

Package ‘rrcov3way’

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Title Robust Methods for Multiway Data Analysis, Applicable also for Compositional Data

Description Provides methods for multiway data analysis by means of Parafac and Tucker 3 models. Robust versions (Engelen and Hubert (2011) <[doi:10.1016/j.aca.2011.04.043](https://doi.org/10.1016/j.aca.2011.04.043)>) and versions for compositional data are also provided (Gallo (2015) <[doi:10.1080/03610926.2013.798664](https://doi.org/10.1080/03610926.2013.798664)>, Di Palma et al. (2018) <[doi:10.1080/02664763.2017.1381669](https://doi.org/10.1080/02664763.2017.1381669)>). Several optimization methods alternative to ALS are available (Simonacci and Gallo (2019) <[doi:10.1016/j.chemolab.2019.103822](https://doi.org/10.1016/j.chemolab.2019.103822)>, Simonacci and Gallo (2020) <[doi:10.1007/s00500-019-04320-9](https://doi.org/10.1007/s00500-019-04320-9)>).

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LazyLoad no

LazyData no

License GPL (>= 3)

URL <https://github.com/valentint/rrcov3way>

BugReports <https://github.com/valentint/rrcov3way/issues>

Repository CRAN

NeedsCompilation no

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Contents

amino	2
Arno	4
congruence	5
cp_als	6
cp_atld	9
cp_gen	11
cp_int2	13
do3Postprocess	15
do3Rotate	17
do3Scale	18
dorrit	19
elind	21
girls	22
Kiers2001	24
Kojima	25
krp	27
mtrace	28
Parafac	29
permute	32
plot.tucker3	33
satisfaction	34
toArray	36
Tucker3	37
ulabor	39
unfold	41
va3way	42
waterquality	44
Index	46

amino

Amino acids fluorescence data.

Description

A data set containing five simple laboratory-made samples where each sample contains different amounts of tyrosine, tryptophan and phenylalanine dissolved in phosphate buffered water. The samples were measured by fluorescence (excitation 240-300 nm, emission 250-450 nm, 1 nm intervals) on a PE LS50B spectrofluorometer.

Usage

data(amino)

Format

A three-way array with dimension 5x201x61. The first dimension refers to the 5 samples. The second dimension refers to the emission measurements (250-450nm, 1nm intervals). The third dimension refers to the excitation (240-300 nm, 1nm intervals).

Source

<https://ucphchemometrics.com/datasets/>.

References

Bro, R, PARAFAC: Tutorial and applications, Chemometrics and Intelligent Laboratory Systems, 1997, 38, 149-171 Bro, R, Multi-way Analysis in the Food Industry. Models, Algorithms, and Applications. 1998. Ph.D. Thesis, University of Amsterdam (NL) & Royal Veterinary and Agricultural University (DK). Kiers, H.A.L. (1998) A three-step algorithm for Candecomp/Parafac analysis of large data sets with multicollinearity, Journal of Chemometrics, 12, 155-171.

Examples

```
## Not run:

data(amino)
## Plotting Emission spectra
oldpar <- par(mfrow=c(2,1))
matplot(t(amino[,1]), type="l",
        xlab="Wavelength/nm", ylab="Intensity",
        main="Fluorescence emission spectra")
matplot(t(amino[,5]), type="l",
        xlab="Wavelength/nm", ylab="Intensity",
        main="Fluorescence emission spectra")
par(oldpar)

## Plotting excitation spectra
oldpar <- par(mfrow=c(2,1))
matplot(t(amino[,1,]), type="l",
        xlab="Wavelength/nm", ylab="Intensity",
        main="Fluorescence excitation spectra")
matplot(t(amino[,30,]), type="l",
        xlab="Wavelength/nm", ylab="Intensity",
        main="Fluorescence excitation spectra")
par(oldpar)

## End(Not run)
```

Arno

Chemical composition of water in the main stream of Arno river

Description

Chemical composition of water in the main stream of Arno river.

Usage

```
data("Arno")
```

Format

A three-way array with dimension 23x11x4. The first dimension refers to 23 distances from the spring. The second dimension refers to the 11 chemical compositions. The third dimension refers to the time of collection - four occasions.

Details

The Arno data example was used in Gallo and Buccianti (2013) to illustrate a particular version of the Tucker model, known as the weighted principal component analysis. The Tucker3 results are usually given in the form of tables or plots and in this work for the representation of the Tucker3 results of logratio data, is proposed to use one-mode plots, clr-joint biplots (Gallo, 2015), and trajectory plots.

Source

Nisi B., Vaselli O., Buccianti A., Minissale A., Delgado-Huertas A., Tassi F., Montegrossi G. (2008). Geochemical and isotopic investigation of the dissolved load in the running waters from the Arno valley: evaluation of the natural and anthropogenic input. In *Memorie Descrittive della Carta Geologica d'Italia*, Nisi (eds.), 79: 1-91.

Nisi B., Buccianti A., Vaselli O., Perini G., Tassi F., Minissale A., Montegrossi G. (2008) Hydro-geochemistry and strontium isotopes in the Arno river basin (Tuscany, Italy): Constraints on natural controls by statistical modeling. *Journal of Hydrology* 360: 166-183.

References

Gallo M. and Buccianti A. (2013). Weighted principal component analysis for compositional data: application example for the water chemistry of the Arno river (Tuscany, central Italy), *Environmetrics*, 24(4):269-277.

Gallo M. (2015). Tucker3 model for compositional data. *Communications in Statistics-Theory and Methods*, 44(21):4441-4453.

