

# Package ‘fetwfe’

May 8, 2026

**Title** Fused Extended Two-Way Fixed Effects

**Version** 1.5.0

**Maintainer** Gregory Faletto <gfaletto@gmail.com>

**Depends** R (>= 4.1.0)

**Description** Calculates the fused extended two-way fixed effects (FETWFE) estimator for unbiased and efficient estimation of difference-in-differences in panel data with staggered treatment adoption. This estimator eliminates bias inherent in conventional two-way fixed effects estimators, while also employing a novel bridge regression regularization approach to improve efficiency and yield valid standard errors. Also implements extended TWFE (etwfe) and bridge-penalized ETWFE (betwfe). Provides S3 classes for streamlined workflow and supports flexible tuning (ridge and rank-condition guarantees), automatic covariate centering/scaling, and detailed overall and cohort-specific effect estimates with valid standard errors. Includes simulation and formatting utilities, extensive diagnostic tools, vignettes, and examples. See Faletto (2025) (<doi:10.48550/arXiv.2312.05985>).

**URL** <https://github.com/gregfaletto/fetwfePackage>

**BugReports** <https://github.com/gregfaletto/fetwfePackage/issues>

**License** MIT + file LICENSE

**Encoding** UTF-8

**RoxygenNote** 7.3.2

**Imports** expm, glmnet, grpreg, Matrix (>= 1.6-0)

**Suggests** bacondecomp, knitr, rmarkdown, dplyr, did

**VignetteBuilder** knitr

**NeedsCompilation** no

**Author** Gregory Faletto [aut, cre] (ORCID:  
<<https://orcid.org/0000-0001-8298-1401>>)

**Repository** CRAN

**Date/Publication** 2025-07-02 16:20:12 UTC

## Contents

attgtToFetwfeDf . . . . .	2
betwfe . . . . .	4
betwfeWithSimulatedData . . . . .	9
etwfe . . . . .	12
etwfe-class . . . . .	15
etwfeToFetwfeDf . . . . .	15
etwfeWithSimulatedData . . . . .	17
fetwfe . . . . .	19
fetwfe-class . . . . .	24
fetwfeWithSimulatedData . . . . .	24
genCoefs . . . . .	27
genCoefsCore . . . . .	29
getTes . . . . .	30
simulateData . . . . .	32
simulateDataCore . . . . .	34
twfeCovs . . . . .	37
twfeCovsWithSimulatedData . . . . .	40
<b>Index</b>	<b>43</b>

---

attgtToFetwfeDf	<i>Convert data formatted for att_gt() to a dataframe suitable for fetwfe() / etwfe()</i>
-----------------	---

---

## Description

attgtToFetwfeDf() reshapes and renames a panel dataset that is already formatted for did::att\_gt() (Callaway and Sant’Anna 2021) so that it can be passed directly to fetwfe() or etwfe() from the fetwfe<sup>4</sup> package. In particular, it

- creates an *absorbing-state* treatment dummy that equals 1 from the first treated period onward\* and 0 otherwise,
- (optionally) drops units that are already treated in the very first period of the sample (because fetwfe() removes them internally), and
- returns a tidy dataframe whose column names match the arguments that fetwfe()/etwfe() expect.

## Usage

```
attgtToFetwfeDf(
  data,
  yname,
  tname,
  idname,
  gname,
  covars = character(0),
```

```

    drop_first_period_treated = TRUE,
    out_names = list(time = "time_var", unit = "unit_var", treatment = "treatment",
                     response = "response")
  )

```

### Arguments

<code>data</code>	A data.frame in <b>long</b> format containing at least the four columns used by <code>did::att_gt()</code> : outcome <code>yname</code> , time <code>tname</code> , unit <code>idname</code> , and the first-treatment period <code>gname</code> (which is 0 for the never-treated group).
<code>yname</code>	Character scalar. Name of the outcome column.
<code>tname</code>	Character scalar. Name of the time variable (numeric or integer). This becomes <code>time</code> in the returned dataframe.
<code>idname</code>	Character scalar. Name of the unit identifier. Converted to character and returned as <code>unit_var</code> .
<code>gname</code>	Character scalar. Name of the <i>group</i> variable holding the first period of treatment. Values must be 0 for never-treated, or a positive integer representing the first treated period.
<code>covars</code>	Character vector of additional covariate column names to carry through (default character( $\emptyset$ )). These columns are left untouched and appear <i>after</i> the required columns in the returned dataframe.
<code>drop_first_period_treated</code>	Logical. If TRUE (default), units that are already treated in the first sample period are removed <i>before</i> creating the treatment dummy. <code>fetwfe()</code> would do this internally, but dropping them here keeps the returned dataframe cleaner.
<code>out_names</code>	A named list giving the column names to use in the resulting dataframe. Defaults are <code>list(time = "time", unit = "unit", treatment = "treatment", response = "y")</code> . Override if you prefer different names (for instance, to keep the original <code>yname</code> ). The vector <i>must</i> contain exactly these four names.

### Value

A data.frame with columns `time`, `unit`, `treatment`, `y`, and any covariates requested in `covars`, ready to be fed to `fetwfe()/etwfe()`. All required columns are of the correct type: `time` is integer, `unit` is character, `treatment` is integer 0/1, and `y` is numeric.

### References

Callaway, Brantly and Pedro H.C. Sant'Anna. "Difference-in- Differences with Multiple Time Periods." *Journal of Econometrics*, Vol. 225, No. 2, pp. 200-230, 2021. doi:10.1016/j.jeconom.2020.12.001, <https://arxiv.org/abs/1803.09015>.

### Examples

```

## toy example -----
## Not run:
library(did) # provides the mpdta example dataframe
data(mpdta)

```

```

head(mpdata)

tidy_df <- attgtToFetwfeDf(
  data = mpdata,
  yname = "lemp",
  tname = "year",
  idname = "countyreal",
  gname = "first.treat",
  covars = c("lpop"))

head(tidy_df)

## End(Not run)

## Now you can call fetwfe() -----
# res <- fetwfe(
#   pdata      = tidy_df,
#   time_var   = "time_var",
#   unit_var   = "unit_var",
#   treatment  = "treatment",
#   response   = "response",
#   covs       = c("lpop"))

```

---

betwfe

*Bridge-penalized extended two-way fixed effects*


---

### Description

Implementation of extended two-way fixed effects with a bridge penalty. Estimates overall ATT as well as CATT (cohort average treatment effects on the treated units).

### Usage

```

betwfe(
  pdata,
  time_var,
  unit_var,
  treatment,
  response,
  covs = c(),
  indep_counts = NA,
  sig_eps_sq = NA,
  sig_eps_c_sq = NA,
  lambda.max = NA,
  lambda.min = NA,
  nlambdas = 100,
  q = 0.5,

```

```

    verbose = FALSE,
    alpha = 0.05,
    add_ridge = FALSE
  )

```

### Arguments

<code>pdata</code>	Dataframe; the panel data set. Each row should represent an observation of a unit at a time. Should contain columns as described below.
<code>time_var</code>	Character; the name of a single column containing a variable for the time period. This column is expected to contain integer values (for example, years). Recommended encodings for dates include format YYYY, YYYYMM, or YYYYM-MDD, whichever is appropriate for your data.
<code>unit_var</code>	Character; the name of a single column containing a variable for each unit. This column is expected to contain character values (i.e. the "name" of each unit).
<code>treatment</code>	Character; the name of a single column containing a variable for the treatment dummy indicator. This column is expected to contain integer values, and in particular, should equal 0 if the unit was untreated at that time and 1 otherwise. Treatment should be an absorbing state; that is, if unit $i$ is treated at time $t$ , then it must also be treated at all times $t + 1, \dots, T$ . Any units treated in the first time period will be removed automatically. Please make sure yourself that at least some units remain untreated at the final time period ("never-treated units").
<code>response</code>	Character; the name of a single column containing the response for each unit at each time. The response must be an integer or numeric value.
<code>covs</code>	(Optional.) Character; a vector containing the names of the columns for covariates. All of these columns are expected to contain integer, numeric, or factor values, and any categorical values will be automatically encoded as binary indicators. If no covariates are provided, the treatment effect estimation will proceed, but it will only be valid under unconditional versions of the parallel trends and no anticipation assumptions. Default is <code>c()</code> .
<code>indep_counts</code>	(Optional.) Integer; a vector. If you have a sufficiently large number of units, you can optionally randomly split your data set in half (with $N$ units in each data set). The data for half of the units should go in the <code>pdata</code> argument provided above. For the other $N$ units, simply provide the counts for how many units appear in the untreated cohort plus each of the other $R$ cohorts in this argument <code>indep_counts</code> . The benefit of doing this is that the standard error for the average treatment effect will be (asymptotically) exact instead of conservative. The length of <code>indep_counts</code> must equal 1 plus the number of treated cohorts in <code>pdata</code> . All entries of <code>indep_counts</code> must be strictly positive (if you are concerned that this might not work out, maybe your data set is on the small side and it's best to just leave your full data set in <code>pdata</code> ). The sum of all the counts in <code>indep_counts</code> must match the total number of units in <code>pdata</code> . Default is <code>NA</code> (in which case conservative standard errors will be calculated if $q < 1$ .)
<code>sig_eps_sq</code>	(Optional.) Numeric; the variance of the row-level IID noise assumed to apply to each observation. See Section 2 of Falletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be

	estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.
sig_eps_c_sq	(Optional.) Numeric; the variance of the unit-level IID noise (random effects) assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.
lambda.max	(Optional.) Numeric. A penalty parameter lambda will be selected over a grid search by BIC in order to select a single model. The largest lambda in the grid will be lambda.max. If no lambda.max is provided, one will be selected automatically. When $q \leq 1$ , the model will be sparse, and ideally all of the following are true at once: the smallest model (the one corresponding to lambda.max) selects close to 0 features, the largest model (the one corresponding to lambda.min) selects close to p features, nlambda is large enough so that models are considered at every feasible model size, and nlambda is small enough so that the computation doesn't become infeasible. You may want to manually tweak lambda.max, lambda.min, and nlambda to try to achieve these goals, particularly if the selected model size is very close to the model corresponding to lambda.max or lambda.min, which could indicate that the range of lambda values was too narrow or coarse. You can use the function outputs lambda.max_model_size, lambda.min_model_size, and lambda_star_model_size to try to assess this. Default is NA.
lambda.min	(Optional.) Numeric. The smallest lambda penalty parameter that will be considered. See the description of lambda.max for details. Default is NA.
nlambda	(Optional.) Integer. The total number of lambda penalty parameters that will be considered. See the description of lambda.max for details. Default is 100.
q	(Optional.) Numeric; determines what $L_q$ penalty is used for the regularization. $q = 1$ is the lasso, and for $0 < q < 1$ , it is possible to get standard errors and confidence intervals. $q = 2$ is ridge regression. See Faletto (2025) for details. Default is 0.5.
verbose	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.
alpha	Numeric; function will calculate $(1 - \alpha)$ confidence intervals for the cohort average treatment effects that will be returned in <code>cat t_df</code> .
add_ridge	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

### Value

A named list with the following elements:

att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	If $q < 1$ , a standard error for the ATT. If <code>indep_counts</code> was provided, this standard error is asymptotically exact; if not, it is asymptotically conservative. If $q \geq 1$ , this will be NA.

<code>catt_hats</code>	A named vector containing the estimated average treatment effects for each cohort.
<code>catt_ses</code>	If $q < 1$ , a named vector containing the (asymptotically exact, non-conservative) standard errors for the estimated average treatment effects within each cohort.
<code>cohort_probs</code>	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating <code>att_hat</code> . If <code>indep_counts</code> was provided, <code>cohort_probs</code> was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in <code>pdata</code> .
<code>catt_df</code>	A dataframe displaying the cohort names, average treatment effects, standard errors, and $1 - \alpha$ confidence interval bounds.
<code>beta_hat</code>	The full vector of estimated coefficients.
<code>treat_inds</code>	The indices of <code>beta_hat</code> corresponding to the treatment effects for each cohort at each time.
<code>treat_int_inds</code>	The indices of <code>beta_hat</code> corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
<code>sig_eps_sq</code>	Either the provided <code>sig_eps_sq</code> or the estimated one, if a value wasn't provided.
<code>sig_eps_c_sq</code>	Either the provided <code>sig_eps_c_sq</code> or the estimated one, if a value wasn't provided.
<code>lambda.max</code>	Either the provided <code>lambda.max</code> or the one that was used, if a value wasn't provided. (This is returned to help with getting a reasonable range of <code>lambda</code> values for grid search.)
<code>lambda.max_model_size</code>	The size of the selected model corresponding <code>lambda.max</code> (for $q \leq 1$ , this will be the smallest model size). As mentioned above, for $q \leq 1$ ideally this value is close to 0.
<code>lambda.min</code>	Either the provided <code>lambda.min</code> or the one that was used, if a value wasn't provided.
<code>lambda.min_model_size</code>	The size of the selected model corresponding to <code>lambda.min</code> (for $q \leq 1$ , this will be the largest model size). As mentioned above, for $q \leq 1$ ideally this value is close to $p$ .
<code>lambda_star</code>	The value of <code>lambda</code> chosen by BIC. If this value is close to <code>lambda.min</code> or <code>lambda.max</code> , that could suggest that the range of <code>lambda</code> values should be expanded.
<code>lambda_star_model_size</code>	The size of the model that was selected. If this value is close to <code>lambda.max_model_size</code> or <code>lambda.min_model_size</code> , That could suggest that the range of <code>lambda</code> values should be expanded.
<code>X_ints</code>	The design matrix created containing all interactions, time and cohort dummies, etc.
<code>y</code>	The vector of responses, containing <code>nrow(X_ints)</code> entries.
<code>X_final</code>	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.

y_final	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
T	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.
d	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
p	The final number of columns in the full set of covariates used to estimate the model.

### Author(s)

Gregory Faletto

### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. <https://arxiv.org/abs/2312.05985>.  
 Pesaran, M. H. . Time Series and Panel Data Econometrics. Number 9780198759980 in OUP Catalogue. Oxford University Press, 2015. URL <https://ideas.repec.org/b/oxp/obooks/9780198759980.html>.

### Examples

```
set.seed(23451)

library(bacondecomp)

data(divorce)

# sig_eps_sq and sig_eps_c_sq, calculated in a separate run of `fetwfe()`,
# are provided to speed up the computation of the example
res <- betwfe(
  pdata = divorce[divorce$sex == 2, ],
  time_var = "year",
  unit_var = "st",
  treatment = "changed",
  covs = c("murderrate", "lnpersinc", "afdcrolls"),
  response = "suiciderate_elast_jag",
  sig_eps_sq = 0.1025361,
  sig_eps_c_sq = 4.227651e-35,
  verbose = TRUE)

# Average treatment effect on the treated units (in percentage point
# units)
100 * res$att_hat

# Conservative 95% confidence interval for ATT (in percentage point units)
```

```

low_att <- 100 * (res$att_hat - qnorm(1 - 0.05 / 2) * res$att_se)
high_att <- 100 * (res$att_hat + qnorm(1 - 0.05 / 2) * res$att_se)

c(low_att, high_att)

# Cohort average treatment effects and confidence intervals (in percentage
# point units)

catt_df_pct <- res$catt_df
catt_df_pct[["Estimated TE"]] <- 100 * catt_df_pct[["Estimated TE"]]
catt_df_pct[["SE"]] <- 100 * catt_df_pct[["SE"]]
catt_df_pct[["ConfIntLow"]] <- 100 * catt_df_pct[["ConfIntLow"]]
catt_df_pct[["ConfIntHigh"]] <- 100 * catt_df_pct[["ConfIntHigh"]]

catt_df_pct

```

---

betwfeWithSimulatedData

*Run BETWFE on Simulated Data*


---

## Description

This function runs the bridge-penalized extended two-way fixed effects estimator (`betwfe()`) on simulated data. It is simply a wrapper for `betwfe()`: it accepts an object of class "FETWFE\_simulated" (produced by `simulateData()`) and unpacks the necessary components to pass to `betwfe()`. So the outputs match `betwfe()`, and the needed inputs match their counterparts in `betwfe()`.

## Usage

```

betwfeWithSimulatedData(
  simulated_obj,
  lambda.max = NA,
  lambda.min = NA,
  nlambdas = 100,
  q = 0.5,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)

```

## Arguments

`simulated_obj` An object of class "FETWFE\_simulated" containing the simulated panel data and design matrix.

`lambda.max` (Optional.) Numeric. A penalty parameter `lambda` will be selected over a grid search by BIC in order to select a single model. The largest `lambda` in the grid will be `lambda.max`. If no `lambda.max` is provided, one will be selected

automatically. For  $\lambda \leq 1$ , the model will be sparse, and ideally all of the following are true at once: the smallest model (the one corresponding to  $\lambda_{\max}$ ) selects close to 0 features, the largest model (the one corresponding to  $\lambda_{\min}$ ) selects close to  $p$  features,  $n_{\lambda}$  is large enough so that models are considered at every feasible model size, and  $n_{\lambda}$  is small enough so that the computation doesn't become infeasible. You may want to manually tweak  $\lambda_{\max}$ ,  $\lambda_{\min}$ , and  $n_{\lambda}$  to try to achieve these goals, particularly if the selected model size is very close to the model corresponding to  $\lambda_{\max}$  or  $\lambda_{\min}$ , which could indicate that the range of  $\lambda$  values was too narrow. You can use the function outputs  $\lambda_{\max\_model\_size}$ ,  $\lambda_{\min\_model\_size}$ , and  $\lambda_{star\_model\_size}$  to try to assess this. Default is NA.

<code>lambda.min</code>	(Optional.) Numeric. The smallest $\lambda$ penalty parameter that will be considered. See the description of <code>lambda.max</code> for details. Default is NA.
<code>nlambda</code>	(Optional.) Integer. The total number of $\lambda$ penalty parameters that will be considered. See the description of <code>lambda.max</code> for details. Default is 100.
<code>q</code>	(Optional.) Numeric; determines what $L_q$ penalty is used for the fusion regularization. $q = 1$ is the lasso, and for $0 < q < 1$ , it is possible to get standard errors and confidence intervals. $q = 2$ is ridge regression. See Faletto (2025) for details. Default is 0.5.
<code>verbose</code>	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.
<code>alpha</code>	Numeric; function will calculate $(1 - \alpha)$ confidence intervals for the cohort average treatment effects that will be returned in <code>catt_df</code> .
<code>add_ridge</code>	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

### Value

A named list with the following elements:

<code>att_hat</code>	The estimated overall average treatment effect for a randomly selected treated unit.
<code>att_se</code>	If $q < 1$ , a standard error for the ATT. If <code>indep_counts</code> was provided, this standard error is asymptotically exact; if not, it is asymptotically conservative. If $q \geq 1$ , this will be NA.
<code>catt_hats</code>	A named vector containing the estimated average treatment effects for each cohort.
<code>catt_ses</code>	If $q < 1$ , a named vector containing the (asymptotically exact, non-conservative) standard errors for the estimated average treatment effects within each cohort.
<code>cohort_probs</code>	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating <code>att_hat</code> . If <code>indep_counts</code> was provided, <code>cohort_probs</code> was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in <code>pdata</code> .
<code>catt_df</code>	A dataframe displaying the cohort names, average treatment effects, standard errors, and $1 - \alpha$ confidence interval bounds.

