

# Package ‘hbim’

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**Title** Hill/Bliss Independence Model for Combination Vaccines

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**Description** Calculate expected relative risk and proportion protected assuming normally distributed log10 transformed antibody dose for a several component vaccine. Uses Hill models for each component which are combined under Bliss independence. See Saul and Fay, 2007 <[DOI:10.1371/journal.pone.0000850](https://doi.org/10.1371/journal.pone.0000850)>.

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 hbim-package

*Hill/Bliss Independence Model for Multicomponent Vaccines*


---

### Description

Calculate expected relative risk and proportion protected assuming normally distributed log10 transformed antibody dose for several component vaccine. Uses Hill models for each component which are combined under Bliss independence. (see Saul and Fay (2007) <doi:10.1371/journal.pone.0000850>).

### Details

The hbim package allows users to reproduce plots and calculations for Saul and Fay (2007). See vignette("hbimdetails").

### Author(s)

M.P. Fay, Maintainer: Michael Fay <mfay@niaid.nih.gov>

### References

Saul A, Fay MP (2007). Human Immunity and the Design of Multi-Component, Single Target Vaccines. PLoS ONE 2(9): e850. doi:10.1371/journal.pone.0000850

---

 calc.foldrange

*Calculate standard error and fold-range from confidence interval*


---

### Description

Given a confidence interval and sample size, we find the standard error assuming confidence limits are calculated on the log10 responses by either normal confidence limits or t-distribution confidence limits. The fold-range is also output by either methods.

### Usage

```
calc.foldrange(n, lower, upper, conf.level = 0.95)
```

### Arguments

n	vector of sample size(s) used to create confidence intervals
lower	vector of lower confidence limits
upper	vector of upper confidence limits
conf.level	confidence level, default=.95

### Details

See vignette("hbimdetails")

**Value**

A vector (or matrix) with elements (or columns)

n	sample size
lower	lower confidence limit
upper	upper confidence limit
s.byt	standard deviation assuming confidence intervals calculated by t-distribution
s.byz	standard deviation assuming confidence intervals calculated by normal distribution
foldrange.byt	fold-range assuming confidence intervals calculated by t-distribution
foldrange.byz	fold-range assuming confidence intervals calculated by normal distribution

**Examples**

```
## sample size=43, lower cl=65, upper cl=85
calc.foldrange(43,65,85)
```

---

deff.sigma

*HBIM data*

---

**Description**

These 6 data sets were calculated using the associated function. For example, `deff.sigma` was calculated with `eff.sigma`. The 3 data sets that begin with `deff`, give the expected efficacy for several values of  $\mu$ . The 3 data sets that begin with `dpp` give the percent protected with several values of  $\mu$ . The data sets that end in `.sigma` change for different values of  $\sigma$ , and similarly for `.mu` and `.rho` (see `deff.sigma`).

**Usage**

```
data(deff.sigma)
data(deff.mu)
data(deff.rho)
data(dpp.sigma)
data(dpp.mu)
data(dpp.rho)
```

**Format**

The format is: List of 8

- $\mu$  vector of different values of mean for log10 antibody
- out1 matrix of either expected efficacy or percent protected for 1 component model, rows correspond to  $\mu$ , cols correspond to `cparms`

- out2matrix of either expected efficacy or percent protected for 2 component model, rows correspond to mu, cols correspond to cparms
- out3matrix of either expected efficacy or percent protected for 3 component model, rows correspond to mu, cols correspond to cparms
- col1vector of colors for different cparms of 1 component model
- col2vector of colors for different cparms of 2 component model
- col3vector of colors for different cparms of 3 component model
- cparmsvector parameters that change

