

Package ‘cmna’

May 8, 2026

Type Package

Title Computational Methods for Numerical Analysis

Version 1.0.5

Date 2021-07-14

Encoding UTF-8

URL <https://jameshoward.us/cmna/>

BugReports <https://github.com/k3jph/cmna-pkg/issues>

Description Provides the source and examples for James P. Howard, II,
``Computational Methods for Numerical Analysis with R,"
<<https://jameshoward.us/cmna/>>, a book on numerical
methods in R.

License BSD_2_clause + file LICENSE

Suggests testthat, devtools, markdown, roxygen2

Depends R (>= 2.10)

RoxygenNote 7.1.1

NeedsCompilation no

Author James Howard [aut, cre] (ORCID:
<<https://orcid.org/0000-0003-4530-1547>>)

Maintainer James Howard <jh@jameshoward.us>

Repository CRAN

Date/Publication 2021-07-14 13:40:02 UTC

Contents

cmna-package	3
adaptint	3
bezier	4
bilinear	5
bisection	6
bvp	7

choleskymatrix	8
cubicspline	8
detmatrix	9
division	10
fibonacci	11
findiff	12
gaussint	13
gds	14
giniquintile	15
goldsect	16
gradient	17
heat	18
hillclimbing	19
himmelblau	20
horner	20
invmatrix	21
isPrime	22
iterativematrix	23
ivp	24
ivpsys	25
linterp	25
lumatrix	26
mcint	27
midpt	28
newton	29
nn	30
nthroot	31
polyinterp	32
pwiselinterp	33
quadratic	34
refmatrix	35
resizeImage	36
revolution-solid	36
romberg	37
rowops	38
sa	39
secant	40
simp	41
simp38	42
summation	43
trap	44
tridiagmatrix	45
vecnorm	45
wave	46
wilkinson	47

cmna-package

Computational Methods for Numerical Analysis

Description

Provides the source and examples for *Computational Methods for Numerical Analysis with R*.

Details

This package provides a suite of simple implementations of standard methods from numerical analysis. The collection is designed to accompany *Computational Methods for Numerical Analysis with R* by James P. Howard, II. Together, these functions provide methods to support linear algebra, interpolation, integration, root finding, optimization, and differential equations.

Author(s)

James P. Howard, II <jh@jameshoward.us>

See Also

Useful links:

- <https://jameshoward.us/cmna/>
- Report bugs at <https://github.com/k3jph/cmna-pkg/issues>

adaptint

Adaptive Integration

Description

Adaptive integration

Usage

```
adaptint(f, a, b, n = 10, tol = 1e-06)
```

Arguments

f	function to integrate
a	the a-bound of integration
b	the b-bound of integration
n	the maximum recursive depth
tol	the maximum error tolerance

Details

The `adaptint` function uses Romberg's rule to calculate the integral of the function `f` over the interval from `a` to `b`. The parameter `n` sets the number of intervals to use when evaluating. Additional options are passed to the function `f` when evaluating.

Value

the value of the integral

See Also

Other integration: [gaussint\(\)](#), [giniquintile\(\)](#), [mcint\(\)](#), [midpt\(\)](#), [revolution-solid](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Other newton-cotes: [giniquintile\(\)](#), [midpt\(\)](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Examples

```
f <- function(x) { sin(x)^2 + log(x) }
adaptint(f, 1, 10, n = 4)
adaptint(f, 1, 10, n = 5)
adaptint(f, 1, 10, n = 10)
```

bezier

Bezier curves

Description

Find the quadratic and cubic Bezier curve for the given points

Usage

```
qbezier(x, y, t)
```

```
cbezier(x, y, t)
```

Arguments

<code>x</code>	a vector of x values
<code>y</code>	a vector of y values
<code>t</code>	a vector of t values for which the curve will be computed

Details

`qbezier` finds the quadratic Bezier curve for the given three points and `cbezier` finds the cubic Bezier curve for the given four points. The curve will be computed at all values in the vector `t` and a list of `x` and `y` values returned.

Value

a list composed of an x-vector and a y-vector

See Also

Other interp: [bilinear\(\)](#), [cubicspline\(\)](#), [linterp\(\)](#), [nn\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#)

Examples

```
x <- c(1, 2, 3)
y <- c(2, 3, 5)
f <- qbezier(x, y, seq(0, 1, 1/100))
```

```
x <- c(-1, 1, 0, -2)
y <- c(-2, 2, -1, -1)
f <- cbezier(x, y, seq(0, 1, 1/100))
```

bilinear

Bilinear interpolation

Description

Finds a bilinear interpolation bounded by four points

Usage

```
bilinear(x, y, z, newx, newy)
```

Arguments

x	vector of two x values representing x_1 and x_2
y	vector of two y values representing y_1 and y_2
z	2x2 matrix of z values
newx	vector of new x values to interpolate
newy	vector of new y values to interpolate

Details

bilinear finds a bilinear interpolation bounded by four corners

Value

a vector of interpolated z values at (x, y)

See Also

Other interp: [bezier](#), [cubicspline\(\)](#), [linterp\(\)](#), [nn\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#)

Other algebra: [cubicspline\(\)](#), [division](#), [fibonacci\(\)](#), [horner\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
x <- c(2, 4)
y <- c(4, 7)
z <- matrix(c(81, 84, 85, 89), nrow = 2)
newx <- c(2.5, 3, 3.5)
newy <- c(5, 5.5, 6)
bilinear(x, y, z, newx, newy)
```

bisection

The Bisection Method

Description

Use the bisection method to find real roots

Usage

```
bisection(f, a, b, tol = 0.001, m = 100)
```

Arguments

f	function to locate a root for
a	the a bound of the search region
b	the b bound of the search region
tol	the error tolerance
m	the maximum number of iterations

Details

The bisection method functions by repeatedly halving the interval between a and b and will return when the interval between them is less than tol, the error tolerance. However, this implementation also stops if after m iterations.

Value

the real root found

See Also

Other optimz: [goldsect](#), [gradient](#), [hillclimbing\(\)](#), [newton\(\)](#), [sa\(\)](#), [secant\(\)](#)

Examples

```
f <- function(x) { x^3 - 2 * x^2 - 159 * x - 540 }  
bisection(f, 0, 10)
```

bvp*Boundary value problems*

Description

solve boundary value problems for ordinary differential equations

Usage

```
bvpexample(x)  
  
bvpexample10(x)
```

Arguments

x proposed initial x-value

Details

The euler method implements the Euler method for solving differential equations. The codemidp-
tvp method solves initial value problems using the second-order Runge-Kutta method. The rungekutta4
method is the fourth-order Runge-Kutta method.

Value

a data frame of x and y values

Examples