<code>beta_hat</code>	The full vector of estimated coefficients.
<code>treat_inds</code>	The indices of <code>beta_hat</code> corresponding to the treatment effects for each cohort at each time.
<code>treat_int_inds</code>	The indices of <code>beta_hat</code> corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
<code>sig_eps_sq</code>	Either the provided <code>sig_eps_sq</code> or the estimated one, if a value wasn't provided.
<code>sig_eps_c_sq</code>	Either the provided <code>sig_eps_c_sq</code> or the estimated one, if a value wasn't provided.
<code>lambda.max</code>	Either the provided <code>lambda.max</code> or the one that was used, if a value wasn't provided. (This is returned to help with getting a reasonable range of <code>lambda</code> values for grid search.)
<code>lambda.max_model_size</code>	The size of the selected model corresponding <code>lambda.max</code> (for $q \leq 1$ , this will be the smallest model size). As mentioned above, for $q \leq 1$ ideally this value is close to 0.
<code>lambda.min</code>	Either the provided <code>lambda.min</code> or the one that was used, if a value wasn't provided.
<code>lambda.min_model_size</code>	The size of the selected model corresponding to <code>lambda.min</code> (for $q \leq 1$ , this will be the largest model size). As mentioned above, for $q \leq 1$ ideally this value is close to $p$ .
<code>lambda_star</code>	The value of <code>lambda</code> chosen by BIC. If this value is close to <code>lambda.min</code> or <code>lambda.max</code> , that could suggest that the range of <code>lambda</code> values should be expanded.
<code>lambda_star_model_size</code>	The size of the model that was selected. If this value is close to <code>lambda.max_model_size</code> or <code>lambda.min_model_size</code> , That could suggest that the range of <code>lambda</code> values should be expanded.
<code>X_ints</code>	The design matrix created containing all interactions, time and cohort dummies, etc.
<code>y</code>	The vector of responses, containing <code>nrow(X_ints)</code> entries.
<code>X_final</code>	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
<code>y_final</code>	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
<code>N</code>	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
<code>T</code>	The number of time periods in the final data set.
<code>R</code>	The final number of treated cohorts that appear in the final data set.
<code>d</code>	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
<code>p</code>	The final number of columns in the full set of covariates used to estimate the model.

**Examples**

```
## Not run:
# Generate coefficients
coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

result <- betwfeWithSimulatedData(sim_data)

## End(Not run)
```

---

etwfe

*Extended two-way fixed effects*


---

**Description**

Implementation of extended two-way fixed effects. Estimates overall ATT as well as CATT (cohort average treatment effects on the treated units).

**Usage**

```
etwfe(
  pdata,
  time_var,
  unit_var,
  treatment,
  response,
  covs = c(),
  indep_counts = NA,
  sig_eps_sq = NA,
  sig_eps_c_sq = NA,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)
```

**Arguments**

<code>pdata</code>	Dataframe; the panel data set. Each row should represent an observation of a unit at a time. Should contain columns as described below.
<code>time_var</code>	Character; the name of a single column containing a variable for the time period. This column is expected to contain integer values (for example, years). Recommended encodings for dates include format YYYY, YYYYMM, or YYYYMMDD, whichever is appropriate for your data.

unit_var	Character; the name of a single column containing a variable for each unit. This column is expected to contain character values (i.e. the "name" of each unit).
treatment	Character; the name of a single column containing a variable for the treatment dummy indicator. This column is expected to contain integer values, and in particular, should equal 0 if the unit was untreated at that time and 1 otherwise. Treatment should be an absorbing state; that is, if unit $i$ is treated at time $t$ , then it must also be treated at all times $t + 1, \dots, T$ . Any units treated in the first time period will be removed automatically. Please make sure yourself that at least some units remain untreated at the final time period ("never-treated units").
response	Character; the name of a single column containing the response for each unit at each time. The response must be an integer or numeric value.
covs	(Optional.) Character; a vector containing the names of the columns for covariates. All of these columns are expected to contain integer, numeric, or factor values, and any categorical values will be automatically encoded as binary indicators. If no covariates are provided, the treatment effect estimation will proceed, but it will only be valid under unconditional versions of the parallel trends and no anticipation assumptions. Default is <code>c()</code> .
indep_counts	(Optional.) Integer; a vector. If you have a sufficiently large number of units, you can optionally randomly split your data set in half (with $N$ units in each data set). The data for half of the units should go in the <code>pdata</code> argument provided above. For the other $N$ units, simply provide the counts for how many units appear in the untreated cohort plus each of the other $R$ cohorts in this argument <code>indep_counts</code> . The benefit of doing this is that the standard error for the average treatment effect will be (asymptotically) exact instead of conservative. The length of <code>indep_counts</code> must equal 1 plus the number of treated cohorts in <code>pdata</code> . All entries of <code>indep_counts</code> must be strictly positive (if you are concerned that this might not work out, maybe your data set is on the small side and it's best to just leave your full data set in <code>pdata</code> ). The sum of all the counts in <code>indep_counts</code> must match the total number of units in <code>pdata</code> . Default is <code>NA</code> (in which case conservative standard errors will be calculated if $q < 1$ .)
sig_eps_sq	(Optional.) Numeric; the variance of the row-level IID noise assumed to apply to each observation. See Section 2 of Faleto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is <code>NA</code> .
sig_eps_c_sq	(Optional.) Numeric; the variance of the unit-level IID noise (random effects) assumed to apply to each observation. See Section 2 of Faleto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is <code>NA</code> .
verbose	Logical; if <code>TRUE</code> , more details on the progress of the function will be printed as the function executes. Default is <code>FALSE</code> .
alpha	Numeric; function will calculate $(1 - \alpha)$ confidence intervals for the cohort average treatment effects that will be returned in <code>cat t_df</code> .

`add_ridge` (Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

### Value

A named list with the following elements:

<code>att_hat</code>	The estimated overall average treatment effect for a randomly selected treated unit.
<code>att_se</code>	A standard error for the ATT. If the Gram matrix is not invertible, this will be NA.
<code>catt_hats</code>	A named vector containing the estimated average treatment effects for each cohort.
<code>catt_ses</code>	A named vector containing the (asymptotically exact) standard errors for the estimated average treatment effects within each cohort.
<code>cohort_probs</code>	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating <code>att_hat</code> . If <code>indep_counts</code> was provided, <code>cohort_probs</code> was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in <code>pdata</code> .
<code>catt_df</code>	A dataframe displaying the cohort names, average treatment effects, standard errors, and 1 - alpha confidence interval bounds.
<code>beta_hat</code>	The full vector of estimated coefficients.
<code>treat_inds</code>	The indices of <code>beta_hat</code> corresponding to the treatment effects for each cohort at each time.
<code>treat_int_inds</code>	The indices of <code>beta_hat</code> corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
<code>sig_eps_sq</code>	Either the provided <code>sig_eps_sq</code> or the estimated one, if a value wasn't provided.
<code>sig_eps_c_sq</code>	Either the provided <code>sig_eps_c_sq</code> or the estimated one, if a value wasn't provided.
<code>X_ints</code>	The design matrix created containing all interactions, time and cohort dummies, etc.
<code>y</code>	The vector of responses, containing <code>nrow(X_ints)</code> entries.
<code>X_final</code>	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
<code>y_final</code>	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
<code>N</code>	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
<code>T</code>	The number of time periods in the final data set.
<code>R</code>	The final number of treated cohorts that appear in the final data set.
<code>d</code>	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
<code>p</code>	The final number of columns in the full set of covariates used to estimate the model.

**Author(s)**

Gregory Faletto

**References**

Wooldridge, J. M. (2021). Two-way fixed effects, the two-way mundlak regression, and difference-in-differences estimators. *Available at SSRN 3906345*. doi:10.2139/ssrn.3906345.

---

 etwfe-class

*Extended Two-Way Fixed Effects Output Class*


---

**Description**

S3 class for the output of `etwfe()`.

---

 etwfeToFetwfeDf

*Convert data prepared for `etwfe::etwfe()` to the format required by `fetwfe()` and `fetwfe::etwfe()`*


---

**Description**

`etwfeToFetwfeDf()` reshapes and renames a panel dataset that is already formatted for `etwfe::etwfe()` (McDermott 2024) so that it can be passed directly to `fetwfe()` or `etwfe()` from the `fetwfe` package. In particular, it

- creates an *absorbing-state* treatment dummy that equals 1 from the first treated period onward\* and 0 otherwise,
- (optionally) drops units that are already treated in the very first period of the sample (because `fetwfe()` removes them internally), and
- returns a tidy dataframe whose column names match the arguments that `fetwfe()/etwfe()` expect.

