

# Package ‘lancor’

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**Type** Package

**Title** Statistical Inference via Lancaster Correlation

**Version** 0.1.3

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## Description

Implementation of the methods described in Holzmann, Klar (2024) <[doi:10.1111/sjos.12733](https://doi.org/10.1111/sjos.12733)>. Lancaster correlation is a correlation coefficient which equals the absolute value of the Pearson correlation for the bivariate normal distribution, and is equal to or slightly less than the maximum correlation coefficient for a variety of bivariate distributions. Rank and moment-based estimators and corresponding confidence intervals are implemented, as well as independence tests based on these statistics.

**Imports** arrangements, boot, graphics, sn, stats

**License** GPL-2

**Encoding** UTF-8

**RoxygenNote** 7.3.2

**Suggests** testthat (>= 3.0.0)

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lcor	<i>Lancaster correlation</i>
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### Description

Computes the Lancaster correlation coefficient.

### Usage

```
lcor(x, y = NULL, type = c("rank", "linear"))
```

### Arguments

x	a numeric vector, or a matrix or data frame with two columns.
y	NULL (default) or a vector with same length as x.
type	a character string indicating which lancaster correlation is to be computed. One of "rank" (default), or "linear": can be abbreviated.

### Details

Let  $F_X$  and  $F_Y$  be the distribution functions of  $X$  and  $Y$ , and define

$$X^* = \Phi^{-1}(F_X(X)), \quad Y^* = \Phi^{-1}(F_Y(Y)),$$

where  $\Phi^{-1}$  is the standard normal quantile function. Furthermore for  $X$  and  $Y$  with finite fourth moment, let

$$\tilde{X} = (X - \mathbb{E}(X))/\text{sd}(X), \quad \tilde{Y} = (Y - \mathbb{E}(Y))/\text{sd}(Y).$$

Then

$$\rho_L(X, Y) = \max\{|\text{Cor}_{\text{Pearson}}(X^*, Y^*)|, |\text{Cor}_{\text{Pearson}}((X^*)^2, (Y^*)^2)|\}$$

and

$$\rho_{L,1}(X, Y) = \max\{|\text{Cor}_{\text{Pearson}}(X, Y)|, |\text{Cor}_{\text{Pearson}}((\tilde{X})^2, (\tilde{Y})^2)|\}$$

are called the Lancaster correlation coefficient and the linear Lancaster correlation coefficient, respectively. Two estimation methods are supported:

- **Linear estimator for  $\rho_{L,1}$**  (type = "linear"): Consider  $\rho_{L1} = \text{Cor}_{\text{Pearson}}(X, Y)$  and  $\rho_{L2} = \text{Cor}_{\text{Pearson}}((\tilde{X})^2, (\tilde{Y})^2)$ . Let  $\hat{\rho}_{L1}$  be the sample Pearson correlation and  $\hat{\rho}_{L2}$  the empirical correlation of the squares of the empirically standardized observations, and set  $\hat{\rho}_{L,1} = \max\{|\hat{\rho}_{L1}|, |\hat{\rho}_{L2}|\}$ .
- **Rank-based estimator for  $\rho_L$**  (type = "rank"): Consider  $\rho_{R1} = \text{Cor}_{\text{Pearson}}(X^*, Y^*)$  and  $\rho_{R2} = \text{Cor}_{\text{Pearson}}((X^*)^2, (Y^*)^2)$ . Let  $Q_i$  and  $R_i$  be the ranks of  $X_i$  and  $Y_i$ , within  $X_1, \dots, X_n$  or  $Y_1, \dots, Y_n$  respectively. Define

$$\hat{\rho}_{R1} = \frac{1}{n s_a^2} \sum_{j=1}^n a(Q_j) a(R_j),$$

$$\hat{\rho}_{R2} = \frac{1}{n s_b^2} \sum_{j=1}^n (b(Q_j) - \bar{b}) (b(R_j) - \bar{b}),$$

where the scores are, for  $j = 1, \dots, n$ ,

$$a(j) = \Phi^{-1}\left(\frac{j}{n+1}\right), \quad b(j) = a(j)^2,$$

$$\bar{b} = \frac{1}{n} \sum_{j=1}^n b(j), \quad s_a^2 = \frac{1}{n} \sum_{j=1}^n (a(j) - \bar{a})^2, \quad s_b^2 = \frac{1}{n} \sum_{j=1}^n (b(j) - \bar{b})^2.$$

Finally, the rank-based Lancaster correlation is

$$\hat{\rho}_L = \max\{|\hat{\rho}_{R1}|, |\hat{\rho}_{R2}|\}.$$

### Value

the sample Lancaster correlation.