Examples

```

data(Arno)
dim(Arno)           # [1] 23 11  4
dim(Arno[, ,1])    # [1] 23 11
rownames(Arno[, ,1]) # the 23 distances from the spring
colnames(Arno[, ,1]) # the 11 chemical compositions
dim(Arno[,1,])     # [1] 23  4
colnames(Arno[,1,]) # the four occasions

res <- Tucker3(Arno, robust=FALSE, coda.transform="ilr")
res

## Distance-distance plot
plot(res, which="dd", main="Distance-distance plot")

## Paired component plot, mode A
plot(res, which="comp", main="Paired component plot (mode A)")

## Paired component plot, mode B
plot(res, which="comp", mode="B", main="Paired component plot (mode B)")

## Joint biplot
plot(res, which="jbplot", main="Joint biplot")

## Trajectory
plot(res, which="tjplot", main="Trajectory biplot")

```

congruence

Coefficient of factor congruence (ϕ)

Description

The function `congruence(x, y)` computes the Tucker's congruence (ϕ) coefficients among two sets of factors.

Usage

```
congruence(x, y = NULL)
```

Arguments

`x` A vector or matrix of factor loadings.
`y` A vector or matrix of factor loadings (may be NULL).

Details

Find the Tucker's coefficient of congruence between two sets of factor loadings. Factor congruences are the cosines of pairs of vectors defined by the loadings matrix and based at the origin. Thus, for loadings that differ only by a scalar (e.g. the size of the eigen value), the factor congruences will be 1.

For factor loading vectors of X and Y the measure of factor congruence, phi, is

$$\phi = \frac{\sum XY}{\sqrt{\sum(X^2) \sum(Y^2)}}.$$

If y=NULL and x is a numeric matrix, the congruence coefficients between the columns of the matrix x are returned. The result is a symmetric matrix with ones on the diagonal. If two matrices are provided, they must have the same size and the result is a square matrix containing the congruence coefficients between all pairs of columns of the two matrices.

Value

A matrix of factor congruences.

Author(s)

Valentin Todorov, <valentin.todorov@chello.at>

References

L.R Tucker (1951). A method for synthesis of factor analysis studies. Personnel Research Section Report No. 984. Department of the Army, Washington, DC.

Examples

```
require(rrcov)

data(delivery, package="robustbase")
X <- getLoadings(PcaClassic(delivery))
Y <- getLoadings(PcaHubert(delivery, k=3))
round(congruence(X, Y), 3)
```

cp_als

Alternating Least Squares (ALS) for Candecomp/Parafac (CP)

Description

Alternating Least Squares (ALS) algorithm with optional constraints for the minimization of the Candecomp/Parafac (CP) loss function.

Usage

```

cp_als(
  X,
  n,
  m,
  p,
  ncomp,
  const = "none",
  start = "random",
  conv = 1e-06,
  maxit = 10000,
  trace = FALSE
)

```

Arguments

X	A three-way array or a matrix. If X is a matrix (matricised threeway array), n, m and p must be given and are the number of A-, B- and C-mode entities respectively
n	Number of A-mode entities
m	Number of B-mode entities
p	Number of C-mode entities
ncomp	Number of components to extract
const	Optional constraints for each mode. Can be a three element character vector or a single character, one of "none" for no constraints (default), "orth" for orthogonality constraints, "nonneg" for nonnegativity constraints or "zerocor" for zero correlation between the extracted factors. For example, const="orth" means orthogonality constraints for all modes, while const=c("orth", "none", "none") sets the orthogonality constraint only for mode A.
start	Initial values for the A, B and C components. Can be "svd" for starting point of the algorithm from SVD's, "random" for random starting point (orthonormalized component matrices or nonnegative matrices in case of nonnegativity constraint), or a list containing user specified components.
conv	Convergence criterion, default is conv=1e-6.
maxit	Maximum number of iterations, default is maxit=10000.
trace	Logical, provide trace output.

Value

The result of the decomposition as a list with the following elements:

- fit Value of the loss function
- fp Fit value expressed as a percentage
- ss Sum of squares
- A Component matrix for the A-mode

- B Component matrix for the B-mode
- C Component matrix for the C-mode
- iter Number of iterations
- tripcos Minimal triple cosine between two components across the three component matrices, used to inspect degeneracy
- mintripcos Minimal triple cosine during the iterative algorithm observed at every 10 iterations, used to inspect degeneracy
- ftiter Matrix containing in each row the function value and the minimal triple cosine at every 10 iterations
- const Optional constraints (same as the input parameter const)

Note

The argument `const` should be a three element character vector. Set `const[j]="none"` for unconstrained update in j-th mode weight matrix (the default), `const[j]="orth"` for orthogonal update in j-th mode weight matrix, `const[j]="nonneg"` for non-negative constraint on j-th mode or `const[j]="zerocor"` for zero correlation between the extracted factors. The default is unconstrained update for all modes.

The loss function to be minimized is $\sum_k ||X(k) - AD(k)B'||^2$, where $D(k)$ is a diagonal matrix holding the k-th row of C.

Author(s)

Valentin Todorov, <valentin.todorov@chello.at>

References

- Harshman, R.A. (1970). Foundations of Parafac procedure: models and conditions for an "explanatory" multi-mode factor analysis. *UCLA Working Papers in Phonetics*, 16: 1–84.
- Harshman, R. A., & Lundy, M. E. (1994). PARAFAC: Parallel factor analysis. *Computational Statistics and Data Analysis*, 18, 39–72.
- Lawson CL, Hanson RJ (1974). *Solving Least Squares Problems*. Prentice Hall, Englewood Cliffs, NJ.