**Usage**

```
etwfeToFetwfeDf(
  data,
  yvar,
  tvar,
  idvar,
  gvar,
  covars = character(0),
  drop_first_period_treated = TRUE,
  out_names = list(time = "time_var", unit = "unit_var", treatment = "treatment",
    response = "response")
)
```

**Arguments**

data	A long-format data.frame that you could already feed to etwfe().
yvar	Character. Column name of the outcome (left-hand side in your fml).
tvar	Character. Column name of the time variable that you pass to etwfe() as tvar.
idvar	Character. Column name of the unit identifier (the variable you would cluster on, or pass to etwfe(..., ivar = idvar) if you were using unit FEs).
gvar	Character. Column name of the “first treated” cohort variable passed to etwfe() as gvar. Must be 0 for never-treated units, or the (strictly positive) first treated period.
covars	Character vector of <i>additional</i> covariate columns to keep (default character(0)).
drop_first_period_treated	Logical. Should units already treated in the very first sample period be removed? (fetwfe() will drop them internally anyway, but doing it here keeps the returned dataframe clean.) Default TRUE.
out_names	Named list giving the column names that the returned dataframe should have. The default (time, unit, treatment, y) matches the arguments usually supplied to fetwfe(). <b>Do not change the names of this list</b> – only the <i>values</i> – and keep all four.

**Value**

A tidy data.frame with (in this order)

- time integer,
- unit character,
- treatment integer 0/1 absorbing-state dummy,
- response numeric outcome,
- any covariates requested in covars. Ready to pass straight to fetwfe() or fetwfe::etwfe().

**References**

McDermott G (2024). *etwfe: Extended Two-Way Fixed Effects*. doi:10.32614/CRAN.package.etwfe doi:10.32614/CRAN.package.etwfe, R package version 0.5.0, <https://CRAN.R-project.org/package=etwfe>.

**Examples**

```
## toy example -----
## Not run:
library(did) # provides the mpdta example dataframe
data(mpdta)

head(mpdta)

tidy_df <- etwfeToFetwfeDf(
  data = mpdta,
```

```

yvar = "lemp",
tvar = "year",
idvar = "countyreal",
gvar = "first.treat",
covars = c("lpop")

head(tidy_df)

## End(Not run)
## Now you can call fetwfe() -----
# res <- fetwfe(
#   pdata      = tidy_df,
#   time_var   = "time_var",
#   unit_var   = "unit_var",
#   treatment  = "treatment",
#   response   = "response",
#   covs       = c("lpop"))

```

---

etwfeWithSimulatedData

*Run ETWFE on Simulated Data*


---

## Description

This function runs the extended two-way fixed effects estimator (`etwfe()`) on simulated data. It is simply a wrapper for `etwfe()`: it accepts an object of class "FETWFE\_simulated" (produced by `simulateData()`) and unpacks the necessary components to pass to `etwfe()`. So the outputs match `etwfe()`, and the needed inputs match their counterparts in `etwfe()`.

## Usage

```

etwfeWithSimulatedData(
  simulated_obj,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)

```

## Arguments

<code>simulated_obj</code>	An object of class "FETWFE_simulated" containing the simulated panel data and design matrix.
<code>verbose</code>	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.
<code>alpha</code>	Numeric; function will calculate $(1 - \alpha)$ confidence intervals for the cohort average treatment effects that will be returned in <code>catt_df</code> .
<code>add_ridge</code>	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

**Value**

A named list with the following elements:

<code>att_hat</code>	The estimated overall average treatment effect for a randomly selected treated unit.
<code>att_se</code>	A standard error for the ATT. If the Gram matrix is not invertible, this will be NA.
<code>catt_hats</code>	A named vector containing the estimated average treatment effects for each cohort.
<code>catt_ses</code>	A named vector containing the (asymptotically exact) standard errors for the estimated average treatment effects within each cohort.
<code>cohort_probs</code>	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating <code>att_hat</code> . If <code>indep_counts</code> was provided, <code>cohort_probs</code> was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in <code>pdata</code> .
<code>catt_df</code>	A dataframe displaying the cohort names, average treatment effects, standard errors, and 1 - alpha confidence interval bounds.
<code>beta_hat</code>	The full vector of estimated coefficients.
<code>treat_inds</code>	The indices of <code>beta_hat</code> corresponding to the treatment effects for each cohort at each time.
<code>treat_int_inds</code>	The indices of <code>beta_hat</code> corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
<code>sig_eps_sq</code>	Either the provided <code>sig_eps_sq</code> or the estimated one, if a value wasn't provided.
<code>sig_eps_c_sq</code>	Either the provided <code>sig_eps_c_sq</code> or the estimated one, if a value wasn't provided.
<code>X_ints</code>	The design matrix created containing all interactions, time and cohort dummies, etc.
<code>y</code>	The vector of responses, containing <code>nrow(X_ints)</code> entries.
<code>X_final</code>	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
<code>y_final</code>	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
<code>N</code>	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
<code>T</code>	The number of time periods in the final data set.
<code>R</code>	The final number of treated cohorts that appear in the final data set.
<code>d</code>	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
<code>p</code>	The final number of columns in the full set of covariates used to estimate the model.

**Examples**

```
## Not run:
# Generate coefficients
coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

result <- etwfeWithSimulatedData(sim_data)

## End(Not run)
```

---

 fetwfe

---

*Fused extended two-way fixed effects*


---

**Description**

Implementation of fused extended two-way fixed effects. Estimates overall ATT as well as CATT (cohort average treatment effects on the treated units).

**Usage**

```
fetwfe(
  pdata,
  time_var,
  unit_var,
  treatment,
  response,
  covs = c(),
  indep_counts = NA,
  sig_eps_sq = NA,
  sig_eps_c_sq = NA,
  lambda.max = NA,
  lambda.min = NA,
  nlambdas = 100,
  q = 0.5,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)
```

**Arguments**

`pdata` Dataframe; the panel data set. Each row should represent an observation of a unit at a time. Should contain columns as described below.

<code>time_var</code>	Character; the name of a single column containing a variable for the time period. This column is expected to contain integer values (for example, years). Recommended encodings for dates include format YYYY, YYYYMM, or YYYYMMDD, whichever is appropriate for your data.
<code>unit_var</code>	Character; the name of a single column containing a variable for each unit. This column is expected to contain character values (i.e. the "name" of each unit).
<code>treatment</code>	Character; the name of a single column containing a variable for the treatment dummy indicator. This column is expected to contain integer values, and in particular, should equal 0 if the unit was untreated at that time and 1 otherwise. Treatment should be an absorbing state; that is, if unit $i$ is treated at time $t$ , then it must also be treated at all times $t + 1, \dots, T$ . Any units treated in the first time period will be removed automatically. Please make sure yourself that at least some units remain untreated at the final time period ("never-treated units").
<code>response</code>	Character; the name of a single column containing the response for each unit at each time. The response must be an integer or numeric value.
<code>covs</code>	(Optional.) Character; a vector containing the names of the columns for covariates. All of these columns are expected to contain integer, numeric, or factor values, and any categorical values will be automatically encoded as binary indicators. If no covariates are provided, the treatment effect estimation will proceed, but it will only be valid under unconditional versions of the parallel trends and no anticipation assumptions. Default is <code>c()</code> .
<code>indep_counts</code>	(Optional.) Integer; a vector. If you have a sufficiently large number of units, you can optionally randomly split your data set in half (with $N$ units in each data set). The data for half of the units should go in the <code>pdata</code> argument provided above. For the other $N$ units, simply provide the counts for how many units appear in the untreated cohort plus each of the other $R$ cohorts in this argument <code>indep_counts</code> . The benefit of doing this is that the standard error for the average treatment effect will be (asymptotically) exact instead of conservative. The length of <code>indep_counts</code> must equal 1 plus the number of treated cohorts in <code>pdata</code> . All entries of <code>indep_counts</code> must be strictly positive (if you are concerned that this might not work out, maybe your data set is on the small side and it's best to just leave your full data set in <code>pdata</code> ). The sum of all the counts in <code>indep_counts</code> must match the total number of units in <code>pdata</code> . Default is NA (in which case conservative standard errors will be calculated if $q < 1$ .)
<code>sig_eps_sq</code>	(Optional.) Numeric; the variance of the row-level IID noise assumed to apply to each observation. See Section 2 of Falletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.
<code>sig_eps_c_sq</code>	(Optional.) Numeric; the variance of the unit-level IID noise (random effects) assumed to apply to each observation. See Section 2 of Falletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.