### Examples

```
## here is the code that produces the 6 data sets, it takes about 25 hours to run
## so it is commented out here
#NSIM<-5*10^5
#SIGMAS.POWER<-c(9,65,5000)
#SIGMAS<-log10(SIGMAS.POWER)/(2*qnorm(.975))
#SCOLORS<-c("green","blue","red")
#FACTORS<-c(1/10, 1/3, 1/2, 1)
#FCOLORS<-c("red", "green", "blue", "black")
#RHOS<-c(-.5,-.25,0, 0.25, 0.5, 0.75, 1)
#RCOLORS<- c("black","tan","yellow","blue", "green", "red", "black")
#set.seed(1234521)
#MU<-((-40:40)/10)
#deff.sigma<-eff.sigma(mu=MU, sigmas=SIGMAS, COLORS = SCOLORS, rho = 0)
#deff.mu<-eff.mu(mu=MU, factor = FACTORS, COLORS = FCOLORS, sigma = SIGMAS[2], rho = 0)
#deff.rho<-eff.rho(mu=MU, sigma = SIGMAS[2], rho = RHOS, COLORS =RCOLORS,simulate=TRUE,nsim=NSIM)
#set.seed(32401)
#dpp.sigma<-pp.sigma(MU,sigmas=SIGMAS,COLORS = SCOLORS, rho = 0,nsim=NSIM)
#set.seed(21345123)
#dpp.mu<-pp.mu(MU,factor = FACTORS, COLORS = FCOLORS, sigma = SIGMAS[2], rho = 0, nsim=NSIM)
#set.seed(435919)
#dpp.rho<-pp.rho(MU,sigma = SIGMAS[2], rho = RHOS, COLORS =RCOLORS,nsim=NSIM)
```

---

eff.mu

*Create data sets for plots*

---

### Description

These functions create the data sets used in the plots. The first part of the name denotes the output created. Thus, `eff.sigma`, `eff.mu`, `eff.rho` create efficacy values, while `pp.sigma`, `pp.mu`, `pp.rho` create percent protected values. The second part of the name is the parameter which is changed. For example, `eff.sigma` creates efficacy values for different values of `sigma`. See details for a more complete description. Default for `eff.` functions is integration, default for `pp.` functions is simulation.

**Usage**

```

eff.sigma(mu, sigmas, COLORS = c("red", "green", "blue"),
  rho = 0, ...)
eff.mu(mu, factor = c(1/10, 1/3, 1/2, 1),
  COLORS = c("red", "green", "blue", "black"),
  sigma = 0.553, rho = 0, ...)
eff.rho(mu, sigma = 0.553, rho = c(0, 0.25, 0.5, 0.75, 1),
  COLORS = c("black", "blue", "green", "red", "black"), ...)
pp.sigma(mu, sigmas, COLORS = c("red", "green", "blue"),
  rho = 0, nsim = 10^5)
pp.mu(mu, factor = c(1/10,1/3,1/2,1),
  COLORS = c("red", "green", "blue", "black"),
  sigma = 0.553, rho = 0, nsim = 10^5)
pp.rho(mu, sigma = 0.553, rho = c(0, 0.25, 0.5, 0.75, 1),
  COLORS = c("black", "blue", "green", "red", "black"),
  nsim = 10^5)

```

**Arguments**

mu	a vector of values of the mean of the log10 antibody
factor	a vector of values for defining the means of the second and third component (see details and warnings)
COLORS	colors for the plots, the ith color corresponds to the ith value of the parameter which is changing
sigmas	a vector of values of the standard deviation of the log10 antibody
sigma	a single value for sigma
rho	correlation vector (of length one for .sigma and .mu functions) of the log10 antibody, negative values not allowed
nsim	number of simulations for hbpp function
...	additional parameters may be added to the <a href="#">hbrr</a> function

**Details**

For `eff.sigma` and `pp.sigma` we change sigma over the one, two, and three component model. For `eff.mu` and `pp.mu` we change the mean over the two and three component model. For `eff.mu` and `pp.mu` the factor parameter is associated with each level of the second and third component. See `vignette("hbimdetails")` for details. For `eff.rho` and `pp.rho` we change the correlation over the two and three component model; for the jth column of the out2 and out3 matrices, all correlations are given by jth level of factor. Because these calculations may take hours, we save the original calculations used in the paper as output data, `deff.sigma`, `deff.mu`, `deff.rho`, `dpp.sigma`, `dpp.mu`, and `dpp.rho`. These output data set may be accessed by the command `data()`. For example, to access `deff.sigma` type `data(deff.sigma)`.

**Value**

A list with items

out1	response matrix for one component model, ith row corresponds to mu[i] and jth column corresponds to the jth level of the parameter which is changing
col1	colors corresponding to columns of out1
out2	response matrix for two component model, ith row corresponds to mu[i] and jth column corresponds to the jth level of the parameter which is changing
col2	colors corresponding to columns of out2
out3	response matrix for three component model, ith row corresponds to mu[i] and jth column corresponds to the jth level of the parameter which is changing
col3	colors corresponding to columns of out3
cparms	input vector of parameter that changes, e.g., factor vector
sigma	input sigma
rho	input rho

### Warning

Note to save computation time these functions do not check that all variance-covariance matrices used in the internal functions are positive definite. If you get an error message you do not understand check to see if the variance-covariance matrix is positive definite by checking the eigen values. For example, with `sigma=1`, `rho=-.6`, the 3 components model do not have a positive definite variance-covariance matrix because there is a negative eigenvalue (to see this run `eigen(make.v(3, -.6, 1))`).