Examples

```
## Not run:
## Example with the OECD data
data(elind)
dim(elind)

res <- cp_als(elind, ncomp=3)
res$fp
res$fp
res$iter

res <- cp_als(elind, ncomp=3, const="nonneg")
```

```

    res$A
## End(Not run)

```

cp_atld	<i>Alternating Trilinear Decomposition (ATLD) for Candecomp/Parafac (CP)</i>
---------	--

Description

Alternating Trilinear Decomposition algorithm for estimating the Candecomp/Parafac (CP) model. It is based on an alternating least squares principle and replaces the iterative procedure used in the traditional PARAFAC algorithm by an improved procedure. This improved procedure contains Moore-Penrose pseudoinverse computations based on singular value decomposition (SVD) which should be theoretically more robust to similarities in spectra and time profiles

Usage

```

cp_atld(
  X,
  n,
  m,
  p,
  ncomp,
  conv = 1e-06,
  start = "random",
  maxit = 5000,
  trace = FALSE
)

```

Arguments

X	A three-way array or a matrix. If X is a matrix (matricised threeway array), n, m and p must be given and are the number of A-, B- and C-mode entities respectively
n	Number of A-mode entities
m	Number of B-mode entities
p	Number of C-mode entities
ncomp	Number of components to extract
conv	Convergence criterion, default is conv=1e-6.
start	Initial values for the A, B and C components. Can be "svd" for starting point of the algorithm from SVD's, "random" for random starting point (orthonormalized component matrices or nonnegative matrices in case of nonnegativity constraint), or a list containing user specified components.
maxit	Maximum number of iterations, default is maxit=10000.
trace	Logical, provide trace output.

Value

The result of the decomposition as a list with the following elements:

- fit Value of the loss function
- fp Fit value expressed as a percentage
- ss Sum of squares
- A Component matrix for the A-mode
- B Component matrix for the B-mode
- C Component matrix for the C-mode
- iter Number of iterations
- tripcos Minimal triple cosine between two components across the three component matrices, used to inspect degeneracy
- mintripcos Minimal triple cosine during the iterative algorithm observed at every 10 iterations, used to inspect degeneracy
- ftiter Matrix containing in each row the function value and the minimal triple cosine at every 10 iterations

Author(s)

Valentin Todorov, <valentin.todorov@chello.at>; Violetta Simonacci, <violetta.simonacci@unina.it>

References

H.-L. Wu, M. Shibukawa, K. Oguma, An alternating trilinear decomposition algorithm with application to calibration of HPLC-DAD for simultaneous determination of overlapped chlorinated aromatic hydrocarbons, *Journal of Chemometrics* **12** (1998) 1–26.

Examples

```
## Not run:
## Example with the OECD data
data(elind)
dim(elind)

res <- cp_atld(elind, ncomp=3)
res$fp
res$fp
res$iter

## End(Not run)
```

 cp_gen

 Generate PARAFAC data sets, optionally with outliers

Description

Generates nsim data sets according to the given parameters. If $\text{eps} > 0$, the specified fraction of random outliers of the identified by the parameter type type are added to the data sets.

Usage

```
cp_gen(
  I = 20,
  J = 20,
  K = 20,
  nsim = 200,
  nf = 3,
  noise = 0.05,
  noise1 = 0,
  Acol = TRUE,
  Bcol = TRUE,
  Ccol = TRUE,
  congA = 0.5,
  congB = 0.5,
  congC = 0.5,
  eps = 0,
  type = c("none", "bl", "gl", "og"),
  c1 = 10,
  c2 = 0.1,
  silent = FALSE
)
```

Arguments

I	number of observations
J	number of variables
K	number of occasions
nsim	number of data sets to generate
nf	number of PARAFAC components
noise	level of homoscedastic (HO) noise
noise1	level of heteroscedastic (HE) noise
Acol	whether to apply collinearity with factor congA to mode A
Bcol	whether to apply collinearity with factor congB to mode B
Ccol	whether to apply collinearity with factor congC to mode C
congA	collinearity factor for mode A

congB	collinearity factor for mode B
congC	collinearity factor for mode C
eps	fraction of outliers (percent contamination)
type	type of outliers: one of "none" for no outliers (possible only of eps==0), "b1" for bad leverage points, "g1" for good leverage points and "og" for orthogonal outliers
c1	parameter for outlier generation (c1=10 for type="b1" or type="g1" and c1=1 for type="og")
c2	parameter for outlier generation (c2=0.1 for type="b1" or type="og" and c2=0 for type="g1")
silent	whether to issue warnings

Value

A list consisting of the following lists:

- As list of `nsim` matrices for the mode A
- Bs list of `nsim` matrices for the mode B
- Cs list of `nsim` matrices for the mode C
- Xs list of `nsim` PARAFAC data sets, each with dimension $I \times J \times K$
- Os list of `nsim` vectors containing the added outliers (if any)
- param list of parameters used for generation of the data sets

References

Todorov, V. and Simonacci, V. and Gallo, M. and Trendafilov, N. (2023). A novel estimation procedure for robust CANDECOMP/PARAFAC model fitting. *Econometrics and Statistics*. In press.

Tomasi, G. and Bro, R., (2006). A comparison of algorithms for fitting the PARAFAC model. *Computational Statistics & Data Analysis* **50** (7), 1700–1734.

Faber, N.M. and Bro, R. and Hopke, P.K. (2003). Recent developments in CANDECOMP/PARAFAC algorithms: A critical review. *Chemometrics and Intelligent Laboratory Systems* **65**, 119–137.

Examples

```
## Generate one PARAFAC data set (nsim=1) with R=2 components (nf=2) and dimensions
## 50x10x10. Apply 0.15 homoscedastic noise and 0.10 heteroscedastic noise, apply
## collinearity with congruence factor 0.5 to all modes. Add 20% bad leverage points.

library(rrcov3way)
xdat <- cp_gen(I=50, J=100, K=10, nsim=1, nf=2,
              noise=0.15, noise1=0.10, Acol=TRUE, Bcol=TRUE, Ccol=TRUE,
              congA=0.5, congB=0.5, congC=0.5,
              eps=0.2, type="b1")
names(xdat)
```

cp_int2

*ATLD-ALS algorithm for Candecomp/Parafac (CP)***Description**

Integrated algorithm combining ATLD and ALS for the minimization of the Candecomp/Parafac (CP) loss function.