<code>lambda.max</code>	(Optional.) Numeric. A penalty parameter <code>lambda</code> will be selected over a grid search by BIC in order to select a single model. The largest <code>lambda</code> in the grid will be <code>lambda.max</code> . If no <code>lambda.max</code> is provided, one will be selected automatically. When $q \leq 1$ , the model will be sparse, and ideally all of the following are true at once: the smallest model (the one corresponding to <code>lambda.max</code> ) selects close to 0 features, the largest model (the one corresponding to <code>lambda.min</code> ) selects close to $p$ features, <code>nlambda</code> is large enough so that models are considered at every feasible model size, and <code>nlambda</code> is small enough so that the computation doesn't become infeasible. You may want to manually tweak <code>lambda.max</code> , <code>lambda.min</code> , and <code>nlambda</code> to try to achieve these goals, particularly if the selected model size is very close to the model corresponding to <code>lambda.max</code> or <code>lambda.min</code> , which could indicate that the range of <code>lambda</code> values was too narrow or coarse. You can use the function outputs <code>lambda.max_model_size</code> , <code>lambda.min_model_size</code> , and <code>lambda_star_model_size</code> to try to assess this. Default is NA.
<code>lambda.min</code>	(Optional.) Numeric. The smallest <code>lambda</code> penalty parameter that will be considered. See the description of <code>lambda.max</code> for details. Default is NA.
<code>nlambda</code>	(Optional.) Integer. The total number of <code>lambda</code> penalty parameters that will be considered. See the description of <code>lambda.max</code> for details. Default is 100.
<code>q</code>	(Optional.) Numeric; determines what $L_q$ penalty is used for the fusion regularization. $q = 1$ is the lasso, and for $0 < q < 1$ , it is possible to get standard errors and confidence intervals. $q = 2$ is ridge regression. See Faletto (2025) for details. Default is 0.5.
<code>verbose</code>	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.
<code>alpha</code>	Numeric; function will calculate $(1 - \alpha)$ confidence intervals for the cohort average treatment effects that will be returned in <code>catt_df</code> .
<code>add_ridge</code>	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

## Value

An object of class `fetwfe` containing the following elements:

<code>att_hat</code>	The estimated overall average treatment effect for a randomly selected treated unit.
<code>att_se</code>	If $q < 1$ , a standard error for the ATT. If <code>indep_counts</code> was provided, this standard error is asymptotically exact; if not, it is asymptotically conservative. If $q \geq 1$ , this will be NA.
<code>catt_hats</code>	A named vector containing the estimated average treatment effects for each cohort.
<code>catt_ses</code>	If $q < 1$ , a named vector containing the (asymptotically exact, non-conservative) standard errors for the estimated average treatment effects within each cohort.
<code>cohort_probs</code>	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating <code>att_hat</code> . If <code>indep_counts</code> was provided, <code>cohort_probs</code> was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in <code>pdata</code> .

<code>catt_df</code>	A dataframe displaying the cohort names, average treatment effects, standard errors, and $1 - \alpha$ confidence interval bounds.
<code>beta_hat</code>	The full vector of estimated coefficients.
<code>treat_inds</code>	The indices of <code>beta_hat</code> corresponding to the treatment effects for each cohort at each time.
<code>treat_int_inds</code>	The indices of <code>beta_hat</code> corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
<code>sig_eps_sq</code>	Either the provided <code>sig_eps_sq</code> or the estimated one, if a value wasn't provided.
<code>sig_eps_c_sq</code>	Either the provided <code>sig_eps_c_sq</code> or the estimated one, if a value wasn't provided.
<code>lambda.max</code>	Either the provided <code>lambda.max</code> or the one that was used, if a value wasn't provided. (This is returned to help with getting a reasonable range of <code>lambda</code> values for grid search.)
<code>lambda.max_model_size</code>	The size of the selected model corresponding to <code>lambda.max</code> (for $q \leq 1$ , this will be the smallest model size). As mentioned above, for $q \leq 1$ ideally this value is close to 0.
<code>lambda.min</code>	Either the provided <code>lambda.min</code> or the one that was used, if a value wasn't provided.
<code>lambda.min_model_size</code>	The size of the selected model corresponding to <code>lambda.min</code> (for $q \leq 1$ , this will be the largest model size). As mentioned above, for $q \leq 1$ ideally this value is close to $p$ .
<code>lambda_star</code>	The value of <code>lambda</code> chosen by BIC. If this value is close to <code>lambda.min</code> or <code>lambda.max</code> , that could suggest that the range of <code>lambda</code> values should be expanded.
<code>lambda_star_model_size</code>	The size of the model that was selected. If this value is close to <code>lambda.max_model_size</code> or <code>lambda.min_model_size</code> , that could suggest that the range of <code>lambda</code> values should be expanded.
<code>N</code>	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
<code>T</code>	The number of time periods in the final data set.
<code>R</code>	The final number of treated cohorts that appear in the final data set.
<code>d</code>	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
<code>p</code>	The final number of columns in the full set of covariates used to estimate the model.
<code>alpha</code>	The alpha level used for confidence intervals.
<code>internal</code>	A list containing internal outputs that are typically not needed for interpretation: <b>X_ints</b> The design matrix created containing all interactions, time and cohort dummies, etc.

- y** The vector of responses, containing `nrow(X_ints)` entries.
- X\_final** The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
- y\_final** The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
- calc\_ses** Logical indicating whether standard errors were calculated.

The object has methods for `print()`, `summary()`, and `coef()`. By default, `print()` and `summary()` only show the essential outputs. To see internal details, use `print(x, show_internal = TRUE)` or `summary(x, show_internal = TRUE)`. The `coef()` method returns the vector of estimated coefficients (`beta_hat`).

### Author(s)

Gregory Faletto

### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. <https://arxiv.org/abs/2312.05985>.  
 Pesaran, M. H. . Time Series and Panel Data Econometrics. Number 9780198759980 in OUP Catalogue. Oxford University Press, 2015. URL <https://ideas.repec.org/b/oxp/obooks/9780198759980.html>.

### Examples

```
set.seed(23451)

library(bacondecomp)

data(divorce)

# sig_eps_sq and sig_eps_c_sq, calculated in a separate run of `fetwfe()`,
# are provided to speed up the computation of the example
res <- fetwfe(
  pdata = divorce[divorce$sex == 2, ],
  time_var = "year",
  unit_var = "st",
  treatment = "changed",
  covs = c("murderrate", "lnpersinc", "afdcrolls"),
  response = "suiciderate_elast_jag",
  sig_eps_sq = 0.1025361,
  sig_eps_c_sq = 4.227651e-35,
  verbose = TRUE)

# Print results with internal details
print(res, max_cohorts = Inf)
```

---

fetwfe-class	<i>Fused Extended Two-Way Fixed Effects Output Class</i>
--------------	--

---

**Description**

S3 class for the output of fetwfe().

---

fetwfeWithSimulatedData	<i>Run FETWFE on Simulated Data</i>
-------------------------	-------------------------------------

---

**Description**

This function runs the fused extended two-way fixed effects estimator (fetwfe()) on simulated data. It is simply a wrapper for fetwfe(): it accepts an object of class "FETWFE\_simulated" (produced by simulateData()) and unpacks the necessary components to pass to fetwfe(). So the outputs match fetwfe(), and the needed inputs match their counterparts in fetwfe().

**Usage**

```
fetwfeWithSimulatedData(
  simulated_obj,
  lambda.max = NA,
  lambda.min = NA,
  nlambdas = 100,
  q = 0.5,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)
```

**Arguments**

simulated_obj	An object of class "FETWFE_simulated" containing the simulated panel data and design matrix.
lambda.max	(Optional.) Numeric. A penalty parameter lambda will be selected over a grid search by BIC in order to select a single model. The largest lambda in the grid will be lambda.max. If no lambda.max is provided, one will be selected automatically. For lambda <= 1, the model will be sparse, and ideally all of the following are true at once: the smallest model (the one corresponding to lambda.max) selects close to 0 features, the largest model (the one corresponding to lambda.min) selects close to p features, nlambdas is large enough so that models are considered at every feasible model size, and nlambdas is small enough so that the computation doesn't become infeasible. You may want to manually

tweak `lambda.max`, `lambda.min`, and `nlambda` to try to achieve these goals, particularly if the selected model size is very close to the model corresponding to `lambda.max` or `lambda.min`, which could indicate that the range of `lambda` values was too narrow. You can use the function outputs `lambda.max_model_size`, `lambda.min_model_size`, and `lambda.star_model_size` to try to assess this. Default is NA.

<code>lambda.min</code>	(Optional.) Numeric. The smallest <code>lambda</code> penalty parameter that will be considered. See the description of <code>lambda.max</code> for details. Default is NA.
<code>nlambda</code>	(Optional.) Integer. The total number of <code>lambda</code> penalty parameters that will be considered. See the description of <code>lambda.max</code> for details. Default is 100.
<code>q</code>	(Optional.) Numeric; determines what $L_q$ penalty is used for the fusion regularization. $q = 1$ is the lasso, and for $0 < q < 1$ , it is possible to get standard errors and confidence intervals. $q = 2$ is ridge regression. See Faleto (2025) for details. Default is 0.5.
<code>verbose</code>	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.
<code>alpha</code>	Numeric; function will calculate $(1 - \alpha)$ confidence intervals for the cohort average treatment effects that will be returned in <code>catt_df</code> .
<code>add_ridge</code>	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

### Value

An object of class `fetwfe` containing the following elements:

<code>att_hat</code>	The estimated overall average treatment effect for a randomly selected treated unit.
<code>att_se</code>	If $q < 1$ , a standard error for the ATT. If <code>indep_counts</code> was provided, this standard error is asymptotically exact; if not, it is asymptotically conservative. If $q \geq 1$ , this will be NA.
<code>catt_hats</code>	A named vector containing the estimated average treatment effects for each cohort.
<code>catt_ses</code>	If $q < 1$ , a named vector containing the (asymptotically exact, non-conservative) standard errors for the estimated average treatment effects within each cohort.
<code>cohort_probs</code>	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating <code>att_hat</code> . If <code>indep_counts</code> was provided, <code>cohort_probs</code> was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in <code>pdata</code> .
<code>catt_df</code>	A dataframe displaying the cohort names, average treatment effects, standard errors, and $1 - \alpha$ confidence interval bounds.
<code>beta_hat</code>	The full vector of estimated coefficients.
<code>treat_inds</code>	The indices of <code>beta_hat</code> corresponding to the treatment effects for each cohort at each time.
<code>treat_int_inds</code>	The indices of <code>beta_hat</code> corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.

