

# Package ‘excursions’

May 8, 2026

**Type** Package

**Title** Excursion Sets and Contour Credibility Regions for Random Fields

**Version** 2.5.11

**Description** Functions that compute probabilistic excursion sets, contour credibility regions, contour avoiding regions, and simultaneous confidence bands for latent Gaussian random processes and fields. The package also contains functions that calculate these quantities for models estimated with the INLA package. The main references for excursions are Bolin and Lindgren (2015) <[doi:10.1111/rssb.12055](https://doi.org/10.1111/rssb.12055)>, Bolin and Lindgren (2017) <[doi:10.1080/10618600.2016.1228537](https://doi.org/10.1080/10618600.2016.1228537)>, and Bolin and Lindgren (2018) <[doi:10.18637/jss.v086.i05](https://doi.org/10.18637/jss.v086.i05)>. These can be generated by the citation function in R.

**Depends** R (>= 3.5), Matrix

**Imports** fmesher (>= 0.5.0), graphics, methods, stats, withr, lifecycle

**Suggests** INLA (>= 21.08.31), testthat (>= 3.0.0), sf, sp, inlabru (>= 2.12.0), RColorBrewer, splancs, fields, rSPDE, knitr, rmarkdown

**VignetteBuilder** knitr

**SystemRequirements** Gnu Scientific Library version >= 2.1

**Additional\_repositories** <https://inla.r-inla-download.org/R/testing>

**BugReports** <https://github.com/davidbolin/excursions/issues>

**License** GPL (>= 3)

**URL** <https://github.com/davidbolin/excursions>,  
<https://davidbolin.github.io/excursions/>

**Copyright** The R package and code, and the main programs, were written by and are Copyright by David Bolin and Finn Lindgren, and are redistributable under the GNU Public License, version 3 or later. The package also includes code from the libraries CAMD from the SuiteSparse collection of Tim Davis, and the RngStreams library by Pierre L'Ecuyer. For details see the COPYRIGHTS file.

**NeedsCompilation** yes

**RoxygenNote** 7.3.3

**Encoding** UTF-8

**Config/testthat/parallel** true

**Config/testthat/edition** 3

**Author** David Bolin [cre, aut] (ORCID: <<https://orcid.org/0000-0003-2361-5465>>),  
 Finn Lindgren [aut] (ORCID: <<https://orcid.org/0000-0002-5833-2011>>),  
 Suen Man Ho [ctb]

**Maintainer** David Bolin <davidbolin@gmail.com>

**Repository** CRAN

**Date/Publication** 2025-12-15 10:50:02 UTC

## Contents

|                                |    |
|--------------------------------|----|
| excursions-package . . . . .   | 3  |
| continuous . . . . .           | 4  |
| contourmap . . . . .           | 7  |
| contourmap.colors . . . . .    | 9  |
| contourmap.inla . . . . .      | 10 |
| contourmap.mc . . . . .        | 14 |
| excursions . . . . .           | 16 |
| excursions.inla . . . . .      | 19 |
| excursions.mc . . . . .        | 23 |
| excursions.variances . . . . . | 25 |
| exc_safe_inla . . . . .        | 26 |
| gaussint . . . . .             | 27 |
| require.nowarnings . . . . .   | 29 |
| simconf . . . . .              | 30 |
| simconf.inla . . . . .         | 32 |
| simconf.mc . . . . .           | 34 |
| simconf.mixture . . . . .      | 36 |
| submesh.grid . . . . .         | 38 |
| submesh.mesh . . . . .         | 39 |
| summary.excurobj . . . . .     | 40 |
| tricontour . . . . .           | 40 |

**Index** 45

---

excursions-package      *Excursions: Excursion Sets and Contour Credibility Regions for Random Fields*

---

## Description

excursions contains functions that compute probabilistic excursion sets, contour credibility regions, contour avoiding regions, contour map quality measures, and simultaneous confidence bands for latent Gaussian random processes and fields. A detailed manual can be found in the paper Bolin, D and Lindgren, F (2018) *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, 86(5), 1–20.

## Details

The main functions in the package fall into three different categories described below.

### Excursion sets, contour credibility regions, and contour avoiding regions

The main functions for computing excursion sets, contour credibility regions, and contour avoiding regions are

`excursions()` The main function for Gaussian models.

`excursions.inla()` Interface for latent Gaussian models estimated using INLA.

`excursions.mc()` Function for analyzing models that have been estimated using Monte Carlo methods.

The output from the functions above provides a discrete domain estimate of the regions. Based on this estimate, the function `continuous()` computes a continuous domain estimate.

The main reference for these functions is Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

### Contour map quality measures

The package provides several functions for computing contour maps and their quality measures. These quality measures can be used to decide on an appropriate number of contours to use for the contour map.

The main functions for computing contour maps and the corresponding quality measures are

`contourmap()` The main function for Gaussian models.

`contourmap.inla()` Interface for latent Gaussian models estimated using INLA.

`contourmap.mc()` Function for analyzing models that have been estimated using Monte Carlo methods.

Other noteworthy functions relating to contourmaps are `tricontour()` and `tricontourmap()`, which compute contour curves for functions defined on triangulations, as well as `contourmap.colors()` which can be used to compute appropriate colors for displaying contour maps.

The main reference for these functions is Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, 26:3, 513-524.

### Simultaneous confidence bands

The main functions for computing simultaneous confidence bands are

`simconf()` Function for analyzing Gaussian models.

`simconf.inla()` Function for analyzing latent Gaussian models estimated using INLA.

`simconf.mc()` Function for analyzing models estimated using Monte Carlo methods.

`simconf.mixture()` Function for analyzing Gaussian mixture models.

The main reference for these functions is Bolin et al. (2015) *Statistical prediction of global sea level from global temperature*, *Statistica Sinica*, Vol 25, pp 351-367.

### Author(s)

**Maintainer:** David Bolin <davidbolin@gmail.com> ([ORCID](#))

Authors:

- Finn Lindgren <finn.lindgren@gmail.com> ([ORCID](#))

Other contributors:

- Suen Man Ho <M.H.Suen@sms.ed.ac.uk> [contributor]

### See Also

Useful links:

- <https://github.com/davidbolin/excursions>
- <https://davidbolin.github.io/excursions/>
- Report bugs at <https://github.com/davidbolin/excursions/issues>

---

continuous

*Calculate continuous domain excursion and credible contour sets*

---

### Description

Calculates continuous domain excursion and credible contour sets

### Usage

```
continuous(  
  ex,  
  geometry,  
  alpha,  
  method = c("log", "linear", "step"),  
  output = c("sp", "fm", "inla"),  
  subdivisions = 1,  
  calc.credible = TRUE  
)
```

**Arguments**

|               |   |
|---------------|---|
| ex            | An excurobj object generated by a call to <code>excursions()</code> or <code>contourmap()</code> .  |
| geometry      | Specification of the lattice or triangulation geometry of the input. One of <code>list(x, y)</code> , <code>list(loc, dims)</code> , <code>fm_lattice_2d</code> , <code>inla.mesh.lattice</code> , <code>fm_mesh_2d</code> , or <code>inla.mesh</code> , where <code>x</code> and <code>y</code> are vectors, <code>loc</code> is a two-column matrix of coordinates, and <code>dims</code> is the lattice size vector. The first three versions are all treated topologically as lattices, and the lattice boxes are assumed convex. |
| alpha         | The target error probability. A warning is given if it is detected that the information <code>ex</code> isn't sufficient for the given <code>alpha</code> . Defaults to the value used when calculating <code>ex</code> .   |
| method        | The spatial probability interpolation transformation method to use. One of <code>log</code> , <code>linear</code> , or <code>step</code> . For <code>log</code> , the probabilities are interpolated linearly in the transformed scale. For <code>step</code> , a conservative step function is used.   |
| output        | Specifies what type of object should be generated. <code>sp</code> gives a <code>SpatialPolygons</code> object, and <code>fm</code> or <code>inla</code> gives a <code>fm_segm</code> object.   |
| subdivisions  | The number of mesh triangle subdivisions to perform for the interpolation of the excursions or contour function. 0 is no subdivision. The setting has a small effect on the evaluation of $P_0$ for the <code>log</code> method (higher values giving higher accuracy) but the main effect is on the visual appearance of the interpolation. Default=1.   |
| calc.credible | Logical, if TRUE (default), calculate credible contour region objects in addition to avoidance sets.  |

**Value**

|                      |   |
|----------------------|---|
| A list with elements |   |
| M                    | <code>SpatialPolygons</code> or <code>fm_segm</code> object. The subsets are tagged, so that credible regions are tagged "-1", and regions between levels are tagged as <code>character(0:nlevels)</code> . |
| F                    | Interpolated F function.  |
| G                    | Contour and inter-level set indices for the interpolation.  |
| F.geometry           | Mesh geometry for the interpolation.  |
| $P_0$                | $P_0$ measure based on interpolated F function (only for <code>contourmap</code> input).  |

