only). Default is 3.
<code>ic</code>	Character. Information criterion: "aic" or "bic". Default is "aic".
<code>quantiles</code>	Numeric vector. Quantile grid for PQC test (values strictly between 0 and 1). Default is <code>c(0.1, 0.25, 0.50, 0.75, 0.90)</code> .
<code>seed</code>	Integer. Random seed for bootstrap. -1 means no seed. Default is -1.

### Value

An object of class "xtpcaus" containing:

- test** Character. "pfty" or "pqc".
- N** Integer. Number of panel units.
- TT** Integer. Number of time periods.
- nboot** Integer. Number of bootstrap replications.
- y** Character. Name of the y variable.
- x** Character. Name of the x variable. For PFTY:
- fisher** Numeric. Fisher panel statistic.
- fisher\_df** Integer. Degrees of freedom (2\*N).
- fisher\_pv** Numeric. Fisher p-value.
- wbar** Numeric. Average individual Wald statistic.
- zbar** Numeric. Dumitrescu-Hurlin Z-bar statistic.
- zbar\_pv** Numeric. Z-bar p-value.
- ind\_wald** Numeric vector. Individual Wald statistics (length N).
- ind\_freq** Integer vector. Optimal Fourier frequencies (length N).

**ind\_pval\_b** Numeric vector. Bootstrap p-values (length N).  
**ind\_lags** Integer vector. Selected lag orders (length N). For PQC:  
**quantiles** Numeric vector. Quantiles tested.  
**wald\_xy** Numeric vector. Wald statistics per quantile ( $x \Rightarrow y$ ).  
**pval\_xy** Numeric vector. Bootstrap p-values per quantile ( $x \Rightarrow y$ ).  
**wald\_yx** Numeric vector. Wald statistics per quantile ( $y \Rightarrow x$ ).  
**pval\_yx** Numeric vector. Bootstrap p-values per quantile ( $y \Rightarrow x$ ).  
**supwald\_xy** Numeric. Sup-Wald statistic for  $x \Rightarrow y$ .  
**supwald\_yx** Numeric. Sup-Wald statistic for  $y \Rightarrow x$ .  
**p\_opt** Integer. Selected optimal lag.

## References

Chuang, C.C., Kuan, C.M. and Lin, H.Y. (2009). Causality in quantiles and dynamic stock return-volume relations. *Journal of Banking and Finance*, 33(7), 1351–1360. doi:10.1016/j.jbankfin.2009.02.013

Emirmahmutoglu, F. and Kose, N. (2011). Testing for Granger causality in heterogeneous mixed panels. *Economic Modelling*, 28(3), 870–876. doi:10.1016/j.econmod.2010.10.018

Toda, H.Y. and Yamamoto, T. (1995). Statistical inference in vector autoregressions with possibly integrated processes. *Journal of Econometrics*, 66(1–2), 225–250. doi:10.1016/03044076(94)01616-8

Wang, K.M. and Nguyen, T.B. (2022). A quantile panel-type analysis of income inequality and healthcare expenditure. *Economic Research*, 35(1), 873–893. doi:10.1080/1331677X.2021.1952089

Yilanci, V. and Gorus, M.S. (2020). Does economic globalization have predictive power for ecological footprint. *Environmental Science and Pollution Research*, 27, 40552–40562. doi:10.1007/s11356020100929

## Examples

```
dat <- grunfeld_panel()
# PFTY test (quick with few bootstrap reps)

res <- xtpcaus(dat, y = "invest", x = "mvalue",
              panel_id = "firm", time_id = "year",
              test = "pfty", pmax = 2L, dmax = 1L,
              nboot = 99L, kmax = 2L, seed = 42L)

print(res)

# PQC test

res2 <- xtpcaus(dat, y = "invest", x = "mvalue",
               panel_id = "firm", time_id = "year",
               test = "pqc", pmax = 2L, nboot = 99L,
               quantiles = c(0.25, 0.50, 0.75), seed = 42L)

print(res2)
```

xtpcmg

*Panel Cointegrating Polynomial Regressions via FM-OLS***Description**

Estimates a polynomial cointegrating regression in a panel using either Group-Mean FM-OLS (Wagner & Reichold 2023) or Pooled FM-OLS (de Jong & Wagner 2022). Models the long-run relationship:

**Usage**

```
xtpcmg(
  data,
  y,
  x,
  panel_id,
  time_id,
  model = c("mg", "pmg"),
  q = 2L,
  controls = NULL,
  trend = 1L,
  kernel = "ba",
  bw = "And91",
  effects = "oneway",
  corr_rob = FALSE
)
```

**Arguments**

<code>data</code>	A data frame in long format.
<code>y</code>	Character. Name of the dependent variable.
<code>x</code>	Character. Name of the polynomial (I(1)) regressor.
<code>panel_id</code>	Character. Name of the panel identifier variable.
<code>time_id</code>	Character. Name of the time variable.
<code>model</code>	Character. Estimator: "mg" for Group-Mean FM-OLS (default) or "pmg" for Pooled FM-OLS.
<code>q</code>	Integer. Polynomial degree: 2 (quadratic, default) or 3 (cubic).
<code>controls</code>	Character vector. Names of additional I(1) control variables. Default is NULL (no controls).
<code>trend</code>	Integer. Deterministic trend type: 1 for demeaning only (default), 2 for demeaning and detrending.
<code>kernel</code>	Character. HAC kernel: "ba" (Bartlett, default), "pa" (Parzen), "qs" (Quadratic Spectral), "tr" (truncated), "bo" (Bohman).

bw	Character or numeric. Bandwidth for HAC estimation. "And91" (default) uses Andrews (1991) automatic selection. A numeric value sets the bandwidth directly.
effects	Character. For Pooled FM-OLS: "oneway" (default) for one-way demeaning or "twoways" for two-way demeaning.
corr_rob	Logical. For Group-Mean FM-OLS: if TRUE, use cross-sectionally robust VCV. Default is FALSE.

## Details

$$y_{it} = \alpha_i + \beta_1 x_{it} + \beta_2 x_{it}^2 [+ \beta_3 x_{it}^3] [+ \gamma z_{it}] + u_{it}$$

where  $x_{it}$  and  $z_{it}$  are I(1) processes.

## Value

An object of class "xtpcmg" with elements: coefficients (named numeric vector), vcov (variance-covariance matrix), se (standard errors), tstat (t-statistics), pvalue (two-sided p-values), model (estimator type: mg or pmg), q (polynomial degree), N (number of panel units), TT (number of time periods), y (dependent variable name), x (polynomial variable name), tp (turning point estimate, quadratic models only), tp\_se (delta-method SE for turning point), tp\_lo and tp\_hi (95% CI bounds), ind\_coef (individual FM-OLS estimates, MG model), swamy\_s and swamy\_p (Swamy slope homogeneity test).

## References

- Andrews, D.W.K. (1991). Heteroskedasticity and autocorrelation consistent covariance matrix estimation. *Econometrica*, 59(3), 817–858. doi:10.2307/2938229
- de Jong, R.M. and Wagner, M. (2022). Panel cointegrating polynomial regressions. *Annals of Applied Statistics*, 16(1), 416–442. doi:10.1214/21AOAS1536
- Wagner, M. and Reichold, K. (2023). Panel cointegrating polynomial regressions. *Econometric Reviews*, 42(9–10), 782–827. doi:10.1080/07474938.2023.2178141

## Examples

```
dat <- grunfeld_cmg()

# Group-Mean FM-OLS (quadratic EKC-type model)
res <- xtpcmg(dat, y = "invest", x = "mvalue",
             panel_id = "firm", time_id = "year",
             model = "mg", q = 2L)

print(res)
summary(res)

# Pooled FM-OLS
res2 <- xtpcmg(dat, y = "invest", x = "mvalue",
              panel_id = "firm", time_id = "year",
              model = "pmg", q = 2L)
```

```
print(res2)
```

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