<code>sig_eps_sq</code>	Either the provided <code>sig_eps_sq</code> or the estimated one, if a value wasn't provided.
<code>sig_eps_c_sq</code>	Either the provided <code>sig_eps_c_sq</code> or the estimated one, if a value wasn't provided.
<code>lambda.max</code>	Either the provided <code>lambda.max</code> or the one that was used, if a value wasn't provided. (This is returned to help with getting a reasonable range of <code>lambda</code> values for grid search.)
<code>lambda.max_model_size</code>	The size of the selected model corresponding to <code>lambda.max</code> (for $q \leq 1$ , this will be the smallest model size). As mentioned above, for $q \leq 1$ ideally this value is close to 0.
<code>lambda.min</code>	Either the provided <code>lambda.min</code> or the one that was used, if a value wasn't provided.
<code>lambda.min_model_size</code>	The size of the selected model corresponding to <code>lambda.min</code> (for $q \leq 1$ , this will be the largest model size). As mentioned above, for $q \leq 1$ ideally this value is close to $p$ .
<code>lambda_star</code>	The value of <code>lambda</code> chosen by BIC. If this value is close to <code>lambda.min</code> or <code>lambda.max</code> , that could suggest that the range of <code>lambda</code> values should be expanded.
<code>lambda_star_model_size</code>	The size of the model that was selected. If this value is close to <code>lambda.max_model_size</code> or <code>lambda.min_model_size</code> , that could suggest that the range of <code>lambda</code> values should be expanded.
<code>N</code>	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
<code>T</code>	The number of time periods in the final data set.
<code>R</code>	The final number of treated cohorts that appear in the final data set.
<code>d</code>	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
<code>p</code>	The final number of columns in the full set of covariates used to estimate the model.
<code>alpha</code>	The alpha level used for confidence intervals.
<code>internal</code>	A list containing internal outputs that are typically not needed for interpretation: <ul style="list-style-type: none"> <li><b>X_ints</b> The design matrix created containing all interactions, time and cohort dummies, etc.</li> <li><b>y</b> The vector of responses, containing <code>nrow(X_ints)</code> entries.</li> <li><b>X_final</b> The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.</li> <li><b>y_final</b> The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.</li> <li><b>calc_ses</b> Logical indicating whether standard errors were calculated.</li> </ul>

The object has methods for `print()`, `summary()`, and `coef()`. By default, `print()` and `summary()` only show the essential outputs. To see internal details, use `print(x, show_internal = TRUE)` or `summary(x, show_internal = TRUE)`. The `coef()` method returns the vector of estimated coefficients (`beta_hat`).

## Examples

```
## Not run:
# Generate coefficients
coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

result <- fetwfeWithSimulatedData(sim_data)

## End(Not run)
```

---

genCoefs

*Generate Coefficient Vector for Data Generation*

---

## Description

This function generates a coefficient vector `beta` for simulation studies of the fused extended two-way fixed effects estimator. It returns an S3 object of class "FETWFE\_coefs" containing `beta` along with simulation parameters `R`, `T`, and `d`. See the simulation studies section of Faletto (2025) for details.

## Usage

```
genCoefs(R, T, d, density, eff_size, seed = NULL)
```

## Arguments

<code>R</code>	Integer. The number of treated cohorts (treatment is assumed to start in periods 2 to $R + 1$ ).
<code>T</code>	Integer. The total number of time periods.
<code>d</code>	Integer. The number of time-invariant covariates. If $d > 0$ , additional terms corresponding to covariate main effects and interactions are included in <code>beta</code> .
<code>density</code>	Numeric in (0,1). The probability that any given entry in the initial sparse coefficient vector <code>theta</code> is nonzero.
<code>eff_size</code>	Numeric. The magnitude used to scale nonzero entries in <code>theta</code> . Each nonzero entry is set to <code>eff_size</code> or <code>-eff_size</code> (with a 60 percent chance for a positive value).
<code>seed</code>	(Optional) Integer. Seed for reproducibility.

## Details

The length of beta is given by

$$p = R + (T - 1) + d + dR + d(T - 1) + num\_treats + (num\_treats \times d)$$

, where the number of treatment parameters is defined as

$$num\_treats = T \times R - \frac{R(R + 1)}{2}$$

.

The function operates in two steps:

1. It first creates a sparse vector theta of length  $p$ , with nonzero entries occurring with probability density. Nonzero entries are set to `eff_size` or `-eff_size` (with a 60\
2. The full coefficient vector beta is then computed by applying an inverse fusion transform to theta using internal routines (e.g., `genBackwardsInvFusionTransformMat()` and `genInvTwoWayFusionTransformM`

## Value

An object of class "FETWFE\_coefs", which is a list containing:

**beta** A numeric vector representing the full coefficient vector after the inverse fusion transform.

**theta** A numeric vector representing the coefficient vector in the transformed feature space. theta is a sparse vector, which aligns with an assumption that deviations from the restrictions encoded in the FETWFE model are sparse. beta is derived from theta.

**R** The provided number of treated cohorts.

**T** The provided number of time periods.

**d** The provided number of covariates.

**seed** The provided seed.

## References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. <https://arxiv.org/abs/2312.05985>.

## Examples

```
## Not run:
# Generate coefficients
coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

## End(Not run)
```

---

genCoefsCore                      *Generate Coefficient Vector for Data Generation*

---

### Description

This function generates a coefficient vector  $\beta$  along with a sparse auxiliary vector  $\theta$  for simulation studies of the fused extended two-way fixed effects estimator. The returned  $\beta$  is formatted to align with the design matrix created by `genRandomData()`, and is a valid input for the  $\beta$  argument of that function. The vector  $\theta$  is sparse, with nonzero entries occurring with probability density and scaled by `eff_size`. See the simulation studies section of Faletto (2025) for details.

### Usage

```
genCoefsCore(R, T, d, density, eff_size, seed = NULL)
```

### Arguments

R	Integer. The number of treated cohorts (treatment is assumed to start in periods 2 to $R + 1$ ).
T	Integer. The total number of time periods.
d	Integer. The number of time-invariant covariates. If $d > 0$ , additional terms corresponding to covariate main effects and interactions are included in $\beta$ .
density	Numeric in (0,1). The probability that any given entry in the initial sparse coefficient vector $\theta$ is nonzero.
eff_size	Numeric. The magnitude used to scale nonzero entries in $\theta$ . Each nonzero entry is set to <code>eff_size</code> or <code>-eff_size</code> (with a 60 percent chance for a positive value).
seed	(Optional) Integer. Seed for reproducibility.

### Details

The length of  $\beta$  is given by

$$p = R + (T - 1) + d + dR + d(T - 1) + num\_treats + (num\_treats \times d)$$

, where the number of treatment parameters is defined as

$$num\_treats = T \times R - \frac{R(R + 1)}{2}$$

.

The function operates in two steps:

1. It first creates a sparse vector  $\theta$  of length  $p$ , with nonzero entries occurring with probability density. Nonzero entries are set to `eff_size` or `-eff_size` (with a 60\
2. The full coefficient vector  $\beta$  is then computed by applying an inverse fusion transform to  $\theta$  using internal routines (e.g., `genBackwardsInvFusionTransformMat()` and `genInvTwoWayFusionTransformM`

**Value**

A list with two elements:

**beta** A numeric vector representing the full coefficient vector after the inverse fusion transform.

**theta** A numeric vector representing the coefficient vector in the transformed feature space. theta is a sparse vector, which aligns with an assumption that deviations from the restrictions encoded in the FETWFE model are sparse. beta is derived from theta.

**References**

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. <https://arxiv.org/abs/2312.05985>.

**Examples**

```
## Not run:
# Set parameters for the coefficient generation
R <- 3          # Number of treated cohorts
T <- 6          # Total number of time periods
d <- 2          # Number of covariates
density <- 0.1 # Probability that an entry in the initial vector is nonzero
eff_size <- 1.5 # Scaling factor for nonzero coefficients
seed <- 789     # Seed for reproducibility

# Generate coefficients using genCoefsCore()
coefs_core <- genCoefsCore(R = R, T = T, d = d, density = density,
  eff_size = eff_size, seed = seed)
beta <- coefs_core$beta
theta <- coefs_core$theta

# For diagnostic purposes, compute the expected length of beta.
# The length p is defined internally as:
#   p = R + (T - 1) + d + d*R + d*(T - 1) + num_treats + num_treats*d,
# where num_treats = T * R - (R*(R+1))/2.
num_treats <- T * R - (R * (R + 1)) / 2
p_expected <- R + (T - 1) + d + d * R + d * (T - 1) + num_treats + num_treats * d

cat("Length of beta:", length(beta), "\nExpected length:", p_expected, "\n")

## End(Not run)
```

## Description

This function extracts the true treatment effects from a full coefficient vector as generated by `genCoefs()`. It calculates the overall average treatment effect on the treated (ATT) as the equal-weighted average of the cohort-specific treatment effects, and also returns the individual treatment effects for each treated cohort.

## Usage

```
getTes(coefs_obj)
```

## Arguments

`coefs_obj` An object of class "FETWFE\_coefs" containing the coefficient vector and simulation parameters.

## Details

The function internally uses auxiliary routines `getNumTreats()`, `getP()`, `getFirstInds()`, `getTreatInds()`, and `getActualCohortTes()` to determine the correct indices of treatment effect coefficients in `beta`. The overall treatment effect is computed as the simple average of these cohort-specific effects.

## Value

A named list with two elements:

**att\_true** A numeric value representing the overall average treatment effect on the treated. It is computed as the (equal-weighted) mean of the cohort-specific treatment effects.