**Author(s)**

Finn Lindgren <finn.lindgren@gmail.com>

**References**

- Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, vol 26, no 3, pp 513-524.
- Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

## Examples

```

## Not run:
if (require("fmesher") &&
    require("sp")) {
  # Generate mesh and SPDE model
  n.lattice <- 10 # Increase for more interesting, but slower, examples
  x <- seq(from = 0, to = 10, length.out = n.lattice)
  lattice <- fm_lattice_2d(x = x, y = x)
  mesh <- fm_rcdt_2d_inla(lattice = lattice, extend = FALSE, refine = FALSE)

  # Generate an artificial sample
  sigma2.e <- 0.1
  n.obs <- 100
  obs.loc <- cbind(
    runif(n.obs) * diff(range(x)) + min(x),
    runif(n.obs) * diff(range(x)) + min(x)
  )
  Q <- fm_matern_precision(mesh, alpha = 2, rho = 3, sigma = 1)
  x <- fm_sample(n = 1, Q = Q)
  A <- fm_basis(mesh, loc = obs.loc)
  Y <- as.vector(A %*% x + rnorm(n.obs) * sqrt(sigma2.e))

  ## Calculate posterior
  Q.post <- (Q + (t(A) %*% A) / sigma2.e)
  mu.post <- as.vector(solve(Q.post, (t(A) %*% Y) / sigma2.e))
  vars.post <- excursions.variances(chol(Q.post), max.threads = 1)

  ## Calculate contour map with two levels
  map <- contourmap(
    n.levels = 2, mu = mu.post, Q = Q.post,
    alpha = 0.1, F.limit = 0.1, max.threads = 1
  )

  ## Calculate the continuous representation
  sets <- continuous(map, mesh, alpha = 0.1)

  ## Plot the results
  reo <- mesh$idix$lattice
  cols <- contourmap.colors(map,
    col = heat.colors(100, 1, rev = TRUE),
    credible.col = grey(0.5, 1)
  )
  names(cols) <- as.character(-1:2)

  par(mfrow = c(2, 2))
  image(matrix(mu.post[reo], n.lattice, n.lattice),
    main = "mean", axes = FALSE, asp = 1
  )
  image(matrix(sqrt(vars.post[reo]), n.lattice, n.lattice),
    main = "sd", axes = FALSE, asp = 1
  )
  image(matrix(map$M[reo], n.lattice, n.lattice),

```

```

    col = cols, axes = FALSE, asp = 1
  )
  idx.M <- setdiff(names(sets$M), "-1")
  plot(sets$M[idx.M], col = cols[idx.M])
}

## End(Not run)

```

---

contourmap

*Contour maps and contour map quality measures for latent Gaussian models*


---

## Description

contourmap is used for calculating contour maps and quality measures for contour maps for Gaussian models.

## Usage

```

contourmap(
  mu,
  Q,
  vars,
  n.levels,
  ind,
  levels,
  type = c("standard", "pretty", "equalarea", "P0-optimal", "P1-optimal", "P2-optimal"),
  compute = list(F = TRUE, measures = NULL),
  use.marginals = TRUE,
  alpha,
  F.limit,
  n.iter = 10000,
  verbose = FALSE,
  max.threads = 0,
  seed = NULL
)

```

## Arguments

|          |  |
|----------|--|
| mu       | Expectation vector.                                      |
| Q        | Precision matrix.  |
| vars     | Precomputed marginal variances (optional).               |
| n.levels | Number of levels in contour map.                         |
| ind      | Indices of the nodes that should be analyzed (optional). |
| levels   | Levels to use in contour map.                            |

|               |   |
|---------------|---|
| type          | Type of contour map. One of:<br><b>'standard'</b> Equidistant levels between smallest and largest value of the posterior mean (default).<br><b>'pretty'</b> Equally spaced 'round' values which cover the range of the values in the posterior mean.<br><b>'equalarea'</b> Levels such that different spatial regions are approximately equal in size.<br><b>'P0-optimal'</b> Levels chosen to maximize the P0 measure.<br><b>'P1-optimal'</b> Levels chosen to maximize the P1 measure.<br><b>'P2-optimal'</b> Levels chosen to maximize the P2 measure. |
| compute       | A list with quality indices to compute<br><b>'F'</b> : TRUE/FALSE indicating whether the contour map function should be computed (default TRUE).<br><b>'measures'</b> : A list with the quality measures to compute ("P0", "P1", "P2") or corresponding bounds based only on the marginal probabilities ("P0-bound", "P1-bound", "P2-bound").   |
| use.marginals | Only marginal distributions are used when finding P-optimal maps (default TRUE).  |
| alpha         | Maximal error probability in contour map function (default=1).  |
| F.limit       | The limit value for the computation of the F function. F is set to NA for all nodes where $F < 1 - F.limit$ . Default is $F.limit = alpha$ .  |
| n.iter        | Number of iterations in the MC sampler that is used for calculating the quantities in compute. The default value is 10000.  |
| verbose       | Set to TRUE for verbose mode (optional).  |
| max.threads   | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).  |
| seed          | Random seed (optional).   |

### Details

The Gaussian model is specified using the mean  $\mu$  and the precision matrix  $Q$ . The contour map is then computed for the mean, using either the contour levels specified in `levels`, or `n.levels` contours that are placed according to the argument `type`.

A number of quality measures can be computed based based on the specified contour map and the Gaussian distribution. What should be computed is specified using the `compute` argument. For details on these quantities, see the reference below.

### Value

`contourmap` returns an object of class "excurobj" with the following elements

|          |  |
|----------|--|
| u        | Contour levels used in the contour map.                                  |
| n.levels | The number of contours used.   |
| u.e      | The values associated with the level sets $G_k$ .                        |
| G        | A vector which shows which of the level sets $G_k$ each node belongs to. |

|                         |   |
|-------------------------|---|
| map                     | Representation of the contour map with $\text{map}[i]=u.e[k]$ if $i$ is in $G_k$ .  |
| F                       | The contour map function (if computed).   |
| M                       | Contour avoiding sets (if F is computed). $M = -1$ for all non-significant nodes and $M = k$ for nodes that belong to $M_k$ . |
| P0/P1/P2                | Calculated quality measures (if computed).  |
| P0bound/P1bound/P2bound | Calculated upper bounds quality measures (if computed).   |
| meta                    | A list containing various information about the calculation.  |

**Author(s)**

David Bolin <davidbolin@gmail.com>

**References**

Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, vol 26, no 3, pp 513-524.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

**See Also**

[contourmap.inla\(\)](#), [contourmap.mc\(\)](#), [contourmap.colors\(\)](#)

**Examples**

```
n <- 10
Q <- Matrix(toeplitz(c(1, -0.5, rep(0, n - 2))))
mu <- seq(-5, 5, length = n)
lp <- contourmap(mu, Q,
  n.levels = 2,
  compute = list(F = FALSE, measures = c("P1", "P2")),
  max.threads = 1
)
# Plot the contourmap
plot(lp$map)
# Display the quality measures
cat(c(lp$P1, lp$P2))
```

---

contourmap.colors      *Define a color map for displaying contour maps.*

---

**Description**

contourmap.colors calculates suitable colours for displaying contour maps.

**Usage**

```
contourmap.colors(lp, zlim, col, credible.col)
```

**Arguments**

|              |  |
|--------------|--|
| lp           | A contourmap calculated by <code>contourmap</code> , <code>contourmap.inla</code> , or <code>contourmap.mc</code>                |
| zlim         | The range that should be used (optional). The default is the range of the mean value function used when creating the contourmap. |
| col          | The colormap that the colours should be taken from.  |
| credible.col | The color that should be used for displaying the credible regions for the contour curves (optional).                             |

**Value**

A color map.

**Author(s)**

David Bolin <davidbolin@gmail.com>

**Examples**

```
n <- 10
Q <- Matrix(toeplitz(c(1, -0.5, rep(0, n - 2))))
map <- contourmap(
  mu = seq(-5, 5, length = n), Q, n.levels = 2,
  compute = list(F = FALSE), max.threads = 1
)
cols <- contourmap.colors(map,
  col = heat.colors(100, 1),
  credible.col = grey(0.5, 1)
)
```

---

contourmap.inla

*Contour maps and contour map quality measures for latent Gaussian models*

---

**Description**

An interface to the `contourmap` function for latent Gaussian models calculated using the INLA method.