```
bvpexample(-2)  
bvpexample(-1)  
bvpexample(0)  
bvpexample(1)  
bvpexample(2)  
## (bvp.b <- bisection(bvpexample, 0, 1))  
## (bvp.s <- secant(bvpexample, 0))
```

choleskymatrix *Cholesky Decomposition*

Description

Decompose a matrix into the Cholesky

Usage

```
choleskymatrix(m)
```

Arguments

m a matrix

Details

choleskymatrix decomposes the matrix m into the LU decomposition, such that $m == L$

Value

the matrix L

See Also

Other linear: [detmatrix\(\)](#), [gdls\(\)](#), [invmatrix\(\)](#), [iterativematrix](#), [lumatrix\(\)](#), [refmatrix\(\)](#), [rowops](#), [tridiagmatrix\(\)](#), [vecnorm\(\)](#)

Examples

```
(A <- matrix(c(5, 1, 2, 1, 9, 3, 2, 3, 7), 3))
(L <- choleskymatrix(A))
t(L) %**% L
```

cubicspline *Natural cubic spline interpolation*

Description

Finds a piecewise linear function that interpolates the data points

Usage

```
cubicspline(x, y)
```

Arguments

x a vector of x values
y a vector of y values

Details

cubicspline finds a piecewise cubic spline function that interpolates the data points. For each x-y ordered pair. The function will return a list of four vectors representing the coefficients.

Value

a list of coefficient vectors

See Also

Other interp: [bezier](#), [bilinear\(\)](#), [linterp\(\)](#), [nn\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#)
Other algebra: [bilinear\(\)](#), [division](#), [fibonacci\(\)](#), [horner\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
x <- c(1, 2, 3)
y <- c(2, 3, 5)
f <- cubicspline(x, y)

x <- c(-1, 1, 0, -2)
y <- c(-2, 2, -1, -1)
f <- cubicspline(x, y)
```

detmatrix

Calculate the determinant of the matrix

Description

Calculate the determinant of the matrix

Usage

```
detmatrix(m)
```

Arguments

m a matrix

Details

detmatrix calculates the determinant of the matrix given.

Value

the determinant

See Also

Other linear: [choleskymatrix\(\)](#), [gdls\(\)](#), [invmatrix\(\)](#), [iterativematrix](#), [lumatrix\(\)](#), [refmatrix\(\)](#), [rowops](#), [tridiagmatrix\(\)](#), [vecnorm\(\)](#)

Examples

```
A <- matrix(c(1, 2, -7, -1, -1, 1, 2, 1, 5), 3)
detmatrix(A)
```

division

Algorithms for divisions

Description

Algorithms for division that provide a quotient and remainder.

Usage

```
naivediv(m, n)
```

```
longdiv(m, n)
```

Arguments

m the dividend

n the divisor

Details

The `naivediv` divides `m` by `n` by using repeated division. The `longdiv` function uses the long division algorithm in binary.

Value

the quotient and remainder as a list

See Also

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [fibonacci\(\)](#), [horner\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
a <- floor(runif(1, 1, 1000))
b <- floor(runif(1, 1, 100))
naivediv(a, b)
longdiv(a, b)
```

fibonacci

Fibonacci numbers

Description

Return the n-th Fibonacci number

Usage

```
fibonacci(n)
```

Arguments

n n

Details

This function recursively implements the famous Fibonacci sequence. The function returns the nth member of the sequence.

Value

the sequence element

See Also

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [division](#), [horner\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
fibonacci(10)
```

`findiff`*Finite Differences*

Description

Finite differences formulas

Usage

```
findiff(f, x, h = x * sqrt(.Machine$double.eps))
```

```
syndiff(f, x, h = x * .Machine$double.eps^(1/3))
```

```
findiff2(f, x, h)
```

```
rdiff(f, x, n = 10, h = 1e-04)
```

Arguments

<code>f</code>	function to differentiate
<code>x</code>	the x-value to differentiate at
<code>h</code>	the step-size for evaluation
<code>n</code>	the maximum number of convergence steps in <code>rdiff</code>

Details

The `findiff` formula uses the finite differences formula to find the derivative of `f` at `x`. The value of `h` is the step size of the evaluation. The function `findiff2` provides the second derivative.

Value

the value of the derivative

Examples

```
findiff(sin, pi, 1e-3)
syndiff(sin, pi, 1e-3)
```

`gaussint`*Gaussian integration method driver*

Description

Use the Gaussian method to evaluate integrals

Usage

```
gaussint(f, x, w)
```

```
gauss.legendre(f, m = 5)
```

```
gauss.laguerre(f, m = 5)
```

```
gauss.hermite(f, m = 5)
```

Arguments

<code>f</code>	function to integrate
<code>x</code>	list of evaluation points
<code>w</code>	list of weights
<code>m</code>	number of evaluation points

Details

The `gaussint` function uses the Gaussian integration to evaluate an integral. The function itself is a driver and expects the integration points and associated weights as options.

Value

the value of the integral

See Also

Other integration: [adaptint\(\)](#), [giniqintile\(\)](#), [mcint\(\)](#), [midpt\(\)](#), [revolution-solid](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Examples

```
w = c(1, 1)
x = c(-1 / sqrt(3), 1 / sqrt(3))
f <- function(x) { x^3 + x + 1 }
gaussint(f, x, w)
```

`gdls`*Least squares with gradient descent*

Description

Solve least squares with gradient descent

Usage

```
gdls(A, b, alpha = 0.05, tol = 1e-06, m = 1e+05)
```

Arguments

<code>A</code>	a square matrix representing the coefficients of a linear system
<code>b</code>	a vector representing the right-hand side of the linear system
<code>alpha</code>	the learning rate
<code>tol</code>	the expected error tolerance
<code>m</code>	the maximum number of iterations

Details

`gdls` solves a linear system using gradient descent.

Value

the modified matrix

See Also

Other linear: [choleskymatrix\(\)](#), [detmatrix\(\)](#), [invmatrix\(\)](#), [iterativematrix](#), [lumatrix\(\)](#), [refmatrix\(\)](#), [rowops](#), [tridiagmatrix\(\)](#), [vecnorm\(\)](#)

Examples

```
head(b <- iris$Sepal.Length)
head(A <- matrix(cbind(1, iris$Sepal.Width, iris$Petal.Length, iris$Petal.Width), ncol = 4))
gdls(A, b, alpha = 0.05, m = 10000)
```

giniquintile	<i>Gini coefficients</i>
--------------	--------------------------

Description

Calculate the Gini coefficient from quintile data

Usage

```
giniquintile(L)
```

Arguments

L vector of percentages at 20th, 40th, 60th, and 80th percentiles

Details

Calculate the Gini coefficient given the quintile data.