### Author(s)

M.P. Fay

### See Also

`vignette("hbimdetails")`

---

equiv.ab

*Equivalent antibody calculations by Linear Interpolation*

---

### Description

This function inputs two antibody by response curves and outputs values needed for plots of equivalent antibody response. This is called by other functions ([plotresp.equiv](#), [plotresp.mix](#)). It is not to be called directly. For that purpose use [equiv.increase](#).

### Usage

```
equiv.ab(effab1, ab1, effab2, ab2, npts = 100)
```

**Arguments**

effab1	vector of responses for antibody 1
ab1	vector of doses of antibody 1
effab2	vector of responses for antibody 2
ab2	vector of doses of antibody 2
npts	number of points used in some output

**Details**

The function uses the [approx](#) function to do linear interpolation and find the needed values.

**Value**

A list containing:

abpts	a vector of values of antibody dose
abpts10	antilog of abpts, i.e., abpts raised to tenth power
equiv.eff2	equivalent response of antibody 2
equiv.eff1	equivalent response of antibody 1
equiv.ab1	vector of antibody doses that correspond with equiv.eff1
x	equiv.ab1-abpts
y	equiv.eff1

**See Also**

[equiv.increase](#)

---

equiv.increase	<i>Calculate equivalent increase from two dose-response curves</i>
----------------	--

---

**Description**

This function takes two curves defined by vectors of x and y values and calculates the equivalent increase in the x value at the response value for the first curve at e1.

**Usage**

```
equiv.increase(x1, y1, x2, y2, e1, xlog = TRUE)
```

**Arguments**

x1	x vector for first curve
y1	y vector for first curve
x2	x vector for second curve
y2	y vector for second curve
e1	vector of y responses of first curve for associating with output
xlog	TRUE if x values are log transformed, changes the output

**Details**

The function repeatedly uses the [approx](#) function to do linear interpolation.

**Value**

A list with 5 components

a1	vector of x values associated with e1 from first curve
e2	vector of y values associated with a1 from the second curve
a2	vector of x values associated with e2 from the second curve
e1	input vector for e1
equiv.increase	vector of equivalent increases associated with e1

**Examples**

```
data(deff.sigma)
D<-deff.sigma
equiv.increase(D$mu,D$out1[,2],D$mu,D$out2[,2],.5)
```

---

hbrr	<i>Calculate expected relative risk or percent protected from Hill model with Bliss Independence</i>
------	--

---

**Description**

Assuming that the log10 transformed doses are normally distributed, we calculate the expected relative risk (using hbrr) or percent protected (using hbpp) from the Hill model using Bliss Independence. Numeric integration is the default for up to three components for hbrr, while simulation is the default for two or three components for hbpp.

**Usage**

```
hbrr(mu, v, a = rep(1, length(mu)), simulate = FALSE, nsim = 10^4, ...)
hbpp(mu, v, a = rep(1, length(mu)), rp = 0.1, simulate = FALSE, nsim = 10^5, ...)
```

**Arguments**

<code>mu</code>	mean vector of the log10 dose
<code>v</code>	variance matrix of the log10 dose
<code>a</code>	vector of slope parameters in the Hill model, one for each component
<code>simulate</code>	estimation by simulation (TRUE) or numeric integration (FALSE)
<code>nsim</code>	number of simulations, ignored if <code>simulate=FALSE</code>
<code>rp</code>	protection bound, an individual is protected if relative risk is greater than <code>rp</code>
<code>...</code>	additional parameters to pass to the <code>integrate</code> function

**Details**

Although the package `adapt` can do multidimensional integration, we have written specific functions to do this for up to 3 dimensions. This allows faster and more accurate integration. The integration is done by repeated calls to the `integrate` function. The functions which do the actual integration or simulation are internal functions which are not intended to be called by the user. These internal functions are: for `hbr`, when `simulate=FALSE`, the function calls one of either `hbr.integrate1`, `hbr.integrate2`, `hbr.integrate2.rhoeq1`, `hbr.integrate3`, or `hbr.integrate3.rhoeq1` (for 1,2, or 3 component, with or without `rho=1`, taken from the size of the `mu` vector and dimension of the `v` matrix) and when `simulation=TRUE` it calls `hbr.simulate`. Similar functions exist for `hbpp`; however, the `hbpp.integrate2` and `hbpp.integrate3` may have problems because of the discontinuity in the integration function. That is why for two or three component models `hbpp.simulate` is used by default.