**Usage**

```

contourmap.inla(
  result.inla,
  stack,
  name = NULL,
  tag = NULL,
  method = "QC",
  n.levels,
  type = c("standard", "pretty", "equalarea"),
  compute = list(F = TRUE, measures = NULL),
  alpha,
  F.limit,
  n.iter = 10000,
  verbose = FALSE,
  max.threads = 0,
  compressed = TRUE,
  seed = NULL,
  ind,
  ...
)

```

**Arguments**

|                          |  |
|--------------------------|--|
| <code>result.inla</code> | Result object from INLA call.  |
| <code>stack</code>       | The stack object used in the INLA call.  |
| <code>name</code>        | The name of the component for which to do the calculation. This argument should only be used if a stack object is not provided, use the tag argument otherwise.  |
| <code>tag</code>         | The tag of the component in the stack for which to do the calculation. This argument should only be used if a stack object is provided, use the name argument otherwise.   |
| <code>method</code>      | Method for handling the latent Gaussian structure. Currently only Empirical Bayes (EB) and Quantile corrections (QC) are supported.  |
| <code>n.levels</code>    | Number of levels in contour map.   |
| <code>type</code>        | Type of contour map. One of:<br><b>'standard'</b> Equidistant levels between smallest and largest value of the posterior mean (default).<br><b>'pretty'</b> Equally spaced 'round' values which cover the range of the values in the posterior mean.<br><b>'equalarea'</b> Levels such that different spatial regions are approximately equal in size. |
| <code>compute</code>     | A list with quality indices to compute<br><b>'F'</b> : TRUE/FALSE indicating whether the contour map function should be computed (default TRUE)  |

|             |  |
|-------------|--|
|             | <b>'measures'</b> : A list with the quality measures to compute ("P0", "P1", "P2") or corresponding bounds based only on the marginal probabilities ("P0-bound", "P1-bound", "P2-bound")       |
| alpha       | Maximal error probability in contour map function (default=1)  |
| F.limit     | The limit value for the computation of the F function. F is set to NA for all nodes where $F < 1 - F.limit$ . Default is $F.limit = alpha$ .   |
| n.iter      | Number of iterations in the MC sampler that is used for calculating the quantities in compute. The default value is 10000.   |
| verbose     | Set to TRUE for verbose mode (optional)  |
| max.threads | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).   |
| compressed  | If INLA is run in compressed mode and a part of the linear predictor is to be used, then only add the relevant part. Otherwise the entire linear predictor is added internally (default TRUE). |
| seed        | Random seed (optional).  |
| ind         | If only a part of a component should be used in the calculations, this argument specifies the indices for that part (optional).  |
| ...         | Additional arguments to the contour map function. See the documentation for contourmap for details.  |

## Details

The INLA approximation of the quantity of interest is in general a weighted sum of Gaussian distributions with different parameters. If `method = 'EB'` is used, then the contour map is computed for the mean of the component in the weighted sum that has parameters with the highest likelihood. If on the other hand `method = 'QC'`, then the contour map is computed for the posterior mean reported by INLA. If the EB method also is used in INLA, then this reported posterior mean is equal to the mean of the component with the highest likelihood. Therefore, `method = 'EB'` is appropriate if the EB method also is used in INLA, but `method = 'QC'` should be used in general.

The `n.levels` contours in the contour map are placed according to the argument type. A number of quality measures can be computed based on the specified contour map and the distribution of the component of interest. What should be computed is specified using the `compute` argument. For details on these quantities, see the reference below.

## Value

`contourmap.inla` returns an object of class "excurobj" with the same elements as returned by `contourmap`.

## Note

This function requires the INLA package, which is not a CRAN package. See <https://www.r-inla.org/download-install> for easy installation instructions.

## Author(s)

David Bolin <davidbolin@gmail.com>

## References

Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, 26:3, 513-524.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

## See Also

[contourmap\(\)](#), [contourmap.mc\(\)](#), [contourmap.colors\(\)](#)

## Examples

```
## Not run:
if (require.nowarnings("INLA")) {
  # Generate mesh and SPDE model
  n.lattice <- 10 # increase for more interesting, but slower, examples
  x <- seq(from = 0, to = 10, length.out = n.lattice)
  lattice <- fmesher::fm_lattice_2d(x = x, y = x)
  mesh <- fmesher::fm_rcdt_2d_inla(
    lattice = lattice,
    extend = FALSE,
    refine = FALSE
  )
  spde <- inla.spde2.matern(mesh, alpha = 2)

  # Generate an artificial sample
  sigma2.e <- 0.01
  n.obs <- 100
  obs.loc <- cbind(
    runif(n.obs) * diff(range(x)) + min(x),
    runif(n.obs) * diff(range(x)) + min(x)
  )
  Q <- inla.spde2.precision(spde, theta = c(log(sqrt(0.5)), log(sqrt(1))))
  x <- inla.qsample(Q = Q, num.threads = 1)
  A <- fmesher::fm_basis(mesh = mesh, loc = obs.loc)
  Y <- as.vector(A %*% x + rnorm(n.obs) * sqrt(sigma2.e))

  ## Estimate the parameters using INLA
  mesh.index <- inla.spde.make.index(name = "field", n.spde = spde$n.spde)
  ef <- list(c(mesh.index, list(Intercept = 1)))

  s.obs <- inla.stack(
    data = list(y = Y),
    A = list(A),
    effects = ef,
    tag = "obs"
  )
  s.pre <- inla.stack(
    data = list(y = NA),
    A = list(1),
    effects = ef,
```

```

    tag = "pred"
  )
  stack <- inla.stack(s.obs, s.pre)
  formula <- y ~ -1 + Intercept + f(field, model = spde)
  result <- inla(
    formula = formula, family = "normal", data = inla.stack.data(stack),
    control.predictor = list(
      A = inla.stack.A(stack),
      compute = TRUE
    ),
    control.compute = list(
      config = TRUE,
      return.marginals.predictor = TRUE
    ),
    num.threads = 1
  )

  ## Calculate contour map with two levels
  map <- contourmap.inla(result,
    stack = stack, tag = "pred",
    n.levels = 2, alpha = 0.1, F.limit = 0.1,
    max.threads = 1
  )

  ## Plot the results
  cols <- contourmap.colors(map,
    col = heat.colors(100, 1),
    credible.col = grey(0.5, 1)
  )
  image(matrix(map$M[mesh$idx$lattice], n.lattice, n.lattice), col = cols)
}

## End(Not run)

```

---

 contourmap.mc

*Contour maps and contour map quality measures using Monte Carlo samples*

---

## Description

contourmap.mc is used for calculating contour maps and quality measures for contour maps based on Monte Carlo samples of a model.

## Usage

```

contourmap.mc(
  samples,
  n.levels,
  ind,
  levels,

```

```

type = c("standard", "equalarea", "P0-optimal", "P1-optimal", "P2-optimal"),
compute = list(F = TRUE, measures = NULL),
alpha,
verbose = FALSE
)

```

### Arguments

|          |   |
|----------|---|
| samples  | Matrix with model Monte Carlo samples. Each column contains a sample of the model.  |
| n.levels | Number of levels in contour map.  |
| ind      | Indices of the nodes that should be analyzed (optional).  |
| levels   | Levels to use in contour map.   |
| type     | Type of contour map. One of:<br><b>'standard'</b> Equidistant levels between smallest and largest value of the posterior mean (default).<br><b>'pretty'</b> Equally spaced 'round' values which cover the range of the values in the posterior mean.<br><b>'equalarea'</b> Levels such that different spatial regions are approximately equal in size.<br><b>'P0-optimal'</b> Levels chosen to maximize the P0 measure.<br><b>'P1-optimal'</b> Levels chosen to maximize the P1 measure.<br><b>'P2-optimal'</b> Levels chosen to maximize the P2 measure. |
| compute  | A list with quality indices to compute<br><b>'F'</b> : TRUE/FALSE indicating whether the contour map function should be computed (default TRUE).<br><b>'measures'</b> : A list with the quality measures to compute ("P0", "P1", "P2") or corresponding bounds based only on the marginal probabilities ("P0-bound", "P1-bound", "P2-bound").   |
| alpha    | Maximal error probability in contour map function (default=0.1).  |
| verbose  | Set to TRUE for verbose mode (optional).  |

### Details

The contour map is computed for the empirical mean of the samples. See [contourmap\(\)](#) and [contourmap.inla\(\)](#) for further details.

### Value

contourmap returns an object of class "excurobj" with the following elements

|          |  |
|----------|--|
| u        | Contour levels used in the contour map.                                  |
| n.levels | The number of contours used.   |
| u.e      | The values associated with the level sets $G_k$ .                        |
| G        | A vector which shows which of the level sets $G_k$ each node belongs to. |

|                         |   |
|-------------------------|---|
| map                     | Representation of the contour map with $\text{map}[i]=u.e[k]$ if $i$ is in $G_k$ .  |
| F                       | The contour map function (if computed).   |
| M                       | Contour avoiding sets (if F is computed). $M = -1$ for all non-significant nodes and $M = k$ for nodes that belong to $M_k$ . |
| P0/P1/P2                | Calculated quality measures (if computed).  |
| P0bound/P1bound/P2bound | Calculated upper bounds quality measures (if computed).   |
| meta                    | A list containing various information about the calculation.  |

**Author(s)**

David Bolin <davidbolin@gmail.com>

**References**

- Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, 26:3, 513-524.
- Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, 86(5), 1–20.