**actual\_cohort\_tes** A numeric vector containing the true cohort-specific treatment effects, calculated by averaging the coefficients corresponding to the treatment dummies for each cohort.

## Examples

```
## Not run:
# Generate coefficients
coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Compute the true treatment effects:
te_results <- getTes(coefs)

# Overall average treatment effect on the treated:
print(te_results$att_true)

# Cohort-specific treatment effects:
print(te_results$actual_cohort_tes)

## End(Not run)
```

simulateData

*Generate Random Panel Data for FETWFE Simulations***Description**

Generates a random panel data set for simulation studies of the fused extended two-way fixed effects (FETWFE) estimator by taking an object of class "FETWFE\_coefs" (produced by `genCoefs()`) and using it to simulate data. The function creates a balanced panel with  $N$  units over  $T$  time periods, assigns treatment status across  $R$  treated cohorts (with equal marginal probabilities for treatment and non-treatment), and constructs a design matrix along with the corresponding outcome. The covariates are generated according to the specified distribution: by default, covariates are drawn from a normal distribution; if `distribution = "uniform"`, they are drawn uniformly from  $[-\sqrt{3}, \sqrt{3}]$ . When  $d = 0$  (i.e. no covariates), no covariate-related columns or interactions are generated. See the simulation studies section of Faleto (2025) for details.

**Usage**

```
simulateData(
  coefs_obj,
  N,
  sig_eps_sq,
  sig_eps_c_sq,
  distribution = "gaussian",
  guarantee_rank_condition = FALSE
)
```

**Arguments**

<code>coefs_obj</code>	An object of class "FETWFE_coefs" containing the coefficient vector and simulation parameters.
<code>N</code>	Integer. Number of units in the panel.
<code>sig_eps_sq</code>	Numeric. Variance of the idiosyncratic (observation-level) noise.
<code>sig_eps_c_sq</code>	Numeric. Variance of the unit-level random effects.
<code>distribution</code>	Character. Distribution to generate covariates. Defaults to "gaussian". If set to "uniform", covariates are drawn uniformly from $[-\sqrt{3}, \sqrt{3}]$ .
<code>guarantee_rank_condition</code>	(Optional). Logical. If TRUE, the returned data set is guaranteed to have at least $d + 1$ units per cohort, which is necessary for the final design matrix to have full column rank. Default is FALSE, in which case no such condition is enforced.

**Details**

This function extracts simulation parameters from the `FETWFE_coefs` object and passes them, along with additional simulation parameters, to the internal function `simulateDataCore()`. It validates that all necessary components are returned and assigns the S3 class "FETWFE\_simulated" to the output.

The argument `distribution` controls the generation of covariates. For "gaussian", covariates are drawn from `rnorm`; for "uniform", they are drawn from `runif` on the interval  $[-\sqrt{3}, \sqrt{3}]$  (which ensures that the covariates have unit variance regardless of which distribution is chosen).

When  $d = 0$  (i.e. no covariates), the function omits any covariate-related columns and their interactions.

## Value

An object of class "FETWFE\_simulated", which is a list containing:

**pdata** A dataframe containing generated data that can be passed to `fetwfe()`.

**X** The design matrix  $X$ , with  $p$  columns with interactions.

**y** A numeric vector of length  $N \times T$  containing the generated responses.

**covs** A character vector containing the names of the generated features (if  $d > 0$ ), or simply an empty vector (if  $d = 0$ )

**time\_var** The name of the time variable in `pdata`

**unit\_var** The name of the unit variable in `pdata`

**treatment** The name of the treatment variable in `pdata`

**response** The name of the response variable in `pdata`

**coefs** The coefficient vector  $\beta$  used for data generation.

**first\_inds** A vector of indices indicating the first treatment effect for each treated cohort.

**N\_UNTREATED** The number of never-treated units.

**assignments** A vector of counts (of length  $R + 1$ ) indicating how many units fall into the never-treated group and each of the  $R$  treated cohorts.

**indep\_counts** Independent cohort assignments (for auxiliary purposes).

**p** The number of columns in the design matrix  $X$ .

**N** Number of units.

**T** Number of time periods.

**R** Number of treated cohorts.

**d** Number of covariates.

**sig\_eps\_sq** The idiosyncratic noise variance.

**sig\_eps\_c\_sq** The unit-level noise variance.

## References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. <https://arxiv.org/abs/2312.05985>.

**Examples**

```
## Not run:
# Generate coefficients
coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

## End(Not run)
```

---

simulateDataCore

*Generate Random Panel Data for FETWFE Simulations*


---

**Description**

Generates a random panel data set for simulation studies of the fused extended two-way fixed effects (FETWFE) estimator. The function creates a balanced panel with  $N$  units over  $T$  time periods, assigns treatment status across  $R$  treated cohorts (with equal marginal probabilities for treatment and non-treatment), and constructs a design matrix along with the corresponding outcome. When `gen_ints = TRUE` the full design matrix is returned (including interactions between covariates and fixed effects and treatment indicators). When `gen_ints = FALSE` the design matrix is generated in a simpler format (with no interactions) as expected by `fetwfe()`. Moreover, the covariates are generated according to the specified distribution: by default, covariates are drawn from a normal distribution; if `distribution = "uniform"`, they are drawn uniformly from  $[-\sqrt{3}, \sqrt{3}]$ .

When  $d = 0$  (i.e. no covariates), no covariate-related columns or interactions are generated.

See the simulation studies section of Faletto (2025) for details.

**Usage**

```
simulateDataCore(
  N,
  T,
  R,
  d,
  sig_eps_sq,
  sig_eps_c_sq,
  beta,
  seed = NULL,
  gen_ints = FALSE,
  distribution = "gaussian",
  guarantee_rank_condition = FALSE
)
```

**Arguments**

N	Integer. Number of units in the panel.
T	Integer. Number of time periods.
R	Integer. Number of treated cohorts (with treatment starting in periods 2 to T).
d	Integer. Number of time-invariant covariates.
sig_eps_sq	Numeric. Variance of the idiosyncratic (observation-level) noise.
sig_eps_c_sq	Numeric. Variance of the unit-level random effects.
beta	Numeric vector. Coefficient vector for data generation. Its required length depends on the value of gen_ints: <ul style="list-style-type: none"> <li>• If gen_ints = TRUE and <math>d &gt; 0</math>, the expected length is <math>p = R + (T - 1) + d + dR + d(T - 1) + num\_treats + num\_treats \times d</math>, where <math>num\_treats = T \times R - \frac{R(R+1)}{2}</math>.</li> <li>• If gen_ints = TRUE and <math>d = 0</math>, the expected length is <math>p = R + (T - 1) + num\_treats</math>.</li> <li>• If gen_ints = FALSE, the expected length is <math>p = R + (T - 1) + d + num\_treats</math>.</li> </ul>
seed	(Optional) Integer. Seed for reproducibility.
gen_ints	Logical. If TRUE, generate the full design matrix with interactions; if FALSE (the default), generate a design matrix without any interaction terms.
distribution	Character. Distribution to generate covariates. Defaults to "gaussian". If set to "uniform", covariates are drawn uniformly from $[-\sqrt{3}, \sqrt{3}]$ .
guarantee_rank_condition	(Optional). Logical. If TRUE, the returned data set is guaranteed to have at least $d + 1$ units per cohort, which is necessary for the final design matrix to have full column rank. Default is FALSE, in which case no such condition is enforced.

**Details**

When `gen_ints = TRUE`, the function constructs the design matrix by first generating base fixed effects and a long-format covariate matrix (via `generateBaseEffects()`), then appending interactions between the covariates and cohort/time fixed effects (via `generateFEInts()`) and finally treatment indicator columns and treatment-covariate interactions (via `genTreatVarsSim()` and `genTreatInts()`). When `gen_ints = FALSE`, the design matrix consists only of the base fixed effects, covariates, and treatment indicators.

The argument `distribution` controls the generation of covariates. For "gaussian", covariates are drawn from `rnorm`; for "uniform", they are drawn from `runif` on the interval  $[-\sqrt{3}, \sqrt{3}]$ .

When  $d = 0$  (i.e. no covariates), the function omits any covariate-related columns and their interactions.

**Value**

An object of class "FETWFE\_simulated", which is a list containing:

**pdata** A dataframe containing generated data that can be passed to `fetwfe()`.

- X** The design matrix. When `gen_ints = TRUE`,  $X$  has  $p$  columns with interactions; when `gen_ints = FALSE`,  $X$  has no interactions.
- y** A numeric vector of length  $N \times T$  containing the generated responses.
- covs** A character vector containing the names of the generated features (if  $d > 0$ ), or simply an empty vector (if  $d = 0$ )
- time\_var** The name of the time variable in `pdata`
- unit\_var** The name of the unit variable in `pdata`
- treatment** The name of the treatment variable in `pdata`
- response** The name of the response variable in `pdata`
- coefs** The coefficient vector  $\beta$  used for data generation.
- first\_inds** A vector of indices indicating the first treatment effect for each treated cohort.
- N\_UNTREATED** The number of never-treated units.
- assignments** A vector of counts (of length  $R + 1$ ) indicating how many units fall into the never-treated group and each of the  $R$  treated cohorts.
- indep\_counts** Independent cohort assignments (for auxiliary purposes).
- p** The number of columns in the design matrix  $X$ .
- N** Number of units.
- T** Number of time periods.
- R** Number of treated cohorts.
- d** Number of covariates.
- sig\_eps\_sq** The idiosyncratic noise variance.
- sig\_eps\_c\_sq** The unit-level noise variance.