Usage

```
cp_int2(
  X,
  n,
  m,
  p,
  ncomp,
  initconv = 0.01,
  conv = 1e-06,
  const = "none",
  start = "random",
  maxit = 5000,
  trace = FALSE
)
```

Arguments

X	A three-way array or a matrix. If X is a matrix (matricised threeway array), n, m and p must be given and are the number of A-, B- and C-mode entities respectively
n	Number of A-mode entities
m	Number of B-mode entities
p	Number of C-mode entities
ncomp	Number of components to extract
initconv	Convergence criterion for the initialization phase (ATLD), default is conv=1e-2.
conv	Convergence criterion, default is conv=1e-6.
const	Optional constraints for each mode. Can be a three element character vector or a single character, one of "none" for no constraints (default), "orth" for orthogonality constraints or "zerocor" for zero correlation between the extracted factors. For example, const="orth" means orthogonality constraints for all modes, while const=c("orth", "none", "none") sets the orthogonality constraint only for mode A.
start	Initial values for the A, B and C components. Can be "svd" for starting point of the algorithm from SVD's, "random" for random starting point (orthonormalized component matrices or nonnegative matrices in case of nonnegativity constraint), or a list containing user specified components.

maxit	Maximum number of iterations, default is maxit=10000.
trace	Logical, provide trace output.

Value

The result of the decomposition as a list with the following elements:

- fit Value of the loss function
- fp Fit value expressed as a percentage
- ss Sum of squares
- A Component matrix for the A-mode
- B Component matrix for the B-mode
- C Component matrix for the C-mode
- iter Number of iterations
- tripcos Minimal triple cosine between two components across the three component matrices, used to inspect degeneracy
- mintripcos Minimal triple cosine during the iterative algorithm observed at every 10 iterations, used to inspect degeneracy
- ftiter Matrix containing in each row the function value and the minimal triple cosine at every 10 iterations
- const Optional constraints (same as the input parameter const)

Note

The argument const should be a three element character vector. Set const[j]="none" for unconstrained update in j-th mode weight matrix (the default), const[j]="orth" for orthogonal update in j-th mode weight matrix or const[j]="zerocor" for zero correlation between the extracted factors. The default is unconstrained update for all modes.

The loss function to be minimized is $\sum(k) \|X(k) - AD(k)B'\|^2$, where $D(k)$ is a diagonal matrix holding the k-th row of C.

Author(s)

Valentin Todorov, <valentin.todorov@chello.at>; Violetta Simonacci, <violetta.simonacci@unina.it>

References

H.-L. Wu, M. Shibukawa, K. Oguma, An alternating trilinear decomposition algorithm with application to calibration of HPLC-DAD for simultaneous determination of overlapped chlorinated aromatic hydrocarbons, *Journal of Chemometrics* **12** (1998) 1–26.

Simonacci, V. and Gallo, M. (2020). An ATLD–ALS method for the trilinear decomposition of large third-order tensors, *Soft Computing* **24** 13535–13546.

Todorov, V. and Simonacci, V. and Gallo, M. and Trendafilov, N. (2023). A novel estimation procedure for robust CANDECOMP/PARAFAC model fitting. *Econometrics and Statistics*. In press.

Examples

```
## Not run:
## Example with the OECD data
data(elind)
dim(elind)

res <- cp_int2(elind, ncomp=3)
res$fp
res$fp
res$iter

res <- cp_int2(elind, ncomp=3, const="orth")
res$A

## End(Not run)
```

do3Postprocess	<i>Postprocessing: renormalization, reflection and reordering; access to some of the components of the model.</i>
----------------	---

Description

The estimated model will be renormalized, reflected (change of sign) or the components will be reordered. Functions that provide access to some components of the model: coordinates, weights.

Usage

```
## S3 method for class 'tucker3'
do3Postprocess(x, reflectA, reflectB, reflectC, reorderA, reorderB, reorderC, ...)
## S3 method for class 'parafac'
do3Postprocess(x, reflectA, reflectB, reflectC, reorder, ...)
## S3 method for class 'parafac'
coordinates(x, mode = c("A", "B", "C"), type = c("normalized", "unit", "principal"), ...)
## S3 method for class 'tucker3'
coordinates(x, mode = c("A", "B", "C"), type = c("normalized", "unit", "principal"), ...)
## S3 method for class 'parafac'
weights(object, ...)
## S3 method for class 'tucker3'
weights(object, mode = c("A", "B", "C"), ...)
## S3 method for class 'parafac'
reflect(x, mode = c("A", "B", "C"), rsign = 1, ...)
## S3 method for class 'tucker3'
reflect(x, mode = c("A", "B", "C"), rsign = 1, ...)
```

Arguments

x	Tucker3 or Parafac solution
object	Tucker3 or Parafac solution (alternative of x for the generic function weights())

reflectA	How to handle the signs of the components of mode A - can be a single number or a vector with length of the number of components of A
reflectB	How to handle the signs of the components of mode B - can be a single number or a vector with length of the number of components of B
reflectC	How to handle the signs of the components of mode C - can be a single number or a vector with length of the number of components of C
reorder	How to reorder the components of a Parafac solution - a vector with length of the number of components
reorderA	How to reorder the components of mode A - a vector with length of the number of components of A giving the new order
reorderB	How to reorder the components of mode B - a vector with length of the number of components of B giving the new order
reorderC	How to reorder the components of mode C - a vector with length of the number of components of C giving the new order
mode	For which mode to provide the coordinates or weights. Default is mode A
type	Which type of coordinates to provide. Default is "normalized"
rsign	How to change the sign of the components of the given mode. Can be a single number or a vector with length of the number of components of the corresponding mode.
...	Potential further arguments passed to lower level functions.