**See Also**

[contourmap\(\)](#), [contourmap.inla\(\)](#), [contourmap.colors\(\)](#)

**Examples**

```
n <- 100
Q <- Matrix(toeplitz(c(1, -0.5, rep(0, n - 2))))
mu <- seq(-5, 5, length = n)
## Sample the model 100 times (increase for better estimate)
X <- mu + solve(chol(Q), matrix(rnorm(n = n * 100), nrow = n, ncol = 100))

lp <- contourmap.mc(X, n.levels = 2, compute = list(F = FALSE, measures = c("P1", "P2")))

# plot contourmap
plot(lp$map)
# display quality measures
c(lp$P1, lp$P2)
```

**Description**

excursions is one of the main functions in the package with the same name. For an introduction to the package, see [excursions-package\(\)](#). The function is used for calculating excursion sets, contour credible regions, and contour avoiding sets for latent Gaussian models. Details on the function and the package are given in the sections below.

**Usage**

```

excursions(
  alpha,
  u,
  mu,
  Q,
  type,
  n.iter = 10000,
  Q.chol,
  F.limit,
  vars,
  rho,
  reo,
  method = "EB",
  ind,
  max.size,
  verbose = 0,
  max.threads = 0,
  seed,
  prune.ind = FALSE
)

```

**Arguments**

|         |   |
|---------|---|
| alpha   | Error probability for the excursion set.  |
| u       | Excursion or contour level.   |
| mu      | Expectation vector.   |
| Q       | Precision matrix.   |
| type    | Type of region:<br>'>' positive excursion region<br>'<' negative excursion region<br>'!=' contour avoiding region<br>'=' contour credibility region |
| n.iter  | Number of iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.                                    |
| Q.chol  | The Cholesky factor of the precision matrix (optional).   |
| F.limit | The limit value for the computation of the F function. F is set to NA for all nodes where $F < 1 - F.limit$ . Default is $F.limit = \alpha$ .       |
| vars    | Precomputed marginal variances (optional).  |
| rho     | Marginal excursion probabilities (optional). For contour regions, provide $P(X > u)$ .  |
| reo     | Reordering (optional).  |
| method  | Method for handling the latent Gaussian structure:<br>'EB' Empirical Bayes (default)  |

|             |  |
|-------------|--|
|             | 'QC' Quantile correction, rho must be provided if QC is used.  |
| ind         | Indices of the nodes that should be analysed (optional).   |
| max.size    | Maximum number of nodes to include in the set of interest (optional).  |
| verbose     | Set to TRUE for verbose mode (optional).   |
| max.threads | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default). |
| seed        | Random seed (optional).  |
| prune.ind   | If TRUE and ind is supplied, then the result object is pruned to contain only the active nodes specified by ind.                     |

### Details

The estimation of the region is done using sequential importance sampling with `n.iter` samples. The procedure requires computing the marginal variances of the field, which should be supplied if available. If not, they are computed using the Cholesky factor of the precision matrix. The cost of this step can therefore be reduced by supplying the Cholesky factor if it is available.

The latent structure in the latent Gaussian model can be handled in several different ways. The default strategy is the EB method, which is exact for problems with Gaussian posterior distributions. For problems with non-Gaussian posteriors, the QC method can be used for improved results. In order to use the QC method, the true marginal excursion probabilities must be supplied using the argument `rho`. Other more complicated methods for handling non-Gaussian posteriors must be implemented manually unless INLA is used to fit the model. If the model is fitted using INLA, the method `excursions.inla` can be used. See the Package section for further details about the different options.

### Value

`excursions` returns an object of class "excurobj" with the following elements

|      |   |
|------|---|
| E    | Excursion set, contour credible region, or contour avoiding set   |
| G    | Contour map set. $G = 1$ for all nodes where the $\mu > u$ .  |
| M    | Contour avoiding set. $M = -1$ for all non-significant nodes. $M = 0$ for nodes where the process is significantly below $u$ and $M = 1$ for all nodes where the field is significantly above $u$ . Which values that should be present depends on what type of set that is calculated. |
| F    | The excursion function corresponding to the set E calculated or values up to <code>F.limit</code>   |
| rho  | Marginal excursion probabilities  |
| mean | The mean $\mu$ .  |
| vars | Marginal variances.   |
| meta | A list containing various information about the calculation.  |

### Author(s)

David Bolin <davidbolin@gmail.com> and Finn Lindgren <finn.lindgren@gmail.com>

## References

Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

## See Also

[excursions-package\(\)](#), [excursions.inla\(\)](#), [excursions.mc\(\)](#)

## Examples

```
## Create a tridiagonal precision matrix
n <- 21
Q.x <- sparseMatrix(
  i = c(1:n, 2:n), j = c(1:n, 1:(n - 1)), x = c(rep(1, n), rep(-0.1, n - 1)),
  dims = c(n, n), symmetric = TRUE
)
## Set the mean value function
mu.x <- seq(-5, 5, length = n)

## calculate the level 0 positive excursion function
res.x <- excursions(
  alpha = 1, u = 0, mu = mu.x, Q = Q.x,
  type = ">", verbose = 1, max.threads = 2
)

## Plot the excursion function and the marginal excursion probabilities
plot(res.x$F,
  type = "l",
  main = "Excursion function (black) and marginal probabilities (red)"
)
lines(res.x$rho, col = 2)
```

---

|                 |   |
|-----------------|---|
| excursions.inla | <i>Excursion sets and contour credible regions for latent Gaussian models</i> |
|-----------------|---|

---

## Description

Excursion sets and contour credible regions for latent Gaussian models calculated using the INLA method.

## Usage

```
excursions.inla(
  result.inla,
  stack,
```

```

name = NULL,
tag = NULL,
ind = NULL,
method,
alpha = 1,
F.limit,
u,
u.link = FALSE,
type,
n.iter = 10000,
verbose = 0,
max.threads = 0,
compressed = TRUE,
seed = NULL,
prune.ind = FALSE
)

```

### Arguments

|                          |   |
|--------------------------|---|
| <code>result.inla</code> | Result object from INLA call.   |
| <code>stack</code>       | The stack object used in the INLA call.   |
| <code>name</code>        | The name of the component for which to do the calculation. This argument should only be used if a stack object is not provided, use the tag argument otherwise.   |
| <code>tag</code>         | The tag of the component in the stack for which to do the calculation. This argument should only be used if a stack object is provided, use the name argument otherwise.  |
| <code>ind</code>         | If only a part of a component should be used in the calculations, this argument specifies the indices for that part.  |
| <code>method</code>      | Method for handling the latent Gaussian structure:<br><b>'EB'</b> Empirical Bayes<br><b>'QC'</b> Quantile correction<br><b>'NI'</b> Numerical integration<br><b>'NIQC'</b> Numerical integration with quantile correction<br><b>'iNIQC'</b> Improved integration with quantile correction |
| <code>alpha</code>       | Error probability for the excursion set of interest. The default value is 1.  |
| <code>F.limit</code>     | Error probability for when to stop the calculation of the excursion function. The default value is <code>alpha</code> , and the value cannot be smaller than <code>alpha</code> . A smaller value of <code>F.limit</code> results in a smaller computation time.                          |
| <code>u</code>           | Excursion or contour level.   |
| <code>u.link</code>      | If <code>u.link</code> is <code>TRUE</code> , <code>u</code> is assumed to be in the scale of the data and is then transformed to the scale of the linear predictor (default <code>FALSE</code> ).  |
| <code>type</code>        | Type of region:<br><b>'&gt;'</b> positive excursions  |

|             |      |  |
|-------------|------|--|
|             | '<'  | negative excursions  |
|             | '!=' | contour avoiding function  |
|             | '='  | contour credibility function   |
| n.iter      |      | Number of iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.   |
| verbose     |      | Set to TRUE for verbose mode (optional).   |
| max.threads |      | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).   |
| compressed  |      | If INLA is run in compressed mode and a part of the linear predictor is to be used, then only add the relevant part. Otherwise the entire linear predictor is added internally (default TRUE). |
| seed        |      | Random seed (optional).  |
| prune.ind   |      | If TRUE and ind is supplied, then the result object is pruned to contain only the active nodes specified by ind.   |

## Details

The different methods for handling the latent Gaussian structure are listed in order of accuracy and computational cost. The EB method is the simplest and is based on a Gaussian approximation of the posterior of the quantity of interest. The QC method uses the same Gaussian approximation but improves the accuracy by modifying the limits in the integrals that are computed in order to find the region. The other three methods are intended for Bayesian models where the posterior distribution for the quantity of interest is obtained by integrating over the parameters in the model. The NI method approximates this integration in the same way as is done in INLA, and the NIQC and iNIQC methods combine this approximation with the QC method for improved accuracy.