## References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. <https://arxiv.org/abs/2312.05985>.

## Examples

```
## Not run:
# Set simulation parameters
N <- 100          # Number of units in the panel
T <- 5           # Number of time periods
R <- 3           # Number of treated cohorts
d <- 2           # Number of time-invariant covariates
sig_eps_sq <- 1  # Variance of observation-level noise
sig_eps_c_sq <- 0.5 # Variance of unit-level random effects

# Generate coefficient vector using genCoefsCore()
# (Here, density controls sparsity and eff_size scales nonzero entries)
coefs_core <- genCoefsCore(R = R, T = T, d = d, density = 0.2, eff_size = 2, seed = 123)

# Now simulate the data. Setting gen_ints = TRUE generates the full design
matrix with interactions.
```

```

sim_data <- simulateDataCore(
  N = N,
  T = T,
  R = R,
  d = d,
  sig_eps_sq = sig_eps_sq,
  sig_eps_c_sq = sig_eps_c_sq,
  beta = coefs_core$beta,
  seed = 456,
  gen_ints = TRUE,
  distribution = "gaussian"
)

# Examine the returned list:
str(sim_data)

## End(Not run)

```

twfeCovs

*Two-way fixed effects with covariates and separate treatment effects for each cohort*

## Description

**WARNING: This function should NOT be used for estimation. It is a biased estimator of treatment effects.** Implementation of two-way fixed effects with covariates and separate treatment effects for each cohort. Estimates overall ATT as well as CATT (cohort average treatment effects on the treated units). It is implemented only for the sake of the simulation studies in Faleto (2025). This estimator is only unbiased under the assumptions that treatment effects are homogeneous across covariates and are identical within cohorts across all times since treatment.

## Usage

```

twfeCovs(
  pdata,
  time_var,
  unit_var,
  treatment,
  response,
  covs = c(),
  indep_counts = NA,
  sig_eps_sq = NA,
  sig_eps_c_sq = NA,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)

```

**Arguments**

<code>pdata</code>	Dataframe; the panel data set. Each row should represent an observation of a unit at a time. Should contain columns as described below.
<code>time_var</code>	Character; the name of a single column containing a variable for the time period. This column is expected to contain integer values (for example, years). Recommended encodings for dates include format YYYY, YYYYMM, or YYYYM-MDD, whichever is appropriate for your data.
<code>unit_var</code>	Character; the name of a single column containing a variable for each unit. This column is expected to contain character values (i.e. the "name" of each unit).
<code>treatment</code>	Character; the name of a single column containing a variable for the treatment dummy indicator. This column is expected to contain integer values, and in particular, should equal 0 if the unit was untreated at that time and 1 otherwise. Treatment should be an absorbing state; that is, if unit $i$ is treated at time $t$ , then it must also be treated at all times $t + 1, \dots, T$ . Any units treated in the first time period will be removed automatically. Please make sure yourself that at least some units remain untreated at the final time period ("never-treated units").
<code>response</code>	Character; the name of a single column containing the response for each unit at each time. The response must be an integer or numeric value.
<code>covs</code>	(Optional.) Character; a vector containing the names of the columns for covariates. All of these columns are expected to contain integer, numeric, or factor values, and any categorical values will be automatically encoded as binary indicators. If no covariates are provided, the treatment effect estimation will proceed, but it will only be valid under unconditional versions of the parallel trends and no anticipation assumptions. Default is <code>c()</code> .
<code>indep_counts</code>	(Optional.) Integer; a vector. If you have a sufficiently large number of units, you can optionally randomly split your data set in half (with $N$ units in each data set). The data for half of the units should go in the <code>pdata</code> argument provided above. For the other $N$ units, simply provide the counts for how many units appear in the untreated cohort plus each of the other $R$ cohorts in this argument <code>indep_counts</code> . The benefit of doing this is that the standard error for the average treatment effect will be (asymptotically) exact instead of conservative. The length of <code>indep_counts</code> must equal 1 plus the number of treated cohorts in <code>pdata</code> . All entries of <code>indep_counts</code> must be strictly positive (if you are concerned that this might not work out, maybe your data set is on the small side and it's best to just leave your full data set in <code>pdata</code> ). The sum of all the counts in <code>indep_counts</code> must match the total number of units in <code>pdata</code> . Default is NA (in which case conservative standard errors will be calculated if $q < 1$ .)
<code>sig_eps_sq</code>	(Optional.) Numeric; the variance of the row-level IID noise assumed to apply to each observation. See Section 2 of Falletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.
<code>sig_eps_c_sq</code>	(Optional.) Numeric; the variance of the unit-level IID noise (random effects) assumed to apply to each observation. See Section 2 of Falletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using

	simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.
verbose	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.
alpha	Numeric; function will calculate $(1 - \alpha)$ confidence intervals for the cohort average treatment effects that will be returned in <code>catt_df</code> .
add_ridge	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

### Value

A named list with the following elements:

att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	A standard error for the ATT. If the Gram matrix is not invertible, this will be NA.
catt_hats	A named vector containing the estimated average treatment effects for each cohort.
catt_ses	A named vector containing the (asymptotically exact) standard errors for the estimated average treatment effects within each cohort.
cohort_probs	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating <code>att_hat</code> . If <code>indep_counts</code> was provided, <code>cohort_probs</code> was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in <code>pdata</code> .
catt_df	A dataframe displaying the cohort names, average treatment effects, standard errors, and $1 - \alpha$ confidence interval bounds.
beta_hat	The full vector of estimated coefficients.
treat_inds	The indices of <code>beta_hat</code> corresponding to the treatment effects for each cohort at each time.
treat_int_inds	The indices of <code>beta_hat</code> corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
sig_eps_sq	Either the provided <code>sig_eps_sq</code> or the estimated one, if a value wasn't provided.
sig_eps_c_sq	Either the provided <code>sig_eps_c_sq</code> or the estimated one, if a value wasn't provided.
X_ints	The design matrix created containing all interactions, time and cohort dummies, etc.
y	The vector of responses, containing <code>nrow(X_ints)</code> entries.
X_final	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
y_final	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.

N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
T	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.
d	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
p	The final number of columns in the full set of covariates used to estimate the model.

**Author(s)**

Gregory Faletto

**References**

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. <https://arxiv.org/abs/2312.05985>.

---

twfeCovsWithSimulatedData

*Run twfeCovs on Simulated Data*

---

**Description**

This function runs the bridge-penalized extended two-way fixed effects estimator (`twfeCovs()`) on simulated data. It is simply a wrapper for `twfeCovs()`: it accepts an object of class "FETWFE\_simulated" (produced by `simulateData()`) and unpacks the necessary components to pass to `twfeCovs()`. So the outputs match `twfeCovs()`, and the needed inputs match their counterparts in `twfeCovs()`.

**Usage**

```
twfeCovsWithSimulatedData(
  simulated_obj,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)
```

**Arguments**

<code>simulated_obj</code>	An object of class "FETWFE_simulated" containing the simulated panel data and design matrix.
<code>verbose</code>	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.

alpha	Numeric; function will calculate $(1 - \alpha)$ confidence intervals for the cohort average treatment effects that will be returned in <code>catt_df</code> .
add_ridge	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

**Value**

A named list with the following elements:

att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	If $q < 1$ , a standard error for the ATT. If <code>indep_counts</code> was provided, this standard error is asymptotically exact; if not, it is asymptotically conservative. If $q \geq 1$ , this will be NA.
catt_hats	A named vector containing the estimated average treatment effects for each cohort.
catt_ses	If $q < 1$ , a named vector containing the (asymptotically exact, non-conservative) standard errors for the estimated average treatment effects within each cohort.
cohort_probs	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating <code>att_hat</code> . If <code>indep_counts</code> was provided, <code>cohort_probs</code> was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in <code>pdata</code> .
catt_df	A dataframe displaying the cohort names, average treatment effects, standard errors, and $1 - \alpha$ confidence interval bounds.
beta_hat	The full vector of estimated coefficients.
treat_inds	The indices of <code>beta_hat</code> corresponding to the treatment effects for each cohort at each time.
treat_int_inds	The indices of <code>beta_hat</code> corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
sig_eps_sq	Either the provided <code>sig_eps_sq</code> or the estimated one, if a value wasn't provided.
sig_eps_c_sq	Either the provided <code>sig_eps_c_sq</code> or the estimated one, if a value wasn't provided.
X_ints	The design matrix created containing all interactions, time and cohort dummies, etc.
y	The vector of responses, containing <code>nrow(X_ints)</code> entries.
X_final	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
y_final	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
T	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.

- d            The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
- p            The final number of columns in the full set of covariates used to estimate the model.

**Examples**

```
## Not run:  
# Generate coefficients  
coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)  
  
# Simulate data using the coefficients  
sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)  
  
result <- twfeCovsWithSimulatedData(sim_data)  
  
## End(Not run)
```

# Index

attgtToFetwfeDf, [2](#)

betwfe, [4](#)

betwfeWithSimulatedData, [9](#)

etwfe, [12](#)

etwfe-class, [15](#)

etwfeToFetwfeDf, [15](#)

etwfeWithSimulatedData, [17](#)

fetwfe, [19](#)

fetwfe-class, [24](#)

fetwfeWithSimulatedData, [24](#)

genCoefs, [27](#)

genCoefsCore, [29](#)

getTes, [30](#)

simulateData, [32](#)

simulateDataCore, [34](#)

twfeCovs, [37](#)

twfeCovsWithSimulatedData, [40](#)