### Author(s)

Hajo Holzmann, Bernhard Klar

### References

Holzmann, Klar (2024). "Lancaster correlation - a new dependence measure linked to maximum correlation". doi:10.1111/sjos.12733

### See Also

[lcor.comp](#), [lcor.ci](#), [lcor.test](#)

### Examples

```
Sigma <- matrix(c(1,0.1,0.1,1), ncol=2)
R <- chol(Sigma)
n <- 1000
x <- matrix(rnorm(n*2), n)
lcor(x, type = "rank")
lcor(x, type = "linear")

x <- matrix(rnorm(n*2), n)
nu <- 2
y <- x / sqrt(rchisq(n, nu)/nu)
cor(y[,1], y[,2], method = "spearman")
lcor(y, type = "rank")
```

lcor.ci

*Confidence intervals for the Lancaster correlation coefficient***Description**

Computes confidence intervals for the Lancaster correlation coefficient. Lancaster correlation is a bivariate measures of dependence.

**Usage**

```
lcor.ci(
  x,
  y = NULL,
  conf.level = 0.95,
  type = c("rank", "linear"),
  con = TRUE,
  R = 1000,
  method = c("plugin", "boot", "pretest")
)
```

**Arguments**

x	a numeric vector, or a matrix or data frame with two columns.
y	NULL (default) or a vector with same length as x.
conf.level	confidence level of the interval.
type	a character string indicating which lancaster correlation is to be computed. One of "rank" (default), or "linear": can be abbreviated.
con	logical; if TRUE (default), conservative asymptotic confidence intervals are computed.
R	number of bootstrap replications.
method	a character string indicating how the asymptotic covariance matrix is computed if type ="linear". One of "plugin" (default), "boot" or "symmetric": can be abbreviated.

**Details**

Computes asymptotic and bootstrap-based confidence intervals for the (linear) Lancaster correlation coefficient  $\rho_L$  ( $\rho_{L,1}$ ). For more details see [lcor](#).

Asymptotic confidence intervals are derived under two cases (analogously for  $\rho_L$ ; see Holzmann and Klar (2024)):

**Case 1:** If  $|\rho_{L1}| \neq |\rho_{L2}|$ , the  $1 - \alpha$  asymptotic interval is

$$[\max\{\hat{\rho}_{L,1} - z_{1-\alpha/2} s/\sqrt{n}, 0\}, \min\{\hat{\rho}_{L,1} + z_{1-\alpha/2} s/\sqrt{n}, 1\}],$$

where  $z_{1-\alpha/2}$  is the standard normal quantile and  $s$  is an estimator of the corresponding standard deviation.

**Case 2:** If  $|\rho_{L1}| = |\rho_{L2}| = a > 0$ , let  $\tau$  denote the correlation between the two components and let  $q_{1-\alpha/2}$  be the  $1 - \alpha/2$  quantile of the asymptotic distribution of  $\sqrt{n}(\hat{\rho}_{L,1} - a)$ . A conservative asymptotic interval is

$$[\max\{\hat{\rho}_{L,1} - q_{1-\alpha/2}/\sqrt{n}, 0\}, \min\{\hat{\rho}_{L,1} + z_{1-\alpha/2} s/\sqrt{n}, 1\}].$$

Additionally, bootstrap-based intervals can be obtained by resampling and estimating the covariance matrix of the rank or linear correlation components.

### Value

a vector containing the lower and upper limits of the confidence interval.

### Author(s)

Hajo Holzmann, Bernhard Klar

### References

Holzmann, Klar (2024). "Lancaster correlation - a new dependence measure linked to maximum correlation". doi:10.1111/sjos.12733

### See Also

[lcor](#), [lcor.comp](#), [lcor.test](#)

### Examples

```
n <- 1000
x <- matrix(rnorm(n*2), n)
nu <- 2
y <- x / sqrt(rchisq(n, nu)/nu) # multivariate t
lcor(y, type = "rank")
lcor.ci(y, type = "rank")
```

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lcor.comp

*Lancaster correlation and its components*

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### Description

Computes the Lancaster correlation coefficient and its components.