If the main purpose of the analysis is to construct excursion or contour sets for low values of  $\alpha$ , we recommend using QC for problems with Gaussian likelihoods and NIQC for problems with non-Gaussian likelihoods. The reason for this is that the more accurate methods also have higher computational costs.

## Value

excursions.inla returns an object of class "excurobj" with the following elements

|      |   |
|------|---|
| E    | Excursion set, contour credible region, or contour avoiding set   |
| F    | The excursion function corresponding to the set E calculated for values up to F.limit   |
| G    | Contour map set. $G = 1$ for all nodes where the $\mu > u$ .  |
| M    | Contour avoiding set. $M = -1$ for all non-significant nodes. $M = 0$ for nodes where the process is significantly below $u$ and $M = 1$ for all nodes where the field is significantly above $u$ . Which values that should be present depends on what type of set that is calculated. |
| rho  | Marginal excursion probabilities  |
| mean | Posterior mean  |
| vars | Marginal variances  |
| meta | A list containing various information about the calculation.  |

**Note**

This function requires the INLA package, which is not a CRAN package. See <https://www.r-inla.org/download-install> for easy installation instructions.

**Author(s)**

David Bolin <davidbolin@gmail.com> and Finn Lindgren <finn.lindgren@gmail.com>

**References**

Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

**See Also**

[excursions\(\)](#), [excursions.mc\(\)](#)

**Examples**

```
## In this example, we calculate the excursion function
## for a partially observed AR process.
## Not run:
if (require.nowarnings("INLA")) {
  ## Sample the process:
  rho <- 0.9
  tau <- 15
  tau.e <- 1
  n <- 100
  x <- 1:n
  mu <- 10 * ((x < n / 2) * (x - n / 2) + (x >= n / 2) * (n / 2 - x) + n / 4) / n
  Q <- tau * sparseMatrix(
    i = c(1:n, 2:n), j = c(1:n, 1:(n - 1)),
    x = c(1, rep(1 + rho^2, n - 2), 1, rep(-rho, n - 1)),
    dims = c(n, n), symmetric = TRUE
  )
  X <- mu + solve(chol(Q), rnorm(n))

  ## measure the sampled process at n.obs random locations
  ## under Gaussian measurement noise.
  n.obs <- 50
  obs.loc <- sample(1:n, n.obs)
  A <- sparseMatrix(
    i = 1:n.obs, j = obs.loc, x = rep(1, n.obs),
    dims = c(n.obs, n)
  )
  Y <- as.vector(A %*% X + rnorm(n.obs) / sqrt(tau.e))

  ## Estimate the parameters using INLA
  ef <- list(c(list(ar = x), list(cov = mu)))
```

```

s.obs <- inla.stack(data = list(y = Y), A = list(A), effects = ef, tag = "obs")
s.pre <- inla.stack(data = list(y = NA), A = list(1), effects = ef, tag = "pred")
stack <- inla.stack(s.obs, s.pre)
formula <- y ~ -1 + cov + f(ar, model = "ar1")
result <- inla(
  formula = formula, family = "normal", data = inla.stack.data(stack),
  control.predictor = list(A = inla.stack.A(stack), compute = TRUE),
  control.compute = list(
    config = TRUE,
    return.marginals.predictor = TRUE
  )
)

## calculate the level 0 positive excursion function
res.qc <- excursions.inla(result,
  stack = stack, tag = "pred", alpha = 0.99, u = 0,
  method = "QC", type = ">", max.threads = 2
)
## plot the excursion function and marginal probabilities
plot(res.qc$rho,
  type = "l",
  main = "marginal probabilities (black) and excursion function (red)"
)
lines(res.qc$F, col = 2)
}

## End(Not run)

```

---

excursions.mc

*Excursion sets and contour credible regions using Monte Carlo samples*


---

## Description

excursions.mc is used for calculating excursion sets, contour credible regions, and contour avoiding sets based on Monte Carlo samples of models.

## Usage

```

excursions.mc(
  samples,
  alpha,
  u,
  type,
  rho,
  reo,
  ind,
  max.size,

```

```

    verbose = FALSE,
    prune.ind = FALSE
  )

```

### Arguments

|           |   |
|-----------|---|
| samples   | Matrix with model Monte Carlo samples. Each column contains a sample of the model.  |
| alpha     | Error probability for the excursion set.  |
| u         | Excursion or contour level.   |
| type      | Type of region:<br>'>' positive excursions<br>'<' negative excursions<br>'!=' contour avoiding function<br>'=' contour credibility function |
| rho       | Marginal excursion probabilities (optional). For contour regions, provide $P(X > u)$ .  |
| reo       | Reordering (optional).  |
| ind       | Indices of the nodes that should be analysed (optional).  |
| max.size  | Maximum number of nodes to include in the set of interest (optional).   |
| verbose   | Set to TRUE for verbose mode (optional).  |
| prune.ind | If TRUE and ind is supplied, then the result object is pruned to contain only the active nodes specified by ind.                            |

### Value

excursions.mc returns an object of class "excurobj" with the following elements

|      |   |
|------|---|
| E    | Excursion set, contour credible region, or contour avoiding set.  |
| G    | Contour map set. $G = 1$ for all nodes where the $\mu u > u$ .  |
| M    | Contour avoiding set. $M = -1$ for all non-significant nodes. $M = 0$ for nodes where the process is significantly below $u$ and $M = 1$ for all nodes where the field is significantly above $u$ . Which values that should be present depends on what type of set that is calculated. |
| F    | The excursion function corresponding to the set E calculated for values up to <code>F.limit</code>  |
| rho  | Marginal excursion probabilities  |
| mean | The mean $\mu$ .  |
| vars | Marginal variances.   |
| meta | A list containing various information about the calculation.  |

### Author(s)

David Bolin <davidbolin@gmail.com> and Finn Lindgren <finn.lindgren@gmail.com>

## References

Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

## See Also

[excursions\(\)](#), [excursions.inla\(\)](#)

## Examples

```
## Create mean and a tridiagonal precision matrix
n <- 101
mu.x <- seq(-5, 5, length = n)
Q.x <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
## Sample the model 100 times (increase for better estimate)
X <- mu.x + solve(chol(Q.x), matrix(rnorm(n = n * 1000), nrow = n, ncol = 1000))
## calculate the positive excursion function
res.x <- excursions.mc(X, alpha = 0.05, type = ">", u = 0)
## Plot the excursion function and the marginal excursion probabilities
plot(res.x$F,
      type = "l",
      main = "Excursion function (black) and marginal probabilities (red)"
)
lines(res.x$rho, col = 2)
```

---

`excursions.variances` *Calculate variances from a sparse precision matrix*

---

## Description

`excursions.variances` calculates the diagonal of the inverse of a sparse symmetric positive definite matrix  $Q$ .

## Usage

```
excursions.variances(L, Q, max.threads = 0)
```

## Arguments

|                          |  |
|--------------------------|--|
| <code>L</code>           | Cholesky factor of precision matrix.   |
| <code>Q</code>           | Precision matrix.  |
| <code>max.threads</code> | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default). |

**Details**

The method for calculating the diagonal requires the Cholesky factor,  $L$ , of  $Q$ , which should be supplied if available. If  $Q$  is provided, the cholesky factor is calculated and the variances are then returned in the same ordering as  $Q$ . If  $L$  is provided, the variances are returned in the same ordering as  $L$ , even if  $L@invpivot$  exists.

**Value**

A vector with the variances.

**Author(s)**

David Bolin <davidbolin@gmail.com>

**Examples**

```
## Create a tridiagonal precision matrix
n <- 21
Q <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
v2 <- excursions.variances(Q = Q, max.threads = 2)
## var2 should be the same as:
v1 <- diag(solve(Q))
```

---

exc\_safe\_inla

*Load INLA safely for examples and tests*


---

**Description**

Loads the INLA package with `requireNamespace("INLA", quietly = TRUE)`, and optionally checks and sets the multicore `num.threads` INLA option.

**Usage**

```
exc_safe_inla(multicore = NULL, quietly = FALSE)
```

**Arguments**

|           |  |
|-----------|--|
| multicore | logical; if TRUE, multiple cores are allowed, and the INLA <code>num.threads</code> option is not checked or altered. If FALSE, forces <code>num.threads="1:1"</code> . Default: NULL, checks if running in testthat or non-interactively, in which case sets <code>multicore=FALSE</code> , otherwise TRUE. |
| quietly   | logical; if TRUE, prints diagnostic messages. Default: FALSE.  |

**Value**

logical; TRUE if INLA was loaded safely, otherwise FALSE

**Examples**

```
## Not run:
if (exc_safe_inla()) {
  # Run inla dependent calculations
}

## End(Not run)
```

gaussint

*Sequential estimation of Gaussian integrals***Description**

gaussint is used for calculating  $n$ -dimensional Gaussian integrals

$$\int_a^b \frac{|Q|^{1/2}}{(2\pi)^{n/2}} \exp\left(-\frac{1}{2}(x - \mu)^T Q (x - \mu)\right) dx$$

A limit value *lim* can be used to stop the integration if the sequential estimate goes below the limit, which can result in substantial computational savings in cases when one only is interested in testing if the integral is above the limit value. The integral is calculated sequentially, and estimates for all subintegrals are also returned.