Value

the estimated Gini coefficient

References

Leon Gerber, "A Quintile Rule for the Gini Coefficient", *Mathematics Magazine*, 80:2, April 2007.

See Also

Other integration: [adaptint\(\)](#), [gaussint\(\)](#), [mcint\(\)](#), [midpt\(\)](#), [revolution-solid](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Other newton-cotes: [adaptint\(\)](#), [midpt\(\)](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Examples

```
L <- c(4.3, 9.8, 15.4, 22.7)
giniquintile(L)
```

`goldsect`*Golden Section Search*

Description

Use golden section search to find local extrema

Usage

```
goldsectmin(f, a, b, tol = 0.001, m = 100)
```

```
goldsectmax(f, a, b, tol = 0.001, m = 100)
```

Arguments

<code>f</code>	function to integrate
<code>a</code>	the a bound of the search region
<code>b</code>	the b bound of the search region
<code>tol</code>	the error tolerance
<code>m</code>	the maximum number of iterations

Details

The golden section search method functions by repeatedly dividing the interval between a and b and will return when the interval between them is less than `tol`, the error tolerance. However, this implementation also stop if after `m` iterations.

Value

the x value of the minimum found

See Also

Other optimz: [bisection\(\)](#), [gradient](#), [hillclimbing\(\)](#), [newton\(\)](#), [sa\(\)](#), [secant\(\)](#)

Examples

```
f <- function(x) { x^2 - 3 * x + 3 }  
goldsectmin(f, 0, 5)
```

gradient	<i>Gradient descent</i>
----------	-------------------------

Description

Use gradient descent to find local minima

Usage

```
graddsc(fp, x, h = 0.001, tol = 1e-04, m = 1000)
```

```
gradasc(fp, x, h = 0.001, tol = 1e-04, m = 1000)
```

```
gd(fp, x, h = 100, tol = 1e-04, m = 1000)
```

Arguments

fp	function representing the derivative of f
x	an initial estimate of the minima
h	the step size
tol	the error tolerance
m	the maximum number of iterations

Details

Gradient descent can be used to find local minima of functions. It will return an approximation based on the step size h and fp . The tol is the error tolerance, x is the initial guess at the minimum. This implementation also stops after m iterations.

Value

the x value of the minimum found

See Also

Other optimz: [bisection\(\)](#), [goldsect](#), [hillclimbing\(\)](#), [newton\(\)](#), [sa\(\)](#), [secant\(\)](#)

Examples

```
fp <- function(x) { x^3 + 3 * x^2 - 1 }  
graddsc(fp, 0)
```

```
f <- function(x) { (x[1] - 1)^2 + (x[2] - 1)^2 }  
fp <-function(x) {  
  x1 <- 2 * x[1] - 2  
  x2 <- 8 * x[2] - 8
```

```
    return(c(x1, x2))
  }
gd(fp, c(0, 0), 0.05)
```

heat

Heat Equation via Forward-Time Central-Space

Description

solve heat equation via forward-time central-space method

Usage

```
heat(u, alpha, xdelta, tdelta, n)
```

Arguments

u	the initial values of u
alpha	the thermal diffusivity coefficient
xdelta	the change in x at each step in u
tdelta	the time step
n	the number of steps to take

Details

The heat solves the heat equation using the forward-time central-space method in one-dimension.

Value

a matrix of u values at each time step

Examples

```
alpha <- 1
x0 <- 0
xdelta <- .05
x <- seq(x0, 1, xdelta)
u <- sin(x^4 * pi)
tdelta <- .001
n <- 25
z <- heat(u, alpha, xdelta, tdelta, n)
```

hillclimbing	<i>Hill climbing</i>
--------------	----------------------

Description

Use hill climbing to find the global minimum

Usage

```
hillclimbing(f, x, h = 1, m = 1000)
```

Arguments

f	function representing the derivative of f
x	an initial estimate of the minimum
h	the step size
m	the maximum number of iterations

Details

Hill climbing

Value

the x value of the minimum found

See Also

Other optimz: [bisection\(\)](#), [goldsect](#), [gradient](#), [newton\(\)](#), [sa\(\)](#), [secant\(\)](#)

Examples

```
f <- function(x) {  
  (x[1]^2 + x[2] - 11)^2 + (x[1] + x[2]^2 - 7)^2  
}  
hillclimbing(f, c(0,0))  
hillclimbing(f, c(-1,-1))  
hillclimbing(f, c(10,10))
```

`himmelblau`*Himmelblau Function*

Description

Generate the Himmelblau function

Usage`himmelblau(x)`**Arguments**

`x` a vector of x-values

Details

Generate the Himmelblau function

Value

the value of the function at `x`.

`horner`*Horner's rule*

Description

Use Horner's rule to evaluate a polynomial

Usage`horner(x, coefs)``rhorer(x, coefs)``naivepoly(x, coefs)``betterpoly(x, coefs)`**Arguments**

`x` a vector of x values to evaluate the polynomial

`coefs` vector of coefficients of x

Details

This function implements Horner's rule for fast polynomial evaluation. The implementation expects x to be a vector of x values at which to evaluate the polynomial. The parameter `coefs` is a vector of coefficients of x . The vector order is such that the first element is the constant term, the second element is the coefficient of x , the so forth to the highest degree term. Terms with a 0 coefficient should have a 0 element in the vector.

The function `rhorners` implements the the Horner algorithm recursively.

The function `naivepoly` implements a polynomial evaluator using the straightforward algebraic approach.

The function `betterpoly` implements a polynomial evaluator using the straightforward algebraic approach with cached x terms.

Value

the value of the function at x

See Also

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [division](#), [fibonacci\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
b <- c(2, 10, 11)
x <- 5
horner(x, b)
b <- c(-1, 0, 1)
x <- c(1, 2, 3, 4)
horner(x, b)
rhorners(x, b)
```

invmatrix

Invert a matrix

Description

Invert the matrix using Gaussian elimination

Usage

```
invmatrix(m)
```

Arguments

`m` a matrix

Details

`invmatrix` invertse the given matrix using Gaussian elimination and returns the result.

Value

the inverted matrix

See Also

Other linear: [choleskymatrix\(\)](#), [detmatrix\(\)](#), [gdls\(\)](#), [iterativematrix](#), [lumatrix\(\)](#), [refmatrix\(\)](#), [rowops](#), [tridiagmatrix\(\)](#), [vecnorm\(\)](#)

Examples

```
A <- matrix(c(1, 2, -7, -1, -1, 1, 2, 1, 5), 3)
refmatrix(A)
```

isPrime

Test for Primality

Description

Test the number given for primality.

Usage

```
isPrime(n)
```

Arguments

n n

Details

This function tests n if it is prime through repeated division attempts. If a match is found, by finding a remainder of 0, FALSE is returned.

Value

boolean TRUE if n is prime, FALSE if not

See Also

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [division](#), [fibonacci\(\)](#), [horner\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
isPrime(37)
isPrime(89)
isPrime(100)
```

iterativematrix *Solve a matrix using iterative methods*

Description

Solve a matrix using iterative methods.