### Usage

```
lcor.comp(x, y = NULL, type = c("rank", "linear"), plot = FALSE)
```

**Arguments**

x	a numeric vector, or a matrix or data frame with two columns.
y	NULL (default) or a vector with same length as x.
type	a character string indicating which lancaster correlation is to be computed. One of "rank" (default), or "linear": can be abbreviated.
plot	logical; if TRUE, scatterplots of the transformed x and y values and of their squares are drawn.

**Details**

For more details see [lcor](#).

**Value**

a vector containing the two components rho1 and rho2 and the sample Lancaster correlation.

**Author(s)**

Hajo Holzmann, Bernhard Klar

**References**

Holzmann, Klar (2024). "Lancaster correlation - a new dependence measure linked to maximum correlation". doi:10.1111/sjos.12733

**See Also**

[lcor](#), [lcor.comp](#), [lcor.test](#)

**Examples**

```
Sigma <- matrix(c(1,0.1,0.1,1), ncol=2)
R <- chol(Sigma)
n <- 1000
x <- matrix(rnorm(n*2), n)
nu <- 8
y <- x / sqrt(rchisq(n, nu)/nu) #multivariate t
cor(y[,1], y[,2])
lcor.comp(y, type = "linear")

x <- matrix(rnorm(n*2), n)
nu <- 2
y <- x / sqrt(rchisq(n, nu)/nu) #multivariate t
cor(y[,1], y[,2], method = "spearman")
lcor.comp(y, type = "rank", plot = TRUE)
```

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lcor.test	Lancaster correlation test
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### Description

Lancaster correlation test of bivariate independence. Lancaster correlation is a bivariate measures of dependence.

### Usage

```
lcor.test(  
  x,  
  y = NULL,  
  type = c("rank", "linear"),  
  nperm = 999,  
  method = c("permutation", "asymptotic", "symmetric")  
)
```

### Arguments

x	a numeric vector, or a matrix or data frame with two columns.
y	NULL (default) or a vector with same length as x
type	a character string indicating which lancaster correlation is to be computed. One of "rank" (default), or "linear": can be abbreviated.
nperm	number of permutations.
method	a character string indicating how the p-value is computed if type="linear". One of "permutation" (default), "asymptotic" or "symmetric": can be abbreviated.

### Details

For more details on the testing procedure see *Remark 2* in Holzmann, Klar (2024).

### Value

A list containing the following components:

lcor	the value of the test statistic
pval	the p-value of the test

### Author(s)

Hajo Holzmann, Bernhard Klar

### References

Holzmann, Klar (2024). "Lancaster correlation - a new dependence measure linked to maximum correlation". [doi:10.1111/sjos.12733](https://doi.org/10.1111/sjos.12733)

**See Also**

`lcor`, `lcor.comp`, `lcor.ci` and for performing an ACE permutation test of independence see `acepack` (<https://cran.r-project.org/package=acepack>).

**Examples**

```
n <- 200
x <- matrix(rnorm(n*2), n)
nu <- 2
y <- x / sqrt(rchisq(n, nu)/nu)
cor.test(y[,1], y[,2], method = "spearman")
lcor.test(y, type = "rank")
```

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Sigma.est

*Covariance matrix of components of Lancaster correlation coefficient*

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**Description**

Estimate of covariance matrix of the two components of Lancaster correlation. Lancaster correlation is a bivariate measures of dependence.

**Usage**

```
Sigma.est(xx)
```

**Arguments**

`xx` a matrix or data frame with two columns.

**Details**

For more details see the Appendix in Holzmann, Klar (2024).

**Value**

the estimated covariance matrix.

**Author(s)**

Hajo Holzmann, Bernhard Klar

**References**

Holzmann, Klar (2024). "Lancaster correlation - a new dependence measure linked to maximum correlation". [doi:10.1111/sjos.12733](https://doi.org/10.1111/sjos.12733)

**See Also**

[lcor.ci](#)

**Examples**

```
Sigma <- matrix(c(1,0.1,0.1,1), ncol=2)
R <- chol(Sigma)
n <- 1000
x <- matrix(rnorm(n*2), n)
nu <- 8
y <- x / sqrt(rchisq(n, nu)/nu) #multivariate t
Sigma.est(y)
```

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