**Usage**

```
gaussint(
  mu,
  Q.chol,
  Q,
  a,
  b,
  lim = 0,
  n.iter = 10000,
  ind,
  use.reordering = c("natural", "sparsity", "limits"),
  max.size,
  max.threads = 0,
  seed
)
```

**Arguments**

|        |  |
|--------|--|
| mu     | Expectation vector for the Gaussian distribution.  |
| Q.chol | The Cholesky factor of the precision matrix (optional).  |
| Q      | Precision matrix for the Gaussian distribution. If Q is supplied but not Q.chol, the cholesky factor is computed before integrating. |

|                             |  |
|-----------------------------|--|
| <code>a</code>              | Lower limit in integral.   |
| <code>b</code>              | Upper limit in integral.   |
| <code>lim</code>            | If this argument is used, the integration is stopped and 0 is returned if the estimated value goes below <code>lim</code> .  |
| <code>n.iter</code>         | Number of iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.   |
| <code>ind</code>            | Indices of the nodes that should be analyzed (optional).   |
| <code>use.reordering</code> | Determines what reordering to use:<br><b>"natural"</b> No reordering is performed.<br><b>"sparsity"</b> Reorder for sparsity in the cholesky factor (MMD reordering is used).<br><b>"limits"</b> Reorder by moving all nodes with <code>a=-Inf</code> and <code>b=Inf</code> first and then reordering for sparsity (CAMD reordering is used). |
| <code>max.size</code>       | The largest number of sub-integrals to compute. Default is the total dimension of the distribution.  |
| <code>max.threads</code>    | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).   |
| <code>seed</code>           | The random seed to use (optional).   |

### Details

The function uses sequential importance sampling to estimate the Gaussian integral, and returns all computed sub-integrals. This means that if, for example, the function is used to compute  $P(x > 0)$  for an  $n$ -dimensional Gaussian variable  $x$ , then all integrals  $P(x_1 > 0, \dots, x_i > 0)$  for  $i = 1, \dots, n$  are computed.

If one is only interested in whether  $P(x > 0) > \alpha$  or not, then one can stop the integration as soon as  $P(x_1 > 0, \dots, x_i > 0) < \alpha$ . This can save a lot of computation time if  $P(x_1 > 0, \dots, x_i > 0) < \alpha$  for  $i$  much smaller than  $n$ . This limit value is specified by the `lim` argument.

Which reordering to use depends on what the purpose of the calculation is and what the integration limits are. However, in general the `limits` reordering is typically most appropriate since this combines sparsity (which improves accuracy and reduces computational cost) with automatic handling of dimensions with limits `a=-Inf` and `b=Inf`, which do not affect the probability but affect the computation time if they are not handled separately.

### Value

A list with elements

|                 |  |
|-----------------|--|
| <code>P</code>  | Value of the integral.   |
| <code>E</code>  | Estimated error of the <code>P</code> estimate.                      |
| <code>Pv</code> | A vector with the estimates of all sub-integrals.                    |
| <code>Ev</code> | A vector with the estimated errors of the <code>Pv</code> estimates. |

### Author(s)

David Bolin <davidbolin@gmail.com>

## References

Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

## Examples

```
## Create mean and a tridiagonal precision matrix
n <- 11
mu.x <- seq(-5, 5, length = n)
Q.x <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
## Calculate the probability that the variable is between mu-3 and mu+3
prob <- gaussint(mu = mu.x, Q = Q.x, a = mu.x - 3, b = mu.x + 3, max.threads = 2)
prob$P
```

---

require.nowarnings      *Warnings free loading of add-on packages*

---

## Description

Turn off all warnings for require(), to allow clean completion of examples that require unavailable Suggested packages.

## Usage

```
require.nowarnings(package, lib.loc = NULL, character.only = FALSE)
```

## Arguments

|                |   |
|----------------|---|
| package        | The name of a package, given as a character string.   |
| lib.loc        | a character vector describing the location of R library trees to search through, or NULL. The default value of NULL corresponds to all libraries currently known to .libPaths(). Non-existent library trees are silently ignored. |
| character.only | a logical indicating whether package can be assumed to be a character string.   |

## Details

require(package) acts the same as require(package, quietly = TRUE) but with warnings turned off. In particular, no warning or error is given if the package is unavailable. Most cases should use requireNamespace(package, quietly = TRUE) instead, which doesn't produce warnings.

## Value

require.nowarnings returns (invisibly) TRUE if it succeeds, otherwise FALSE

**See Also**[require\(\)](#)**Examples**

```
## This should produce no output:
if (require.nowarnings(nonexistent)) {
  message("Package loaded successfully")
}
```

simconf

*Simultaneous confidence regions for Gaussian models***Description**

simconf is used for calculating simultaneous confidence regions for Gaussian models  $x$ . The function returns upper and lower bounds  $a$  and  $b$  such that  $P(a < x < b) = 1 - \alpha$ .

**Usage**

```
simconf(
  alpha,
  mu,
  Q,
  n.iter = 10000,
  Q.chol,
  vars,
  ind = NULL,
  verbose = 0,
  max.threads = 0,
  seed = NULL
)
```

**Arguments**

|             |  |
|-------------|--|
| alpha       | Error probability for the region.  |
| mu          | Expectation vector for the Gaussian distribution.  |
| Q           | Precision matrix for the Gaussian distribution.  |
| n.iter      | Number of iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.                     |
| Q.chol      | The Cholesky factor of the precision matrix (optional).  |
| vars        | Precomputed marginal variances (optional).   |
| ind         | Indices of the nodes that should be analyzed (optional).   |
| verbose     | Set to TRUE for verbose mode (optional).   |
| max.threads | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default). |
| seed        | Random seed (optional).  |

## Details

The pointwise confidence bands are based on the marginal quantiles, meaning that `a.marginal` is a vector where the  $i$ th element equals  $\mu_i + q_{\alpha,i}$  and `b.marginal` is a vector where the  $i$ th element equals  $\mu_i + q_{1-\alpha,i}$ , where  $\mu_i$  is the expected value of the  $x_i$  and  $q_{\alpha,i}$  is the  $\alpha$ -quantile of  $x_i - \mu_i$ .

The simultaneous confidence band is defined by the lower limit vector `a` and the upper limit vector `b`, where  $a_i = \mu_i + cq_{\alpha}$  and  $b_i = \mu_i + cq_{1-\alpha}$ , where  $c$  is a constant computed such that  $P(a < x < b) = 1 - \alpha$ .

## Value

An object of class "excurobj" with elements

|                         |   |
|-------------------------|---|
| <code>a</code>          | The lower bound.                                |
| <code>b</code>          | The upper bound.                                |
| <code>a.marginal</code> | The lower bound for pointwise confidence bands. |
| <code>b.marginal</code> | The upper bound for pointwise confidence bands. |

## Author(s)

David Bolin <davidbolin@gmail.com> and Finn Lindgren <finn.lindgren@gmail.com>

## References

Bolin et al. (2015) *Statistical prediction of global sea level from global temperature*, *Statistica Sinica*, vol 25, pp 351-367.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, *Journal of Statistical Software*, vol 86, no 1, pp 1-20.

## See Also

[simconf.inla\(\)](#), [simconf.mc\(\)](#), [simconf.mixture\(\)](#)

## Examples

```
## Create mean and a tridiagonal precision matrix
n <- 11
mu.x <- seq(-5, 5, length = n)
Q.x <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
## calculate the confidence region
conf <- simconf(0.05, mu.x, Q.x, max.threads = 2)
## Plot the region
plot(mu.x,
     type = "l", ylim = c(-10, 10),
     main = "Mean (black) and confidence region (red)"
)
lines(conf$a, col = 2)
lines(conf$b, col = 2)
```

simconf.inla

*Simultaneous confidence regions for latent Gaussian models***Description**

simconf.inla is used for calculating simultaneous confidence regions for latent Gaussian models estimated using INLA.