Value

The output value of `do3Postproces()` is the postprocessed solution, Parafac or Tucker3. The output of `weights()` and `coordinates()` are the respective values.

Author(s)

Valentin Todorov <valentin.todorov@chello.at> and Maria Anna Di Palma <madipalma@unior.it> and Michele Gallo <mgallo@unior.it>

References

Kroonenberg (2008). Applied multiway data analysis. Wiley series in probability and statistics. Hoboken NJ, Wiley.

Examples

```
data(elind)
x1 <- do3Scale(elind, center=TRUE, scale=TRUE)
(cp <- Parafac(x1, ncomp=3, const=c("orth", "none", "none")))

cp$B
cp1 <- do3Postprocess(cp, reflectB=-1)      # change the sign of all components of B
cp1$B
weights(cp1)
coordinates(cp1)
```

```

coordinates(cp1, type="principal")

## Same as above - the centering and scaling is done inside the Parafac procedure
(cp1 <- Parafac(elind, ncomp=3, const=c("orth", "none", "none"),
  center=TRUE, scale=TRUE))

## Robust estimation with robust scaling with median and mad
(cp1 <- Parafac(elind, ncomp=3, const=c("orth", "none", "none"),
  center=median, scale=mad, robust=TRUE))

## Robust estimation with robust scaling with median and Qn (Rousseeuw and Croux, 1993)
require(robustbase)
(cp1 <- Parafac(elind, ncomp=3, const=c("orth", "none", "none"),
  center=median, scale=Qn, robust=TRUE))

```

do3Rotate

*Varimax Rotation for Tucker3 models***Description**

Computes *varimax* rotation of the core and component matrix of a Tucker3 model to simple structure.

Usage

```

do3Rotate(x, ...)

## S3 method for class 'tucker3'
do3Rotate(x, weights = c(0, 0, 0), rotate = c("A", "B", "C"), ...)

```

Arguments

x	A Tucker 3 object
...	Potential further arguments passed to called functions.
weights	A numeric vector with length 3: relative weights (greater or equal 0) for the simplicity of the component matrices A, B and C respectively.
rotate	Within which mode to rotate the Tucker3 solution: rotate="A" means to rotate the component matrix A of mode A; rotate=c("A", "B") means to rotate the component matrices A and B of modes A and B respectively. Default is to rotate all modes, i.e. rotate=c("A", "B", "C").

Value

A list including the following components:

Author(s)

Valentin Todorov, <valentin.todorov@chello.at>

Examples

```
## Rotation of a Tucker3 solution
data(elind)
(t3 <- Tucker3(elind, 3, 2, 2))
xout <- do3Rotate(t3, c(3, 3, 3), rotate=c("A", "B", "C"))
xout$vvvalue
```

do3Scale

*Centering and scaling***Description**

Centering and/or normalization of a three way array or a matricized array across one mode (modes indicated by "A", "B" or "C").

Usage

```
## S3 method for class 'tucker3'
do3Scale(x, renorm.mode = c("A", "B", "C"), ...)
## S3 method for class 'parafac'
do3Scale(x, renorm.mode = c("A", "B", "C"), ...)
## Default S3 method:
do3Scale(x, center = FALSE, scale = FALSE,
         center.mode = c("A", "B", "C", "AB", "AC", "BC", "ABC"),
         scale.mode = c("B", "A", "C"),
         only.data=TRUE, ...)
```

Arguments

x	Three dimensional array of order (I x J x K) or a matrix (or data.frame coerced to a matrix) of order (I x JK) containing the matricized array (frontal slices)
center	Whether and how to center the data. Can be NULL, logical TRUE or FALSE, function or a numeric vector with length corresponding to the number of columns in the corresponding mode. If center=TRUE, mean() is used; default is center=FALSE.
scale	Whether and how to scale the data. Can be NULL, logical TRUE or FALSE, function or a numeric vector with length corresponding to the number of columns in the corresponding mode. If scale=TRUE, sd() is used; default is scale=FALSE.
center.mode	Across which mode to center. Default is center.mode="A"
scale.mode	Within which mode to scale. Default is scale.mode="B"
renorm.mode	Within which mode to renormalize a Parafac or Tucker3 solution. See in Details how this is performed for the different models. Default is renorm.mode="A"
only.data	Whether to return only the centered/scaled data or also the center and the scale themselves. Default is only.data=TRUE
...	potential further arguments passed to lower level functions.

Value

A named list, consisting of the centered and/or scaled data, a center vector, a scale vector and the mode in which the data were centered/scaled.

Author(s)

Valentin Todorov <valentin.todorov@chello.at> and Maria Anna Di Palma <madipalma@unior.it> and Michele Gallo <mgallo@unior.it>

References

Kiers, H.A.L. (2000). Towards a standardized notation and terminology in multiway analysis. *Journal of Chemometrics*, 14:105-122.

Kroonenberg, P.M. (1983). Three-mode principal component analysis: Theory and applications (Vol. 2), DSWO press.

Examples

```
data(elind)
(x1 <- do3Scale(elind, center=TRUE, scale=TRUE))
(x2 <- do3Scale(elind, center=TRUE, scale=TRUE, center.mode="B"))
(x3 <- do3Scale(elind, center=TRUE, scale=TRUE, center.mode="C", scale.mode="C"))
```

dorrit

Dorrit fluorescence data.

Description

A data set with 27 synthetic samples containing different concentrations of four analytes (hydroquinone, tryptophan, phenylalanine and dopa) measured in a Perkin-Elmer LS50 B fluorescence spectrometer.

Usage

```
data(dorrit)
```

Format

A three-way array with dimension 27 x 116 x 18. The first dimension refers to the 27 samples. The second dimension refers to the emission measurements (251-481nm, 2nm intervals). The third dimension refers to the excitation (230-315nm, 5nm intervals).

