

Package ‘nsga2R’

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Type Package

Title Elitist Non-Dominated Sorting Genetic Algorithm

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Description Box-constrained multiobjective optimization using the elitist non-dominated sorting genetic algorithm - NSGA-II. Fast non-dominated sorting, crowding distance, tournament selection, simulated binary crossover, and polynomial mutation are called in the main program. The methods are described in Deb et al. (2002) <[doi:10.1109/4235.996017](https://doi.org/10.1109/4235.996017)>.

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`nsga2R`-package*Elitist Non-dominated Sorting Genetic Algorithm based on R*

Description

Functions for box-constrained multiobjective optimization using the elitist non-dominated sorting genetic algorithm - NSGA-II.

Details

Package: `nsga2R`
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This package provide functions for box-constrained multiobjective optimization using the elitist non-dominated sorting genetic algorithm - NSGA-II. Fast non-dominated sorting, crowding distance, tournament selection, simulated binary crossover, and polynomial mutation are called in the main program, `nsga2R`, to complete the search.

Author(s)

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References

Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002), " A fast and elitist multiobjective genetic algorithm: NSGA-II", IEEE Transactions on Evolutionary Computation, 6(2), 182-197.

`boundedPolyMutation`*Bounded Polynomial Mutation Operator*

Description

The bounded polynomial mutation operator is a real-parameter genetic operator. Like in the simulated binary crossover operator, the probability distribution is also a polynomial function instead of a normal distribution.

Usage

```
boundedPolyMutation(parent_chromosome, lowerBounds, upperBounds, mprob, mum)
```

Arguments

parent_chromosome	Mating pool with decision variables
lowerBounds	Lower bounds of each decision variable
upperBounds	Upper bounds of each decision variable
mprob	Mutation probability
mum	Mutation distribution index, it can be any nonnegative real number

Value

Return the offspring population with decision variables

Author(s)

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References

Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002), " A fast and elitist multiobjective genetic algorithm: NSGA-II", *IEEE Transactions on Evolutionary Computation*, **6(2)**, 182-197.

Examples

```
set.seed(1234)
lowerBounds <- rep(0,30)
upperBounds <- rep(1,30)
mprob <- 0.2
MutDistIdx <- 20
matingPool <- matrix(runif(1200, 0, 1), nrow=40, ncol=30)
childAfterM <- boundedPolyMutation(matingPool,lowerBounds,upperBounds,mprob,MutDistIdx)
childAfterM
```

boundedSBXover

Bounded Simulated Binary Crossover Operator

Description

The simulated binary crossover operator is a real-parameter genetic operator. It simulates the working principal of the single-point crossover operator on binary strings.

Usage

```
boundedSBXover(parent_chromosome, lowerBounds, upperBounds, cprob, mu)
```

Arguments

parent_chromosome	Mating pool with decision variables
lowerBounds	Lower bounds of each decision variable
upperBounds	Upper bounds of each decision variable
cprob	Crossover probability
mu	Crossover distribution index, it can be any nonnegative real number

Value

Return the offspring population with decision variables

Author(s)

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References

Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002), " A fast and elitist multiobjective genetic algorithm: NSGA-II", *IEEE Transactions on Evolutionary Computation*, **6(2)**, 182-197.

Examples

```
set.seed(1234)
lowerBounds <- rep(0,30)
upperBounds <- rep(1,30)
cprob <- 0.7
XoverDistIdx <- 20
matingPool <- matrix(runif(1200, 0, 1), nrow=40, ncol=30)
childAfterX <- boundedSBXover(matingPool,lowerBounds,upperBounds,cprob,XoverDistIdx)
childAfterX
```

crowdingDist4frnt

Crowding Distance Assignment for Each Front

Description

This function estimates the density of solutions surrounding a particular solution within each front. It calculates the crowding distances of solutions according to their objectives and those within the same front.

Usage

```
crowdingDist4frnt(pop, rnk, rng)
```

Arguments

pop	Population matrix including decision variables, objective functions, and non-domination rank
rnk	List of solution indices for each front
rng	Vector of each objective function range, i.e. the difference between the maximum and minimum objective function value of each objective

Value

Return a matrix of crowding distances of all solutions

Author(s)

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References

Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002), " A fast and elitist multiobjective genetic algorithm: NSGA-II", *IEEE Transactions on Evolutionary Computation*, **6(2)**, 182-197.