Usage

```
jacobi(A, b, tol = 1e-06, maxiter = 100)
gaussseidel(A, b, tol = 1e-06, maxiter = 100)
cgmmatrix(A, b, tol = 1e-06, maxiter = 100)
```

Arguments

A	a square matrix representing the coefficients of a linear system
b	a vector representing the right-hand side of the linear system
tol	is a number representing the error tolerance
maxiter	is the maximum number of iterations

Details

`jacobi` finds the solution using Jacobi iteration. Jacobi iteration depends on the matrix being diagonally-dominant. The tolerance is specified the norm of the solution vector.

`gaussseidel` finds the solution using Gauss-Seidel iteration. Gauss-Seidel iteration depends on the matrix being either diagonally-dominant or symmetric and positive definite.

`cgmmatrix` finds the solution using the conjugate gradient method. The conjugate gradient method depends on the matrix being symmetric and positive definite.

Value

the solution vector

See Also

Other linear: [choleskymatrix\(\)](#), [detmatrix\(\)](#), [gdls\(\)](#), [invmatrix\(\)](#), [lumatrix\(\)](#), [refmatrix\(\)](#), [rowops](#), [tridiagmatrix\(\)](#), [vecnorm\(\)](#)

Examples

```
A <- matrix(c(5, 2, 1, 2, 7, 3, 3, 4, 8), 3)
b <- c(40, 39, 55)
jacobi(A, b)
```

ivp

Initial value problems

Description

solve initial value problems for ordinary differential equations

Usage

```
euler(f, x0, y0, h, n)
midptivp(f, x0, y0, h, n)
rungekutta4(f, x0, y0, h, n)
adamsbashforth(f, x0, y0, h, n)
```

Arguments

f	function to integrate
x0	the initial value of x
y0	the initial value of y
h	selected step size
n	the number of steps

Details

The euler method implements the Euler method for solving differential equations. The codemidptivp method solves initial value problems using the second-order Runge-Kutta method. The rungekutta4 method is the fourth-order Runge-Kutta method.

Value

a data frame of x and y values

Examples

```
f <- function(x, y) { y / (2 * x + 1) }
ivp.euler <- euler(f, 0, 1, 1/100, 100)
ivp.midpt <- midptivp(f, 0, 1, 1/100, 100)
ivp.rk4 <- rungekutta4(f, 0, 1, 1/100, 100)
```

`ivpsys`*Initial value problems for systems of ordinary differential equations*

Description

solve initial value problems for systems ordinary differential equations

Usage

```
eulersys(f, x0, y0, h, n)
```

Arguments

<code>f</code>	function to integrate
<code>x0</code>	the initial value of x
<code>y0</code>	the vector initial values of y
<code>h</code>	selected step size
<code>n</code>	the number of steps

Details

The euler method implements the Euler method for solving differential equations. The `codemidp` method solves initial value problems using the second-order Runge-Kutta method. The `rungekutta4` method is the fourth-order Runge-Kutta method.

Value

a data frame of x and y values

Examples

```
f <- function(x, y) { y / (2 * x + 1) }  
ivp.euler <- euler(f, 0, 1, 1/100, 100)
```

`linterp`*Linear interpolation*

Description

Finds a linear function between two points

Usage

```
linterp(x1, y1, x2, y2)
```

Arguments

x1	x value of the first point
y1	y value of the first point
x2	x value of the second point
y2	y value of the second point

Details

linterp finds a linear function between two points.

Value

a linear equation's coefficients

See Also

Other interp: [bezier](#), [bilinear\(\)](#), [cubicspline\(\)](#), [nn\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#)

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [division](#), [fibonacci\(\)](#), [horner\(\)](#), [isPrime\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
f <- linterp(3, 2, 7, -2)
```

 lumatrix

LU Decomposition

Description

Decompose a matrix into lower- and upper-triangular matrices

Usage

```
lumatrix(m)
```

Arguments

m	a matrix
---	----------

Details

lumatrix decomposes the matrix m into the LU decomposition, such that $m == L$

Value

list with matrices L and U representing the LU decomposition

See Also

Other linear: [choleskymatrix\(\)](#), [detmatrix\(\)](#), [gdls\(\)](#), [invmatrix\(\)](#), [iterativematrix](#), [refmatrix\(\)](#), [rowops](#), [tridiagmatrix\(\)](#), [vecnorm\(\)](#)

Examples

```
A <- matrix(c(1, 2, -7, -1, -1, 1, 2, 1, 5), 3)
lumatrix(A)
```

 mcint

Monte Carlo Integration

Description

Simple Monte Carlo Integraton

Usage

```
mcint(f, a, b, m = 1000)

mcint2(f, xdom, ydom, m = 1000)
```

Arguments

f	function to integrate
a	the lower-bound of integration
b	the upper-bound of integration
m	the number of subintervals to calculate
xdom	the domain on x of integration in two dimensions
ydom	the domain on y of integration in two dimensions

Details

The mcint function uses a simple Monte Carlo algorithm to estimate the value of an integral. The parameter n sets the total number of evaluation points. The parameter max.y is the maximum expected value of the range of function f. The mcint2 provides Monte Carlo integration in two dimensions.

Value

the value of the integral

See Also

Other integration: [adaptint\(\)](#), [gaussint\(\)](#), [giniquintile\(\)](#), [midpt\(\)](#), [revolution-solid](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Examples

```
f <- function(x) { sin(x)^2 + log(x) }
mcint(f, 0, 1)
mcint(f, 0, 1, m = 10e6)
```

midpt	<i>rectangle method</i>
-------	-------------------------

Description

Use the rectangle method to integrate a function

Usage