**Usage**

```
simconf.inla(
  result.inla,
  stack,
  name = NULL,
  tag = NULL,
  ind = NULL,
  alpha,
  method = "NI",
  n.iter = 10000,
  verbose = FALSE,
  link = FALSE,
  max.threads = 0,
  compressed = TRUE,
  seed = NULL,
  inla.sample = TRUE
)
```

**Arguments**

|             |  |
|-------------|--|
| result.inla | Result object from INLA call.  |
| stack       | The stack object used in the INLA call.  |
| name        | The name of the component for which to do the calculation. This argument should only be used if a stack object is not provided, use the tag argument otherwise.  |
| tag         | The tag of the component in the stack for which to do the calculation. This argument should only be used if a stack object is provided, use the name argument otherwise.   |
| ind         | If only a part of a component should be used in the calculations, this argument specifies the indices for that part.   |
| alpha       | Error probability for the region.  |
| method      | Method for handling the latent Gaussian structure:<br><b>'EB'</b> Empirical Bayes (Gaussian approximation of posterior).<br><b>'NI'</b> Numerical integration (Calculation based on the Gaussian mixture approximation of the posterior, as calculated by INLA). |

|             |  |
|-------------|--|
| n.iter      | Number of iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.   |
| verbose     | Set to TRUE for verbose mode (optional).   |
| link        | Transform output to the scale of the data using the link function as defined in the model estimated with INLA (default FALSE).   |
| max.threads | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).   |
| compressed  | If INLA is run in compressed mode and a part of the linear predictor is to be used, then only add the relevant part. Otherwise the entire linear predictor is added internally (default TRUE). |
| seed        | Random seed (optional).  |
| inla.sample | Set to TRUE if inla.posterior.sample should be used for the MC integration.  |

### Details

See `simconf()` for details.

### Value

An object of class "excurobj" with elements

|            |   |
|------------|---|
| a          | The lower bound.                                |
| b          | The upper bound.                                |
| a.marginal | The lower bound for pointwise confidence bands. |
| b.marginal | The upper bound for pointwise confidence bands. |

### Note

This function requires the INLA package, which is not a CRAN package. See <https://www.r-inla.org/download-install> for easy installation instructions.

### Author(s)

David Bolin <davidbolin@gmail.com>

### References

Bolin et al. (2015) *Statistical prediction of global sea level from global temperature*, *Statistica Sinica*, vol 25, pp 351-367.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, *Journal of Statistical Software*, vol 86, no 1, pp 1-20.

### See Also

`simconf()`, `simconf.mc()`, `simconf.mixture()`

**Examples**

```

## Not run:
if (require.nowarnings("INLA")) {
  n <- 10
  x <- seq(0, 6, length.out = n)
  y <- sin(x) + rnorm(n)
  mu <- 1:n
  result <- inla(y ~ 1 + f(mu, model = "rw2"),
    data = list(y = y, mu = mu), verbose = FALSE,
    control.compute = list(
      config = TRUE,
      return.marginals.predictor = TRUE
    ),
    num.threads = "1:1"
  )

  res <- simconf.inla(
    result,
    name = "mu", alpha = 0.05,
    max.threads = 1, num.threads = "1:1"
  )

  plot(result$summary.random$mu$mean, ylim = c(-2, 2))
  lines(res$a)
  lines(res$b)
  lines(res$a.marginal, col = "2")
  lines(res$b.marginal, col = "2")
}

## End(Not run)

```

---

simconf.mc

*Simultaneous confidence regions using Monte Carlo samples*


---

**Description**

simconf.mc is used for calculating simultaneous confidence regions based on Monte Carlo samples. The function returns upper and lower bounds  $a$  and  $b$  such that  $P(a < x < b) = 1 - \alpha$ .

**Usage**

```
simconf.mc(samples, alpha, ind, verbose = FALSE)
```

**Arguments**

|         |  |
|---------|--|
| samples | Matrix with model Monte Carlo samples. Each column contains a sample of the model. |
| alpha   | Error probability for the region.  |

ind                   Indices of the nodes that should be analyzed (optional).  
 verbose               Set to TRUE for verbose mode (optional).

### Details

See [simconf\(\)](#) for details.

### Value

An object of class "excurobj" with elements

a                    The lower bound.  
 b                    The upper bound.  
 a.marginal          The lower bound for pointwise confidence bands.  
 b.marginal          The upper bound for pointwise confidence bands.

### Author(s)

David Bolin <davidbolin@gmail.com>

### See Also

[simconf\(\)](#), [simconf.inla\(\)](#)

### Examples

```
## Create mean and a tridiagonal precision matrix
n <- 11
mu.x <- seq(-5, 5, length = n)
Q.x <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
## Sample the model 100 times (increase for better estimate)
X <- mu.x + solve(chol(Q.x), matrix(rnorm(n = n * 100), nrow = n, ncol = 100))
## calculate the confidence region
conf <- simconf.mc(X, 0.2)
## Plot the region
plot(mu.x,
     type = "l", ylim = c(-10, 10),
     main = "Mean (black) and confidence region (red)"
)
lines(conf$a, col = 2)
lines(conf$b, col = 2)
```

simconf.mixture

*Simultaneous confidence regions for Gaussian mixture models***Description**

simconf.mixture is used for calculating simultaneous confidence regions for Gaussian mixture models. The distribution for the process  $x$  is assumed to be

$$\pi(x) = \sum_{k=1}^K w_k N(\mu_k, Q_k^{-1}).$$

The function returns upper and lower bounds  $a$  and  $b$  such that  $P(a < x < b) = 1 - \alpha$ .

**Usage**

```
simconf.mixture(
  alpha,
  mu,
  Q,
  w,
  ind,
  n.iter = 10000,
  vars,
  verbose = FALSE,
  max.threads = 0,
  seed = NULL,
  mix.samp = TRUE
)
```

**Arguments**

|             |  |
|-------------|--|
| alpha       | Error probability for the region.  |
| mu          | A list with the $k$ expectation vectors $\mu_k$ .  |
| Q           | A list with the $k$ precision matrices $Q_k$ .   |
| w           | A vector with the weights for each class in the mixture.   |
| ind         | Indices of the nodes that should be analyzed (optional).   |
| n.iter      | Number of iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.                     |
| vars        | A list with precomputed marginal variances for each class (optional).  |
| verbose     | Set to TRUE for verbose mode (optional).   |
| max.threads | Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default). |
| seed        | Random seed (optional).  |
| mix.samp    | If TRUE, the MC integration is done by directly sampling the mixture, otherwise sequential integration is used.                      |

**Details**

See [simconf\(\)](#) for details.

**Value**

An object of class "excurobj" with elements

|            |   |
|------------|---|
| a          | The lower bound.                                |
| b          | The upper bound.                                |
| a.marginal | The lower bound for pointwise confidence bands. |
| b.marginal | The upper bound for pointwise confidence bands. |

**Author(s)**

David Bolin <davidbolin@gmail.com>

**References**

Bolin et al. (2015) *Statistical prediction of global sea level from global temperature*, *Statistica Sinica*, vol 25, pp 351-367.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, *Journal of Statistical Software*, vol 86, no 1, pp 1-20.

**See Also**

[simconf\(\)](#), [simconf.inla\(\)](#), [simconf.mc\(\)](#)

**Examples**

```
n <- 11
K <- 3
mu <- Q <- list()
for (k in 1:K) {
  mu[[k]] <- k * 0.1 + seq(-5, 5, length = n)
  Q[[k]] <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
}
## calculate the confidence region
conf <- simconf.mixture(0.05, mu, Q, w = rep(1 / 3, 3), max.threads = 2)

## Plot the region
plot(mu[[1]], type = "l")
lines(mu[[2]])
lines(mu[[3]])
lines(conf$a, col = 2)
lines(conf$b, col = 2)
```

---

submesh.grid                      *Extract a part of a grid*

---

### Description

Extracts a part of a grid.

### Usage

```
submesh.grid(z, grid = NULL)
```

### Arguments

**z**                      A matrix with values indicating which nodes that should be present in the sub-mesh.

**grid**                    A list with locations and dimensions of the grid.

### Value

An fm\_mesh\_2d object.

### Author(s)

Finn Lindgren <finn.lindgren@gmail.com>

### Examples

```
## Not run:
if (require("fmesher")) {
  nxy <- 40
  x <- seq(from = 0, to = 4, length.out = nxy)
  lattice <- fm_lattice_2d(x = x, y = x)
  mesh <- fm_rcdt_2d_inla(lattice = lattice, extend = FALSE, refine = FALSE)

  # extract a part of the mesh inside a circle
  xy.in <- rowSums((mesh$loc[, 1:2] - 2)^2) < 1
  submesh <- submesh.grid(
    matrix(xy.in, nxy, nxy),
    list(loc = mesh$loc, dim = c(nxy, nxy))
  )
  plot(mesh$loc[, 1:2])
  lines(2 + cos(seq(0, 2 * pi, length.out = 100)), 2 + sin(seq(0, 2 * pi, length.out = 100)))
  plot(submesh, add = TRUE)
  points(mesh$loc[xy.in, 1:2], col = "2")
}

## End(Not run)
```

---

|              |                                 |
|--------------|---------------------------------|
| submesh.mesh | <i>Extract a part of a mesh</i> |
|--------------|---------------------------------|

---

**Description**

Extracts a part of a mesh

**Usage**

```
submesh.mesh(z, mesh)
```

**Arguments**

|      |   |
|------|---|
| z    | A matrix with values indicating which nodes that should be present in the sub-mesh. |
| mesh | An fm_mesh_2d object.   |

**Value**

An fm\_mesh\_2d object.