See Also

[fastNonDominatedSorting](#)

Examples

```
library(mco)
popSize <- 50
lowerBounds <- rep(0,30)
upperBounds <- rep(1,30)
varNo <- length(lowerBounds)
objDim <- 2
set.seed(1234)
population <- t(sapply(1:popSize, function(u) array(runif(length(lowerBounds),
  lowerBounds,upperBounds))))
population <- cbind(population, t(apply(population,1,zdt2)))
ranking <- fastNonDominatedSorting(population[, (varNo+1):(varNo+objDim)])
rnkIndex <- integer(popSize)
i <- 1
while (i <= length(ranking)) {
  rnkIndex[ranking[[i]]] <- i
  i <- i + 1
}
population <- cbind(population,rnkIndex)
objRange <- apply(population[, (varNo+1):(varNo+objDim)], 2, max) -
  apply(population[, (varNo+1):(varNo+objDim)], 2, min)
cd <- crowdingDist4frnt(population,ranking,objRange)
cd
```

fastNonDominatedSorting

Fast Non-dominated Sorting

Description

A fast approach to sort non-dominated solutions into different nondomination levels.

Usage

```
fastNonDominatedSorting(inputData)
```

Arguments

inputData Matrix of solutions with objective function values

Value

Return a list of indices for all fronts.

Author(s)

Ching-Shih (Vince) Tsou <cstsou@mail.ntcb.edu.tw>

References

Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002), " A fast and elitist multiobjective genetic algorithm: NSGA-II", *IEEE Transactions on Evolutionary Computation*, **6(2)**, 182-197.

Examples

```
set.seed(1234)
# randomly generate a population of fifty chromosomes, each with two objectives
y <- matrix(runif(100, -5, 5), nrow=50, ncol=2)
rankIdxList <- fastNonDominatedSorting(y)
rankIdxList
```

nsga2R

R Based Non-dominated Sorting Genetic Algorithm II

Description

A fast and elitist multiobjective genetic algorithm based on R.

Usage

```
nsga2R(fn, varNo, objDim, lowerBounds = rep(-Inf, varNo), upperBounds = rep(Inf, varNo),
  popSize = 100, tourSize = 2, generations = 20, cprob = 0.7, XoverDistIdx = 5,
  mprob = 0.2, MuDistIdx = 10)
```

Arguments

fn	Objective functions to be minimized
varNo	Number of decision variables
objDim	Number of objective functions
lowerBounds	Lower bounds of each decision variable
upperBounds	Upper bounds of each decision variable
popSize	Size of population
tourSize	Size of tournament
generations	Number of generations
cprob	Crossover probability
XoverDistIdx	Crossover distribution index, it can be any nonnegative real number
mprob	Mutation probability
MuDistIdx	Mutation distribution index, it can be any nonnegative real number

Value

The returned value is a 'nsga2R' object with the following fields in addition to above NSGA-II settings:

parameters	Solutions of decision variables found
objectives	Non-dominated objective function values
paretoFrontRank	Nondomination ranks (or levels) that each non-dominated solution belongs to
crowdingDistance	Crowding distance of each non-dominated solution

Author(s)

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References

Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002), " A fast and elitist multiobjective genetic algorithm: NSGA-II", *IEEE Transactions on Evolutionary Computation*, **6(2)**, 182-197.

Examples

```
# find the non-dominated solutions of zdt3 test problem
results <- nsga2R(fn=zdt3, varNo=30, objDim=2, lowerBounds=rep(0,30), upperBounds=rep(1,30),
  popSize=50, tourSize=2, generations=50, cprob=0.9, XoverDistIdx=20, mprob=0.1, MuDistIdx=3)

plot(results$objectives)
```

tournamentSelection *Tournament Selection*

Description

Tournaments are played among several solutions. The best one is chosen according to their non-domination levels and crowding distances. And it is placed in the mating pool.

Usage

```
tournamentSelection(pop, pool_size, tour_size)
```

Arguments

pop	Population matrix with nondomination rank and crowding distance
pool_size	Size of mating pool, usually same as the population size
tour_size	Size of tournament, the selection pressure can be adjusted by varying the tournament size

Value

Return the mating pool with decision variables, objective functions, nondomination level, and crowding distance

Author(s)

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References

Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002), " A fast and elitist multiobjective genetic algorithm: NSGA-II", *IEEE Transactions on Evolutionary Computation*, **6(2)**, 182-197.

Examples

```
library(mco)
tourSize <- popSize <- 10
lowerBounds <- rep(0,30)
upperBounds <- rep(1,30)
varNo <- length(lowerBounds)
objDim <- 2
set.seed(1234)
population <- t(sapply(1:popSize, function(u) array(runif(length(lowerBounds),
  lowerBounds,upperBounds))))
population <- cbind(population, t(apply(population,1,zdt3)))
ranking <- fastNonDominatedSorting(population[, (varNo+1):(varNo+objDim)])
rnkIndex <- integer(popSize)
i <- 1
while (i <= length(ranking)) {
  rnkIndex[ranking[[i]]] <- i
  i <- i + 1
}
population <- cbind(population,rnkIndex);
objRange <- apply(population[, (varNo+1):(varNo+objDim)], 2, max) -
  apply(population[, (varNo+1):(varNo+objDim)], 2, min);
cd <- crowdingDist4frnt(population,ranking,objRange)
population <- cbind(population,apply(cd,1,sum))
matingPool <- tournamentSelection(population,popSize,tourSize)
matingPool
```

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