```
midpt(f, a, b, m = 100)
```

Arguments

f	function to integrate
a	the a-bound of integration
b	the b-bound of integration
m	the number of subintervals to calculate

Details

The midpt function uses the rectangle method to calculate the integral of the function f over the interval from a to b. The parameter m sets the number of intervals to use when evaluating the rectangles. Additional options are passed to the function f when evaluating.

Value

the value of the integral

See Also

Other integration: [adaptint\(\)](#), [gaussint\(\)](#), [giniquintile\(\)](#), [mcint\(\)](#), [revolution-solid](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Other newton-cotes: [adaptint\(\)](#), [giniquintile\(\)](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Examples

```
f <- function(x) { sin(x)^2 + cos(x)^2 }
midpt(f, -pi, pi, m = 10)
midpt(f, -pi, pi, m = 100)
midpt(f, -pi, pi, m = 1000)
```

newton	<i>Newton's method</i>
--------	------------------------

Description

Use Newton's method to find real roots

Usage

```
newton(f, fp, x, tol = 0.001, m = 100)
```

Arguments

f	function to integrate
fp	function representing the derivative of f
x	an initial estimate of the root
tol	the error tolerance
m	the maximum number of iterations

Details

Newton's method finds real roots of a function, but requires knowing the function derivative. It will return when the interval between them is less than `tol`, the error tolerance. However, this implementation also stops after `m` iterations.

Value

the real root found

See Also

Other optimz: [bisection\(\)](#), [goldsect](#), [gradient](#), [hillclimbing\(\)](#), [sa\(\)](#), [secant\(\)](#)

Examples

```
f <- function(x) { x^3 - 2 * x^2 - 159 * x - 540 }
fp <- function(x) { 3 * x^2 - 4 * x - 159 }
newton(f, fp, 1)
```

nn	<i>Nearest interpolation</i>
----	------------------------------

Description

Find the nearest neighbor for a set of data points

Usage

```
nn(p, y, q)
```

Arguments

p	matrix of variable values, each row is a data point
y	vector of values, each entry corresponds to one row in p
q	vector of variable values, each entry corresponds to one column of p

Details

nn finds the n-dimensional nearest neighbor for given datapoint

Value

an interpolated value for *q*

See Also

Other interp: [bezier](#), [bilinear\(\)](#), [cubicspline\(\)](#), [linterp\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#)

Examples

```
p <- matrix(floor(runif(100, 0, 9)), 20)
y <- floor(runif(20, 0, 9))
q <- matrix(floor(runif(5, 0, 9)), 1)
nn(p, y, q)
```

nthroot	<i>The n-th root formula</i>
---------	------------------------------

Description

Find the n-th root of real numbers

Usage

```
nthroot(a, n, tol = 1/1000)
```

Arguments

a	a positive real number
n	n
tol	the permitted error tolerance

Details

The nthroot function finds the nth root of a via an iterative process.

Value

the root

See Also

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [division](#), [fibonacci\(\)](#), [horner\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
nthroot(100, 2)
nthroot(65536, 4)
nthroot(1000, 3)
```

polyinterp	<i>Polynomial interpolation</i>
------------	---------------------------------

Description

Finds a polynomial function interpolating the given points

Usage

```
polyinterp(x, y)
```

Arguments

x	a vector of x values
y	a vector of y values

Details

polyinterp finds a polynomial that interpolates the given points.

Value

a polynomial equation's coefficients

See Also

Other interp: [bezier](#), [bilinear\(\)](#), [cubicspline\(\)](#), [linterp\(\)](#), [nn\(\)](#), [pwiselinterp\(\)](#)

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [division](#), [fibonacci\(\)](#), [horner\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [pwiselinterp\(\)](#), [quadratic\(\)](#)

Examples

```
x <- c(1, 2, 3)
y <- x^2 + 5 * x - 3
f <- polyinterp(x, y)
```

pwiselinterp

Piecewise linear interpolation

Description

Finds a piecewise linear function that interpolates the data points

Usage

```
pwiselinterp(x, y)
```

Arguments

x	a vector of x values
y	a vector of y values

Details

pwiselinterp finds a piecewise linear function that interpolates the data points. For each x-y ordered pair, there function finds the unique line interpolating them. The function will return a data.frame with three columns.

The column x is the upper bound of the domain for the given piece. The columns m and b represent the coefficients from the y-intercept form of the linear equation, $y = mx + b$.

The matrix will contain length(x) rows with the first row having m and b of NA.

Value

a matrix with the linear function components

See Also

Other interp: [bezier](#), [bilinear\(\)](#), [cubicspline\(\)](#), [linterp\(\)](#), [nn\(\)](#), [polyinterp\(\)](#)

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [division](#), [fibonacci\(\)](#), [horner\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [quadratic\(\)](#)

Examples

```
x <- c(5, 0, 3)
y <- c(4, 0, 3)
f <- pwiselinterp(x, y)
```

`quadratic`*The quadratic equation.*

Description

Find the zeros of a quadratic equation.

Usage

```
quadratic(b2, b1, b0)
```

```
quadratic2(b2, b1, b0)
```

Arguments

<code>b2</code>	the coefficient of the x^2 term
<code>b1</code>	the coefficient of the x term
<code>b0</code>	the constant term

Details

`quadratic` and `quadratic2` implement the quadratic equation from standard algebra in two different ways. The `quadratic` function is susceptible to cascading numerical error and the `quadratic2` has reduced potential error.

Value

numeric vector of solutions to the equation

See Also

Other algebra: [bilinear\(\)](#), [cubicspline\(\)](#), [division](#), [fibonacci\(\)](#), [horner\(\)](#), [isPrime\(\)](#), [linterp\(\)](#), [nthroot\(\)](#), [polyinterp\(\)](#), [pwiselinterp\(\)](#)

Examples

```
quadratic(1, 0, -1)
quadratic(4, -4, 1)
quadratic2(1, 0, -1)
quadratic2(4, -4, 1)
```

`refmatrix`*Matrix to Row Echelon Form*

Description

Transform a matrix to row echelon form.

Usage`refmatrix(m)``rrefmatrix(m)``solvematrix(A, b)`**Arguments**

`m` a matrix

`A` a square matrix representing the coefficients of a linear system in `solvematrix`

`b` a vector representing the right-hand side of the linear system in `solvematrix`

Details

`refmatrix` reduces a matrix to row echelon form. This is not a reduced row echelon form, though that can be easily calculated from the diagonal. This function works on non-square matrices.

`rrefmatrix` returns the reduced row echelon matrix.

`solvematrix` solves a linear system using `rrefmatrix`.