**Author(s)**

Finn Lindgren <finn.lindgren@gmail.com>

**Examples**

```
## Not run:
if (require(fmesher)) {
  nxy <- 30
  x <- seq(from = 0, to = 4, length.out = nxy)
  lattice <- fm_lattice_2d(x = x, y = x)
  mesh <- fm_rcdt_2d_inla(lattice = lattice, extend = FALSE, refine = FALSE)

  # extract a part of the mesh inside a circle
  xy.in <- rowSums((mesh$loc[, 1:2] - 2)^2) < 1
  submesh <- submesh.mesh(matrix(xy.in, nxy, nxy), mesh)
  plot(mesh$loc[, 1:2], pch = 20)
  lines(2 + cos(seq(0, 2 * pi, length.out = 100)), 2 + sin(seq(0, 2 * pi, length.out = 100)))
  plot(submesh, add = TRUE)
  points(mesh$loc[xy.in, 1:2], col = "2")
}

## End(Not run)
```

---

summary.excurobj      *Summarise excurobj objects*

---

### Description

Summary method for class "excurobj"

### Usage

```
## S3 method for class 'excurobj'
summary(object, ...)

## S3 method for class 'summary.excurobj'
print(x, ...)

## S3 method for class 'excurobj'
print(x, ...)
```

### Arguments

object      an object of class "excurobj", usually, a result of a call to [excursions\(\)](#).  
 ...      further arguments passed to or from other methods.  
 x      an object of class "summary.excurobj", usually, a result of a call to [summary.excurobj\(\)](#).

---

tricontour      *Calculate contour curves on a triangulation*

---

### Description

Calculates contour curves and/or regions between them, for functions defined on a triangulation

### Usage

```
tricontour(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  ...
)

## S3 method for class 'fm_mesh_2d'
tricontour(
  x,
  z,
```

```
    nlevels = 10,
    levels = pretty(range(z, na.rm = TRUE), nlevels),
    ...
)

## S3 method for class 'matrix'
tricontour(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  loc,
  ...
)

## S3 method for class 'list'
tricontour(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  loc,
  type = c("+", "-"),
  tol = 1e-07,
  ...
)

tricontourmap(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  ...
)

## S3 method for class 'fm_mesh_2d'
tricontourmap(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  ...
)

## S3 method for class 'matrix'
tricontourmap(
  x,
  z,
```

```

    nlevels = 10,
    levels = pretty(range(z, na.rm = TRUE), nlevels),
    loc,
    ...
)

## S3 method for class 'list'
tricontourmap(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  loc,
  type = c("+", "-"),
  tol = 1e-07,
  output = c("sp", "fm", "inla.mesh.segment"),
  ...
)

```

### Arguments

|         |  |
|---------|--|
| x       | An object generated by a call to <code>fm_mesh_2d</code> or <code>fm_rcdt_2d</code> , a triangle-vertex index matrix, or a list of triangulation information, <code>list(loc, graph=list(tv))</code> . |
| z       | A vector containing the values to be contoured (NAs are allowed).  |
| nlevels | Number of contour levels desired, if and only if <code>levels</code> is not supplied.  |
| levels  | Numeric vector of levels at which to calculate contour lines.  |
| ...     | Additional arguments passed to the other methods.  |
| loc     | coordinate matrix, to be supplied when <code>x</code> is given as a triangle-vertex index matrix only.   |
| type    | "+" or "-", indicating positive or negative association. For +, the generated contours enclose regions where $u_1 \leq z < u_2$ , for - the regions fulfil $u_1 < z \leq u_2$ .                        |
| tol     | tolerance for determining if the value at a vertex lies on a level.  |
| output  | The format of the generated output. Implemented options are "sp" (default) and "fm" (and deprecated "inla.mesh.segment", converted to "fm").   |

### Value

For `tricontour`, a list with some of the fields that `fm_seg` objects have:

|     |   |
|-----|---|
| loc | A coordinate matrix   |
| idx | Contour segment indices, as a 2-column matrix, each row indexing a single segment   |
| grp | A vector of group labels. Each segment has a label, in $1, \dots, nlevels*2+1$ , where even labels indicate interior on-level contour segments, and odd labels indicate boundary segments between levels. |

For `tricontourmap`, a list:

|                      |   |
|----------------------|---|
| <code>contour</code> | A list of <code>sp</code> or <code>fm_seg</code> objects defining contour curves (level sets) |
| <code>map</code>     | A list of <code>sp</code> or <code>fm_seg</code> objects enclosing regions between level sets |

### Author(s)

Finn Lindgren <finn.lindgren@gmail.com>

### Examples

```
## Not run:
if (require("fmesher") &&
    require("sp")) {
  ## Generate mesh and SPDE model
  n.lattice <- 20 # increase for more interesting, but slower, examples
  x <- seq(from = 0, to = 10, length.out = n.lattice)
  lattice <- fm_lattice_2d(x = x, y = x)
  mesh <- fm_rcdt_2d_inla(lattice = lattice, extend = FALSE, refine = FALSE)

  ## Generate an artificial sample
  sigma2.e <- 0.1
  n.obs <- 1000
  obs.loc <- cbind(
    runif(n.obs) * diff(range(x)) + min(x),
    runif(n.obs) * diff(range(x)) + min(x)
  )
  Q <- fm_matern_precision(mesh, alpha = 2, rho = 3, sigma = 1)
  x <- fm_sample(n = 1, Q = Q)
  A <- fm_basis(mesh, loc = obs.loc)
  Y <- as.vector(A %*% x + rnorm(n.obs) * sqrt(sigma2.e))

  ## Calculate posterior
  Q.post <- (Q + (t(A) %*% A) / sigma2.e)
  mu.post <- as.vector(solve(Q.post, (t(A) %*% Y) / sigma2.e))

  ## Calculate continuous contours
  tric <- tricontour(mesh,
    z = mu.post,
    levels = as.vector(quantile(x, c(0.25, 0.75)))
  )

  ## Discrete domain contours
  map <- contourmap(
    n.levels = 2, mu = mu.post, Q = Q.post,
    alpha = 0.1, compute = list(F = FALSE), max.threads = 1
  )

  ## Calculate continuous contour map
  setsc <- tricontourmap(mesh,
    z = mu.post,
    levels = as.vector(quantile(x, c(0.25, 0.75)))
  )
}
```

```
)  
  
## Plot the results  
reo <- mesh$idx$lattice  
idx.setsc <- setdiff(names(setsc$map), "-1")  
cols2 <- contourmap.colors(map,  
  col = heat.colors(100, 0.5, rev = TRUE),  
  credible.col = grey(0.5, 0)  
)  
names(cols2) <- as.character(-1:2)  
  
par(mfrow = c(1, 2))  
image(matrix(mu.post[reo], n.lattice, n.lattice),  
  main = "mean", axes = FALSE, asp = 1  
)  
plot(setsc$map[idx.setsc], col = cols2[idx.setsc])  
par(mfrow = c(1, 1))  
}  
  
## End(Not run)
```

# Index

continuous, 4  
continuous(), 3  
contourmap, 7  
contourmap(), 3, 5, 13, 15, 16  
contourmap.colors, 9  
contourmap.colors(), 3, 9, 13, 16  
contourmap.inla, 10  
contourmap.inla(), 3, 9, 15, 16  
contourmap.mc, 14  
contourmap.mc(), 3, 9, 13

exc\_safe\_inla, 26  
excursions, 16  
excursions(), 3, 5, 22, 25, 40  
excursions-package, 3  
excursions.inla, 19  
excursions.inla(), 3, 19, 25  
excursions.mc, 23  
excursions.mc(), 3, 19, 22  
excursions.variances, 25

gaussint, 27

print.excuobj(summary.excuobj), 40  
print.summary.excuobj  
    (summary.excuobj), 40

require(), 30  
require.nowarnings, 29

simconf, 30  
simconf(), 4, 33, 35, 37  
simconf.inla, 32  
simconf.inla(), 4, 31, 35, 37  
simconf.mc, 34  
simconf.mc(), 4, 31, 33, 37  
simconf.mixture, 36  
simconf.mixture(), 4, 31, 33  
submesh.grid, 38  
submesh.mesh, 39  
summary.excuobj, 40

summary.excuobj(), 40

tricontour, 40  
tricontour(), 3  
tricontourmap(tricontour), 40  
tricontourmap(), 3