**Value**

a numeric value of the expected relative risk or percent protected.

**Author(s)**

M.P. Fay

**References**

Saul A, Fay MP (2007). Human Immunity and the Design of Multi-Component, Single Target Vaccines. PLoS ONE 2(9): e850. doi:10.1371/journal.pone.0000850

**Examples**

```
## example of two dimensional integral
hbr(c(.123, .432), matrix(c(1, .5, .5, 1), 2, 2))
## faster but less accurate estimation by simulation
hbr(c(.123, .432), matrix(c(1, .5, .5, 1), 2, 2), simulate=TRUE, nsim=10^4)
```

---

 irdata
 

---



---

*Immune Response data*


---

**Description**

Data from literature.

**Usage**

data(irdata)

**Format**

A data frame with 574 observations on the following 16 variables.

RecordNum a numeric vector

Old.Reference a numeric vector

Reference a numeric vector

Vaccine.and.trial.group a factor with levels (Pentacel +Recombivax) then Prevnar 11 valent Pneumococcal-DT Finland 11 valent Pneumococcal-DT Israel 11 valent Pneumococcal-DT+alum Finland 11 valent Pneumococcal-DT+alum Israel 11 valent Pneumococcal-DT+alum Philippines ACTHIB AP-YF AVA IMAVA SQ BERNA-YF Boostrix Boostrix + Poliorix Boostrix Polio (dTpa-IPV) DPaT-HVB-IPV/HIB mix DPaT-HVB-IPV+HIB separate DPaT-IPV/HiB mix DPaT-IPV+HiB separately DPT +Hib/HBV DPT +Hib + HBV DPTa DPTa/Pa DPTa5 DT DTP-HB + Hib DTPa-HBV DTPa/IPV/PRP-TT +PncD/T11 DTPa2 DTPa3 DTPa5 DTPaHBV-IPV+Hib DTPaHBV-IPV+Hib, PRP DTPaHBV-IPV+Hib, PRP-TT DTPw-C DTPw-E DTPw/IPV/PRP-TT +PncD/T11 group 1 DTPw/IPV/PRP-TT +PncD/T11 group 2 DTPwHBV-Hib DTPwHBV + Hib (Separate) Engerix B GBS Ia-TT 15 ug GBS Ia-TT 3.75 ug GBS Ia 55 ug GBS IaTT 60 ug GBS Ib-TT 15.75 ug GBS Ib-TT 3.94 ug GBS Ib-TT 63 ug GBS Ib 53 ug GBS II-TT GBS II-TT 14.3 ug GBS II-TT 3.6 ug GBS II-TT 57 ug GBS II-TT/III-TT GBS III-TT GBS III-TT 14.5 ug GBS III-TT 3.6 ug GBS III-TT 58 ug GBS III 50 ug GBS V-CRM197 GBS V-TT GBS V-TT 2.4/1.1 ug GBS V-TT 38.5/17 ug GBS V-TT 9.6/4.3 ug H5N1Influenza 45ug H5N1Influenza 7.5ug H5N1Influenza 90ug H5N1Influenza 15ug H5N1Influenza Placebo Havrix+Engerix B HBV/Pentavax Heptavalent Pneumococcal-CMR197 Heptavalent Pneumococcal-OMPC Heptavalent Pneumococcal-CMR197 Hiberix HibTITER HibTITER (PRP-CRM197) Infanrix-IVP+Hib Infanrix-IVP+Hib+Prevnar Infanrix + Engerix separate Infanrix/Engerix Mixed Infanrix/Engerix Mixed IPV-mkc IPV-vero Lyme OspA 15ug Lyme OspA 30ug LYMERix (OpsA) MCV4-DT Menactra Meningococcal PS-DT (MCV-4) Mencevax ACWY Meningitec (Menc-CRM197) Menomune Meningococcal PS Menomune Meningococcal PS (PSV-4) Octavalent Pneumococcal-DT Octavalent Pneumococcal-TT Oka/Merck varicella 16K PFU +M-M-R Oka/Merck varicella 50K PFU +M-M-R OpsA Lyme Disease Orimmune OspA Lyme Pentacel + Prevnar +Recombivax Pentavax Revaxis (Td-IPV) RKI-YF RSV PFP3 Tripedia Tripedia-Orimmune-HibTITER Twinrix Twinrix adult Twinrix pediatric Typhoid/HAV Varilrix + M-M-R