Value

the modified matrix

See Also

Other linear: [choleskymatrix\(\)](#), [detmatrix\(\)](#), [gdls\(\)](#), [invmatrix\(\)](#), [iterativematrix](#), [lumatrix\(\)](#), [rowops](#), [tridiagmatrix\(\)](#), [vecnorm\(\)](#)

Examples

```
A <- matrix(c(1, 2, -7, -1, -1, 1, 2, 1, 5), 3)
refmatrix(A)
```

resizeImage	<i>Image resizing</i>
-------------	-----------------------

Description

Resize images using nearest neighbor and

Usage

```
resizeImageNN(imx, width, height)
```

```
resizeImageBL(imx, width, height)
```

Arguments

imx	a 3-dimensional array containing image data
width	the new width
height	the new height

Details

The *resizeImageNN* function uses the nearest neighbor method to resize the image. Also, *resizeImageBL* uses bilinear interpolation to resize the image.

Value

a three-dimensional array containing the resized image.

revolution-solid	<i>Volumes of solids of revolution</i>
------------------	--

Description

Find the volume of a solid of revolution

Usage

```
shellmethod(f, a, b)
```

```
discmethod(f, a, b)
```

Arguments

f	function of revolution
a	lower-bound of the solid
b	upper-bound of the solid

Details

The functions `discmethod` and `shellmethod` implement the algorithms for finding the volume of solids of revolution. The `discmethod` function is suitable for volumes revolved around the x-axis and the `shellmethod` function is suitable for volumes revolved around the y-axis.

Value

the volume of the solid

See Also

Other integration: [adaptint\(\)](#), [gaussint\(\)](#), [giniquintile\(\)](#), [mcint\(\)](#), [midpt\(\)](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Examples

```
f <- function(x) { x^2 }
shellmethod(f, 1, 2)
discmethod(f, 1, 2)
```

romberg

Romberg Integration

Description

Romberg's adaptive integration

Usage

```
romberg(f, a, b, m, tab = FALSE)
```

Arguments

f	function to integrate
a	the lowerbound of integration
b	the upperbound of integration
m	the maximum number of iterations
tab	if TRUE, return the table of values

Details

The `romberg` function uses Romberg's rule to calculate the integral of the function `f` over the interval from `a` to `b`. The parameter `m` sets the number of intervals to use when evaluating. Additional options are passed to the function `f` when evaluating.

Value

the value of the integral

See Also

Other integration: [adaptint\(\)](#), [gaussint\(\)](#), [giniquintile\(\)](#), [mcint\(\)](#), [midpt\(\)](#), [revolution-solid](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Other newton-cotes: [adaptint\(\)](#), [giniquintile\(\)](#), [midpt\(\)](#), [simp38\(\)](#), [simp\(\)](#), [trap\(\)](#)

Examples

```
f <- function(x) { sin(x)^2 + log(x) }
romberg(f, 1, 10, m = 3)
romberg(f, 1, 10, m = 5)
romberg(f, 1, 10, m = 10)
```

rowops

Elementary row operations

Description

These are elementary operations for a matrix. They do not presume a square matrix and will work on any matrix. They use R's internal row addressing to function.

Usage

```
swaprows(m, row1, row2)
```

```
replacerow(m, row1, row2, k)
```

```
scalerow(m, row, k)
```

Arguments

m	a matrix
row1	a source row
row2	a destination row
k	a scaling factor
row	a row to modify

Details

replacerow replaces one row with the sum of itself and the multiple of another row. swaprows swap two rows in the matrix. scalerow scales all entries in a row by a constant.

Value

the modified matrix

See Also

Other linear: [choleskymatrix\(\)](#), [detmatrix\(\)](#), [gdls\(\)](#), [invmatrix\(\)](#), [iterativematrix](#), [lumatrix\(\)](#), [refmatrix\(\)](#), [tridiagmatrix\(\)](#), [vecnorm\(\)](#)

Examples

```
n <- 5
A <- matrix(sample.int(10, n^2, TRUE) - 1, n)
A <- swaprows(A, 2, 4)
A <- replacerow(A, 1, 3, 2)
A <- scalerow(A, 5, 10)
```

sa

Simulated annealing

Description

Use simulated annealing to find the global minimum

Usage

```
sa(f, x, temp = 10000, rate = 1e-04)
```

```
tspsa(x, temp = 100, rate = 1e-04)
```

Arguments

f	function representing f
x	an initial estimate of the minimum
temp	the initial temperature
rate	the cooling rate

Details

Simulated annealing finds a global minimum by mimicing the metallurgical process of annealing.

Value

the x value of the minimum found

See Also

Other optimz: [bisection\(\)](#), [goldsect](#), [gradient](#), [hillclimbing\(\)](#), [newton\(\)](#), [secant\(\)](#)

Examples

```
f <- function(x) { x^6 - 4 * x^5 - 7 * x^4 + 22 * x^3 + 24 * x^2 + 2 }
sa(f, 0)
```

```
f <- function(x) { (x[1] - 1)^2 + (x[2] - 1)^2 }
sa(f, c(0, 0), 0.05)
```

 secant

Secant Method

Description

The secant method for root finding

Usage

```
secant(f, x, tol = 0.001, m = 100)
```

Arguments

f	function to integrate
x	an initial estimate of the root
tol	the error tolerance
m	the maximum number of iterations

Details

The secant method for root finding extends Newton's method to estimate the derivative. It will return when the interval between them is less than `tol`, the error tolerance. However, this implementation also stop if after `m` iterations.

Value

the real root found

See Also

Other optimz: [bisection\(\)](#), [goldsect](#), [gradient](#), [hillclimbing\(\)](#), [newton\(\)](#), [sa\(\)](#)

Examples

```
f <- function(x) { x^3 - 2 * x^2 - 159 * x - 540 }
secant(f, 1)
```

`simp`*Simpson's rule*

Description

Use Simpson's rule to integrate a function

Usage

```
simp(f, a, b, m = 100)
```

Arguments

<code>f</code>	function to integrate
<code>a</code>	the a-bound of integration
<code>b</code>	the b-bound of integration
<code>m</code>	the number of subintervals to calculate

Details

The `simp` function uses Simpson's rule to calculate the integral of the function `f` over the interval from `a` to `b`. The parameter `m` sets the number of intervals to use when evaluating. Additional options are passed to the function `f` when evaluating.