Details

Each fluorescence landscape corresponding to each sample in the original data set consists of 233 emission wavelengths (250-482 nm) and 24 excitation wavelengths (200-315 nm taken each 5 nm). The fluorescence data is three-way. Ideally, the data is trilinear, the components of the modes corresponding to concentrations (27), emission spectra (233) and excitation spectra (24). Hence a three-way PARAFAC model should be capable of uniquely and meaningfully describing the variation in the data set.

The data set is modified as described in Engelen and Hubert (2011): the emission wavelengths are taken at 2 nm, noisy parts situated at the excitation wavelengths from 200 to 230 nm and at emission wavelengths below 250 nm are excluded. The severe Rayleigh scattering areas present in all samples are replaced by interpolated values. Thus we end up with a (27 x 116 x 18) data array.

Source

<https://ucphchemometrics.com/datasets/>.

References

- Bro, R, Sidiropoulos, ND and Smilde, AK (2002). Maximum likelihood fitting using ordinary least squares algorithms. *Journal of Chemometrics*, **16**(8–10), 387–400.
- Riu, J and Bro, R (2003) Jack-knife estimation of standard errors and outlier detection in PARAFAC models. *Chemometrics and Intelligent Laboratory Systems*, **65**(1), 35–49
- Engelen, S and Hubert, M (2011) Detecting outlying samples in a parallel factor analysis model, *Analytica Chimica Acta* **705** 155–165.
- Baunsgaard, D (1999) Factors Affecting 3-way Modelling (PARAFAC) of Fluorescence Landscapes, Royal Veterinary and Agricultural University, Department of Dairy and Food Science, Frederiksberg, Denmark.

Examples

```
## Not run:

data(dorrit)
## Plotting Emission spectra
oldpar <- par(mfrow=c(2,1))
matplot(t(dorrit[,1]), type="l",
        xlab="Wavelength/nm", ylab="Intensity",
        main="Fluorescence emission spectra")
matplot(t(dorrit[,5]), type="l",
        xlab="Wavelength/nm", ylab="Intensity",
        main="Fluorescence emission spectra")
par(oldpar)

## Plotting excitation spectra
oldpar <- par(mfrow=c(2,1))
matplot(t(dorrit[,1,]), type="l",
        xlab="Wavelength/nm", ylab="Intensity",
        main="Fluorescence excitation spectra")
matplot(t(dorrit[,30,]), type="l",
```

```

        xlab="Wavelength/nm", ylab="Intensity",
        main="Fluorescence excitation spectra")
par(oldpar)

persp(as.numeric(dimnames(dorrit)[[2]]),
      as.numeric(dimnames(dorrit)[[3]]), dorrit[4,,],
      xlab="Emission", ylab="Excitation", zlab="Intensity",
      theta = 30, phi = 30, expand = 0.5, col = "lightblue",
      ticktype="detailed")

pp <- Parafac(dorrit, ncomp=4, robust=TRUE)
plot(pp)

## End(Not run)

```

elind

OECD Electronics Industries Data

Description

OECD publishes comparative statistics of the export size of various sectors of the electronics industry:

1. information science,
2. telecommunication products,
3. radio and television equipment,
4. components and parts,
5. electromedical equipment, and
6. scientific equipment.

The data consist of specialisation indices of electronics industries of 23 European countries for the years 1973–1979. The specialization index is defined as the proportion of the monetary value of an electronic industry compared to the total export value of manufactured goods of a country compared to the similar proportion for the world as a whole (see D’Ambra, 1985, p. 249 and Kroonenberg, 2008, p.282).

Usage

```
data(elind)
```

Format

A three-way array with dimension 23x6x7. The first dimension refers to 23 countries. The second dimension refers to the six indices of electronics industries. The third dimension refers to the years in the period 1978–1985.

Source

The data set is available from Pieter Kroonenberg's web site at: ["three-mode.leidenuniv.nl/data/electronicindustriesinfo.htm"](http://three-mode.leidenuniv.nl/data/electronicindustriesinfo.htm)

References

D'Ambra, L. (1985). Alcune estensione dell'analisi in componenti principali per lo studio dei sistemi evolutivi. Uno studio sul commercio internazionale dell'elettronica. In: Ricerche Economiche. 2. del Dipartimento di Scienze Economiche Ca'Foscari, Venezia.

Kroonenberg PM (2008). Applied multiway data analysis. Wiley series in probability and statistics. John Wiley and Sons, Hoboken, NJ, p.282.

Examples

```
data(elind)

res <- Parafac(elind, robust=FALSE, coda.transform="none")

## Distance-distance plot
plot(res, which="dd", main="Distance-distance plot")

## Paired component plot, mode A
plot(res, which="comp", main="Paired component plot (mode A)")

## Paired component plot, mode B
plot(res, which="comp", mode="B", main="Paired component plot (mode B)")

## Per-component plot
plot(res, which="percomp", comp=1, main="Per component plot")

## all components plot
plot(res, which="allcomp", main="All components plot", legend.position="topright")
```

girls

Sempe girls' growth curves data

Description

Thirty girls selected from a French auxiological study (1953-1975) to get insight into the physical growth patterns of children from ages four to fifteen, Sempe (1987). They were measured yearly between the ages 4 and 15 on the following eight variables:

1. weight = Weight
2. length = Length
3. crump = Crown-rump length
4. head = Head circumference
5. chest = Chest circumference

6. arm = Arm
7. calf = Calf
8. pelvis = Pelvis

The data set is three way data array of size 30 (girls) x 8 (variables) x 12 (years).

Usage

```
data("girls")
```

Format

The format is a three way array with the following dimensions: The first dimension refers to 30 girls. The second dimension refers to the eight variables measured on the girls. The third dimension refers to the years – 4 to 15.