Carrier.for.conjugate.vaccines a factor with levels CRM197 Diphtheria toxoid OMPC Tetanus protein Tetanus toxoid

Age.in.yrs.at.first.vaccination a factor with levels 0.12 0.17 0.17-0.5 0.25 0.5 1 1-12  
 1-2 1.5 11-18 12-15 15-18 15-70 16-65 17-72 18-32 18-39 18-40 18-45 18-50 18-60  
 18-64 19-52 19-56 19-57 19-64 19-70 19-83 2 2-5 20-45 20-60 20-61 21-60 3 4 4-14  
 40-70 5-16 65-83

Dose.schedule.in.weeks a factor with levels 0 0, 2 0, 2, 4 0, 26 0, 26/0, 4, 26 0, 4 0, 4, 10  
 0, 4, 26 0, 4, 52 0, 4, 8 0, 4, 8, 52 0, 52 0, 52, 104 0, 6, 13 0, 8 0, 8, 16 0, 8, 18 0,  
 8, 18 0, 8, 18, 220 0, 8, 18, 270 0, 8, 18, 320 0, 8, 18, 44 0, 8, 18, 56 0, 8, 18, 60  
 0, 8, 18, 70 0, 8, 18; 4,12,22 0, 8, 18; 4,12,22 0, 8, 39 0, 9, 37

Num.Immunizations a numeric vector

Endpoint.in.weeks.after.first.vaccine a numeric vector

Antigen a factor with levels 1 14 18C 19F 23F 3 4 5 6B 7F 9V A AVA C DT F protein FHA FIM HAV  
 HBs Hemagglutinin Ia-CPS Ib-CPS II-CPS III-CPS Measles MenC Mumps OspA Polio-1  
 Polio-2 Polio-3 PRN PRP PRP\* PT Rubella TT V-CPS Varicella Vi W135 Y YF

Units a factor with levels EL.U/mL EU HI IU mIU ng SBA ug

GMT a numeric vector

GMT.95.pct.interval.low.limit a numeric vector

GMT.95.pct.interval.high.limit a numeric vector

n a numeric vector

Fold.Range a numeric vector

## Source

See data(refs) for references

## Examples

```
data(irdata)
irdata[1,]
```

---

make.v *Make Exchangeable Variance Matrix*

---

## Description

Not to be called directly. Used by [eff.sigma](#), [eff.mu](#), [eff.rho](#), [pp.sigma](#), [pp.mu](#), and [pp.rho](#).

## Usage

```
make.v(n, r, sig2)
```

## Arguments

n	dimension of variance matrix
r	correlation
sig2	variance

**Value**

An variance-covariance matrix, with all diagonal elements equal and all off diagonal elements equal.

---

plotlogm.resp	<i>Plot Hill/Bliss Independence Model Data.</i>
---------------	---

---

**Description**

These functions take data output calculated from the data generating functions (see details) and plot either: the mean of the log transformed antibody doses by the response (plotlogm.resp), equivalent increase in antibody plots (plotresp.equiv), or response of one component versus a mixture (for details see vignette("hbimdetails")).

**Usage**

```
plotlogm.resp(D, YLAB = "Efficacy", YLIM = c(0, 1),
              XLIM = c(-2, 2), TITLE = "")
plotresp.equiv(D, XLIM = c(0, 1), YLIM = c(1, 100),
               RLAB = "Efficacy of", bounds = XLIM, TITLE = "")
plotresp.mix(D, RLAB = "Efficacy of", XYLIM = c(0, 1), TITLE = "")
```

**Arguments**

D	data, see details
YLAB	y label
YLIM	range of y axis
XLIM	range of x axis
RLAB	response label, currently use only either "Efficacy of" or "% Protected by"
bounds	bounds on response of second antibody curve, see vignette("hbimdetails")
XYLIM	range of both x and y axes
TITLE	title of plot

**Details**

The following functions create data sets for plotting: [eff.sigma](#), [eff.mu](#), [eff.rho](#), [pp.sigma](#), [pp.mu](#), [pp.rho](#). These functions plot that data. For details see vignette("hbimdetails").

**Value**

Plots

---

refs

*Reference list*

---

**Description**

Each reference is one long character string. See `data(irdata)` for data from each reference.

**Usage**

```
data(refs)
```

**Format**

The format is: Factor w/ 50 levels (the 50 references)

**Examples**

```
data(refs)
refs[1]
```

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