Value

the value of the integral

See Also

Other integration: [adaptint\(\)](#), [gaussint\(\)](#), [giniquintile\(\)](#), [mcint\(\)](#), [midpt\(\)](#), [revolution-solid](#), [romberg\(\)](#), [simp38\(\)](#), [trap\(\)](#)

Other newton-cotes: [adaptint\(\)](#), [giniquintile\(\)](#), [midpt\(\)](#), [romberg\(\)](#), [simp38\(\)](#), [trap\(\)](#)

Examples

```
f <- function(x) { sin(x)^2 + cos(x)^2 }
simp(f, -pi, pi, m = 10)
simp(f, -pi, pi, m = 100)
simp(f, -pi, pi, m = 1000)
```

`simp38`*Simpson's 3/8 rule*

Description

Use Simpson's 3/8 rule to integrate a function

Usage

```
simp38(f, a, b, m = 100)
```

Arguments

<code>f</code>	function to integrate
<code>a</code>	the a-bound of integration
<code>b</code>	the b-bound of integration
<code>m</code>	the number of subintervals to calculate

Details

The `simp38` function uses Simpson's 3/8 rule to calculate the integral of the function `f` over the interval from `a` to `b`. The parameter `m` sets the number of intervals to use when evaluating. Additional options are passed to the function `f` when evaluating.

Value

the value of the integral

See Also

Other integration: [adaptint\(\)](#), [gaussint\(\)](#), [giniquintile\(\)](#), [mcint\(\)](#), [midpt\(\)](#), [revolution-solid](#), [romberg\(\)](#), [simp\(\)](#), [trap\(\)](#)

Other newton-cotes: [adaptint\(\)](#), [giniquintile\(\)](#), [midpt\(\)](#), [romberg\(\)](#), [simp\(\)](#), [trap\(\)](#)

Examples

```
f <- function(x) { sin(x)^2 + log(x) }
simp38(f, 1, 10, m = 10)
simp38(f, 1, 10, m = 100)
simp38(f, 1, 10, m = 1000)
```

`summation`*Two summing algorithms*

Description

Find the sum of a vector

Usage`naivesum(x)``kahansum(x)``pwisum(x)`**Arguments**

`x` a vector of numbers to be summed

Details

`naivesum` calculates the sum of a vector by keeping a counter and repeatedly adding the next value to the interim sum. `kahansum` uses Kahan's algorithm to capture the low-order precision loss and ensure that the loss is reintegrated into the final sum. `pwisum` is a recursive implementation of the piecewise summation algorithm that divides the vector in two and adds the individual vector sums for a result.

Value

the sum

Examples

```
k <- 1:10^6
n <- sample(k, 1)
bound <- sample(k, 2)
bound.upper <- max(bound) - 10^6 / 2
bound.lower <- min(bound) - 10^6 / 2
x <- runif(n, bound.lower, bound.upper)
naivesum(x)
kahansum(x)
pwisum(x)
```

trap

Trapezoid method

Description

Use the trapezoid method to integrate a function

Usage

```
trap(f, a, b, m = 100)
```

Arguments

f	function to integrate
a	the a-bound of integration
b	the b-bound of integration
m	the number of subintervals to calculate

Details

The trap function uses the trapezoid method to calculate the integral of the function f over the interval from a to b. The parameter m sets the number of intervals to use when evaluating the trapezoids. Additional options are passed to the function f when evaluating.

Value

the value of the integral

See Also

Other integration: [adaptint\(\)](#), [gaussint\(\)](#), [giniqintile\(\)](#), [mcint\(\)](#), [midpt\(\)](#), [revolution-solid](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#)

Other newton-cotes: [adaptint\(\)](#), [giniqintile\(\)](#), [midpt\(\)](#), [romberg\(\)](#), [simp38\(\)](#), [simp\(\)](#)

Examples

```
f <- function(x) { sin(x)^2 + cos(x)^2 }  
trap(f, -pi, pi, m = 10)  
trap(f, -pi, pi, m = 100)  
trap(f, -pi, pi, m = 1000)
```

tridiagmatrix	<i>Solve a tridiagonal matrix</i>
---------------	-----------------------------------

Description

use the tridiagonal matrix algorithm to solve a tridiagonal matrix

Usage

```
tridiagmatrix(L, D, U, b)
```

Arguments

L	vector of entries below the main diagonal
D	vector of entries on the main diagonal
U	vector of entries above the main diagonal
b	vector of the right-hand side of the linear system

Details

tridiagmatrix uses the tridiagonal matrix algorithm to solve a tridiagonal matrix.

Value

the solution vector

See Also

Other linear: [choleskymatrix\(\)](#), [detmatrix\(\)](#), [gdls\(\)](#), [invmatrix\(\)](#), [iterativematrix](#), [lumatrix\(\)](#), [refmatrix\(\)](#), [rowops](#), [vecnorm\(\)](#)

vecnorm	<i>Norm of a vector</i>
---------	-------------------------

Description

Find the norm of a vector

Usage

```
vecnorm(b)
```

Arguments

b	a vector
---	----------

Details

Find the norm of a vector

Value

the norm

See Also

Other linear: [choleskymatrix\(\)](#), [detmatrix\(\)](#), [gdls\(\)](#), [invmatrix\(\)](#), [iterativematrix](#), [lumatrix\(\)](#), [refmatrix\(\)](#), [rowops](#), [tridiagmatrix\(\)](#)

Examples

```
x <- c(1, 2, 3)
vecnorm(x)
```

wave

Wave Equation using

Description

solve heat equation via forward-time central-space method

Usage

```
wave(u, alpha, xdelta, tdelta, n)
```

Arguments

u	the initial values of u
alpha	the thermal diffusivity coefficient
xdelta	the change in x at each step in u
tdelta	the time step
n	the number of steps to take

Details

The heat solves the heat equation using the forward-time central-space method in one-dimension.

Value

a matrix of u values at each time step

Examples

```
speed <- 2
x0 <- 0
xdelta <- .05
x <- seq(x0, 1, xdelta)
m <- length(x)
u <- sin(x * pi * 2)
u[11:21] <- 0
tdelta <- .02
n <- 40
z <- wave(u, speed, xdelta, tdelta, n)
```

wilkinson

Wilkinson's Polynomial

Description

Wilkinson's polynomial

Usage

```
wilkinson(x, w = 20)
```

Arguments

x	the x-value
w	the number of terms in the polynomial

Details

Wilkinson's polynomial is a terrible joke played on numerical analysis. By tradition, the function is $f(x) = (x - 1)(x - 2)\dots(x - 20)$, giving a function with real roots at each integer from 1 to 20. This function is generalized and allows for n and the function value is $f(x) = (x - 1)(x - 2)\dots(x - n)$. The default of n is 20.