Details

The data are generally preprocessed as standard multiway profile data. For details see Kroonenberg (2008), Chapters 6 and 15.

Source

The data sets are available from Pieter Kroonenberg's web site at: ["three-mode.leidenuniv.nl/data/girlsgrowthcurvesinfo.htm"](http://three-mode.leidenuniv.nl/data/girlsgrowthcurvesinfo.htm)

References

Sempe, M. (1987). Multivariate and longitudinal data on growing children: Presentation of the French auxiological survey. In J.Janssen et al. Data analysis. The Ins and Outs of solving real problems (pp. 3-6). New York: Plenum Press.

Kroonenberg (2008). Applied multiway data analysis. Wiley series in probability and statistics. Hoboken NJ, Wiley.

Examples

```
data(girls)
str(girls)
## Center the data in mode A and find the "average girl"
center.girls <- do3Scale(girls, center=TRUE, only.data=FALSE)
X <- center.girls$x
center <- center.girls$center
average.girl <- as.data.frame(matrix(center, ncol=8, byrow=TRUE))
dimnames(average.girl) <- list(dimnames(X)[[3]], dimnames(X)[[2]])

## Divide these variables by 10 to reduce their range
average.girl$weight <- average.girl$weight/10
average.girl$length <- average.girl$length/10
average.girl$crump <- average.girl$crump/10

average.girl
p <- ncol(average.girl)
```

```

plot(rownames(average.girl), average.girl[,1], ylim=c(min(average.girl),
  max(average.girl)), type="n", xlab="Age", ylab="")
for(i in 1: p)
{
  lines(rownames(average.girl), average.girl[,i], lty=i, col=i)
  points(rownames(average.girl), average.girl[,i], pch=i, col=i)
}
legend <- colnames(average.girl)
legend[1] <- paste0(legend[1], "*")
legend[2] <- paste0(legend[3], "*")
legend[3] <- paste0(legend[4], "*")
legend("topleft", legend=legend, col=1:p, lty=1:p, pch=1:p)

```

Kiers2001

Fictitious data set of Kiers and Mechelen (2001).

Description

A fictitious data presented by Kiers and Mechelen (2001) to illustrate Tucker3 model: A set of six persons with scores on five response variables for four different situations. The response variables indicate to what extent each individual displays an emotional, sensitive, caring, thorough, or accurate behavior. The data set is represented as a $6 \times 5 \times 4$ array. The data are chosen such that they correspond to a Tucker3 model with $P=2$, $Q=2$, $R=2$.

Usage

```
data(Kiers2001)
```

Format

A three-way array with dimension $6 \times 5 \times 4$. The first dimension refers to the 6 persons. The second dimension refers to the five response variables. The third dimension refers to four different situations.

Source

Kiers HAL, Mechelen IV (2001) Three-way component analysis: Principles and illustrative application. *Psychological Methods* 6(1):84–110

References

Todorov, V., Simonacci, V., Gallo, M., and Di Palma, M. (2025). Robust tools for three-way component analysis of compositional data: The R package *rrcov3way*. *Behaviormetrika*. In press.

Examples

```
data(Kiers2001)

t3 <- Tucker3(Kiers2001, P=2, Q=2, R=2)
t3
t3$A
t3$B
t3$C
t3$G
plot(t3)
plot(t3, which="jbplot", xlim=c(0, 2))
```

Kojima

Parental behaviour in Japan

Description

The data are drawn from a study (Kojima, 1975) of the perception of parental behaviour by parents and their children. Two data sets, boys and girls are available as Kojima.boys and Kojima.girls.

- Boys data were analysed in Kroonenberg (2008)
- Girls data were analysed in Kroonenberg, Harshman, & Murakami (2009).

Usage

```
data(Kojima)
```

Format

Both data sets are three dimensional arrays:

- boys: 150 x 18 x 4
- girls: 153 x 18 x 4

The rows (1st mode) are 150 Japanese sons/153 Japanese daughters. The columns (2nd mode) are 18 scales (Acceptance, Child centerness, Possesiveness, etc.). The slices (3rd mode) are the 4 judgements (See Details for explanation).

Details

The boys data are ratings expressing the judgments of parents with respect to their own behaviour toward their sons, and the judgments of their sons with respect to their parents. Thus, there are four conditions:

- Father-Own behaviour (F-F),
- Mother-Own behaviour (M-M),

- Son-Father (B-F),
- Son-Mother (B-M).

The judgments involved 150 middle-class Japanese eighth-grade boys on the 18 subscales of the inventory. Thus, the data set consists of a 150 (Sons) x 18 (scales) x 4 (judgment combinations) data array.

Similarly, the girls data are ratings expressing the judgments of parents with respect to their own behaviour toward their daughters, and the judgments of their daughters with respect to their parents. Thus, there are four conditions:

- Father-Own behaviour (F-F),
- Mother-Own behaviour (M-M),
- Daughter-Father (G-F),
- Daughter-Mother (G-M).

The judgments involved 153 middle-class Japanese eighth-grade girls on the 18 subscales of the inventory. Thus, the data set consists of a 153 (Daughters) x 18 (scales) x 4 (judgment combinations) data array.

Preprocessing Given that the data are three-way profile data they are treated in the standard manner: centering per occasion-variable combination and by normalising the data after centring per lateral slice i.e. per scale over all sons/daughters x judges combinations. For details see Kroonenberg (2008), Chapter 13.

Source

The data sets are available from the Pieter Kroonenberg's web site at <https://three-mode.leidenuniv.nl/>.

References

Kojima, H. (1975). Inter-battery factor analysis of parents' and children's reports of parental behavior. *Japanese Psychological Bulletin*, 17, 33-48 (in Japanese).

Kroonenberg, P. M. (2008). *Applied multiway data analysis*. Wiley series in probability and statistics. Wiley, Hoboken NJ.