Value

the value of the function at x

Examples

```
wilkinson(0)
```

Index

- * **adaptive**
 - adaptint, 3
 - * **algebra**
 - bilinear, 5
 - cubicspline, 8
 - division, 10
 - fibonacci, 11
 - horner, 20
 - isPrime, 22
 - linterp, 25
 - nthroot, 31
 - polyinterp, 32
 - pwiselinterp, 33
 - quadratic, 34
 - * **differentiation**
 - findiff, 12
 - * **integration**
 - adaptint, 3
 - gaussint, 13
 - giniquintile, 15
 - mcint, 27
 - midpt, 28
 - revolution-solid, 36
 - romberg, 37
 - simp, 41
 - simp38, 42
 - trap, 44
 - * **interpolation**
 - resizeImage, 36
 - * **interp**
 - bezier, 4
 - bilinear, 5
 - cubicspline, 8
 - linterp, 25
 - nn, 30
 - polyinterp, 32
 - pwiselinterp, 33
 - * **intro**
 - summation, 43
 - * **linear**
 - choleskymatrix, 8
 - detmatrix, 9
 - gdls, 14
 - invmatrix, 21
 - iterativematrix, 23
 - lumatrix, 26
 - refmatrix, 35
 - rowops, 38
 - tridiagmatrix, 45
 - vecnorm, 45
 - * **newton-cotes**
 - adaptint, 3
 - giniquintile, 15
 - midpt, 28
 - romberg, 37
 - simp, 41
 - simp38, 42
 - trap, 44
 - * **optimz**
 - bisection, 6
 - goldsect, 16
 - gradient, 17
 - hillclimbing, 19
 - newton, 29
 - sa, 39
 - secant, 40
 - * **polynomials**
 - wilkinson, 47
- adamsbashforth (ivp), 24
- adaptint, 3, 13, 15, 27, 28, 37, 38, 41, 42, 44
- betterpoly (horner), 20
- bezier, 4, 6, 9, 26, 30, 32, 33
- bilinear, 5, 5, 9–11, 21, 22, 26, 30–34
- bisection, 6, 16, 17, 19, 29, 39, 40
- bvp, 7
- bvpexample (bvp), 7
- bvpexample10 (bvp), 7

- cbezier (bezier), 4
- cgmmatrix (iterativematrix), 23
- choleskymatrix, 8, 10, 14, 22, 23, 27, 35, 39, 45, 46
- cmna (cmna-package), 3
- cmna-package, 3
- cubicspline, 5, 6, 8, 10, 11, 21, 22, 26, 30–34
- detmatrix, 8, 9, 14, 22, 23, 27, 35, 39, 45, 46
- discmethod (revolution-solid), 36
- division, 6, 9, 10, 11, 21, 22, 26, 31–34
- euler (ivp), 24
- eulersys (ivpsys), 25
- fibonacci, 6, 9, 10, 11, 21, 22, 26, 31–34
- findiff, 12
- findiff2 (findiff), 12
- gauss.hermite (gaussint), 13
- gauss.laguerre (gaussint), 13
- gauss.legendre (gaussint), 13
- gaussint, 4, 13, 15, 27, 28, 37, 38, 41, 42, 44
- gaussseidel (iterativematrix), 23
- gd (gradient), 17
- gdls, 8, 10, 14, 22, 23, 27, 35, 39, 45, 46
- giniquintile, 4, 13, 15, 27, 28, 37, 38, 41, 42, 44
- goldsect, 6, 16, 17, 19, 29, 39, 40
- goldsectmax (goldsect), 16
- goldsectmin (goldsect), 16
- gradasc (gradient), 17
- graddsc (gradient), 17
- gradient, 6, 16, 17, 19, 29, 39, 40
- heat, 18
- hillclimbing, 6, 16, 17, 19, 29, 39, 40
- himmelblau, 20
- horner, 6, 9–11, 20, 22, 26, 31–34
- invmatrix, 8, 10, 14, 21, 23, 27, 35, 39, 45, 46
- isPrime, 6, 9–11, 21, 22, 26, 31–34
- iterativematrix, 8, 10, 14, 22, 23, 27, 35, 39, 45, 46
- ivp, 24
- ivpsys, 25
- jacobi (iterativematrix), 23
- kahansum (summation), 43
- linterp, 5, 6, 9–11, 21, 22, 25, 30–34
- longdiv (division), 10
- lumatrix, 8, 10, 14, 22, 23, 26, 35, 39, 45, 46
- mcint, 4, 13, 15, 27, 28, 37, 38, 41, 42, 44
- mcint2 (mcint), 27
- midpt, 4, 13, 15, 27, 28, 37, 38, 41, 42, 44
- midptivp (ivp), 24
- naivediv (division), 10
- naivepoly (horner), 20
- naivesum (summation), 43
- newton, 6, 16, 17, 19, 29, 39, 40
- nn, 5, 6, 9, 26, 30, 32, 33
- nthroot, 6, 9–11, 21, 22, 26, 31, 32–34
- polyinterp, 5, 6, 9–11, 21, 22, 26, 30, 31, 32, 33, 34
- pwiselinterp, 5, 6, 9–11, 21, 22, 26, 30–32, 33, 34
- pwisesum (summation), 43
- qbezier (bezier), 4
- quadratic, 6, 9–11, 21, 22, 26, 31–33, 34
- quadratic2 (quadratic), 34
- rdiff (findiff), 12
- refmatrix, 8, 10, 14, 22, 23, 27, 35, 39, 45, 46
- replacerow (rowops), 38
- resizeImage, 36
- resizeImageBL (resizeImage), 36
- resizeImageNN (resizeImage), 36
- revolution-solid, 36
- rhorners (horner), 20
- romberg, 4, 13, 15, 27, 28, 37, 37, 41, 42, 44
- rowops, 8, 10, 14, 22, 23, 27, 35, 38, 45, 46
- rrefmatrix (refmatrix), 35
- rungekutta4 (ivp), 24
- sa, 6, 16, 17, 19, 29, 39, 40
- scalerow (rowops), 38
- secant, 6, 16, 17, 19, 29, 39, 40
- shellmethod (revolution-solid), 36
- simp, 4, 13, 15, 27, 28, 37, 38, 41, 42, 44
- simp38, 4, 13, 15, 27, 28, 37, 38, 41, 42, 44
- solvematrix (refmatrix), 35
- summation, 43
- swaprows (rowops), 38
- syndiff (findiff), 12

trap, [4](#), [13](#), [15](#), [27](#), [28](#), [37](#), [38](#), [41](#), [42](#), [44](#)
tridiagmatrix, [8](#), [10](#), [14](#), [22](#), [23](#), [27](#), [35](#), [39](#),
[45](#), [46](#)
tspas (sa), [39](#)

vecnorm, [8](#), [10](#), [14](#), [22](#), [23](#), [27](#), [35](#), [39](#), [45](#), [45](#)

wave, [46](#)
wilkinson, [47](#)