Kroonenberg, P. M., Harshman, R. A., & Murakami, T. (2009). Analysing three-way profile data using the Parafac and Tucker3 models illustrated with views on parenting. *Applied Multivariate Research*, 13:5-41. PDF available at: <http://www.phaenex.uwindsor.ca/ojs/leddy/index.php/AMR/article/viewFile/2833/2271>

Examples

```
data(Kojima)
dim(Kojima.boys)
dim(Kojima.girls)
```

krp

The Khatri-Rao product of two matrices

Description

The function `krp(A,B)` returns the Khatri-Rao product of two matrices A and B, of dimensions I x K and J x K respectively. The result is an IJ x K matrix formed by the matching column-wise Kronecker products, i.e. the k-th column of the Khatri-Rao product is defined as `kron(A[, k], B[, k])`.

Usage

```
krp(A, B)
```

Arguments

A	Matrix of order I x K.
B	Matrix of order J x K.

Value

The IJ x K matrix of columnwise Kronecker products.

Author(s)

Valentin Todorov, <valentin.todorov@chello.at>

References

Khatri, C. G., and Rao, C. Radhakrishna (1968). Solutions to Some Functional Equations and Their Applications to Characterization of Probability Distributions. *Sankhya: Indian J. Statistics, Series A* 30, 167-180.

Smilde, A., Bro R. and Gelardi, P. (2004). *Multi-way Analysis: Applications in Chemical Sciences*, Chichester:Wiley

Examples

```
a <- matrix(1:12, 3, 4)
b <- diag(1:4)
krp(a, b)
krp(b, a)
```

mtrace

The trace of a square numeric matrix

Description

Computes the trace of a square numeric matrix. If A is not numeric and square matrix, the function terminates with an error message.

Usage

```
mtrace(A)
```

Arguments

A A square numeric matrix.

Value

the sum of the values on the diagonal of the matrix A, i.e. `sum(diag(A))`.

Author(s)

Valentin Todorov, <valentin.todorov@chello.at>

Examples

```
(a <- matrix(c(5,2,3, 4,-3,7, 4,1,2), ncol=3))
(b <- matrix(c(1,0,1, 0,1,2, 1,0,3), ncol=3))

mtrace(a)
mtrace(b)

## tr(A+B)=tr(A)+tr(B)
all.equal(mtrace(a) + mtrace(b), mtrace(a+b))

## tr(A)=tr(A')
all.equal(mtrace(a), mtrace(t(a)))

## tr(alphaA)=alphatr(A)
alpha <- 0.5
all.equal(mtrace(alpha*a), alpha*mtrace(a))

## tr(AB)=tr(BA)
all.equal(mtrace(a %*% b), mtrace(b %*% a))

## tr(A)=tr(BAB-1)
all.equal(mtrace(a), mtrace(b %*% a %*% solve(b)))
```

Parafac	<i>Robust Parafac estimator for compositional data</i>
---------	--

Description

Compute a robust Parafac model for compositional data

Usage

```
Parafac(X, ncomp = 2, center = FALSE,
        center.mode = c("A", "B", "C", "AB", "AC", "BC", "ABC"),
        scale=FALSE, scale.mode=c("B", "A", "C"),
        const="none", conv = 1e-06, start="svd", maxit=10000,
        optim=c("als", "atld", "int2"),
        robust = FALSE, coda.transform=c("none", "ilr", "clr"),
        ncomp.rpca = 0, alpha = 0.75, robiter = 100, crit=0.975, trace = FALSE)
```

Arguments

X	3-way array of data
ncomp	Number of components
center	Whether to center the data
center.mode	If centering the data, on which mode to do this
scale	Whether to scale the data
scale.mode	If scaling the data, on which mode to do this
const	Optional constraints for each mode. Can be a three element character vector or a single character, one of "none" for no constraints (default), "orth" for orthogonality constraints, "nonneg" for nonnegativity constraints or "zerocor" for zero correlation between the extracted factors. For example, const="orth" means orthogonality constraints for all modes, while const=c("orth", "none", "none") sets the orthogonality constraint only for mode A.
conv	Convergence criterion, defaults to 1e-6
start	Initial values for the A, B and C components. Can be "svd" for starting point of the algorithm from SVD's, "random" for random starting point (orthonormalized component matrices or nonnegative matrices in case of nonnegativity constraint), or a list containing user specified components.
maxit	Maximum number of iterations, default is maxit=10000.
optim	How to optimize the CP loss function, default is to use ALS, i.e. optim="als". Other options are ATLD (optim="atld") and INT2 (optim="INT2"). Please note that ATLD cannot be used with the robust option.
robust	Whether to apply a robust estimation
coda.transform	If the data are a composition, use an <i>ilr</i> or <i>clr</i> transformation. Default is non-compositional data, i.e. coda.transform="none"

<code>ncomp.rpca</code>	Number of components for robust PCA
<code>alpha</code>	Measures the fraction of outliers the algorithm should resist. Allowed values are between 0.5 and 1 and the default is 0.75
<code>robiter</code>	Maximal number of iterations for robust estimation
<code>crit</code>	Cut-off for identifying outliers, default <code>crit=0.975</code>
<code>trace</code>	Logical, provide trace output

Details

The function can compute four versions of the Parafac model:

1. Classical Parafac,
2. Parafac for compositional data,
3. Robust Parafac and
4. Robust Parafac for compositional data.

This is controlled though the paramters `robust=TRUE` and `coda.transform=c("none", "ilr")`.

Value

An object of class "parafac" which is basically a list with components:

<code>fit</code>	Fit value
<code>fp</code>	Fit percentage
<code>ss</code>	Sum of squares
<code>A</code>	Orthogonal loading matrix for the A-mode
<code>B</code>	Orthogonal loading matrix for the A-mode
<code>Bclr</code>	Orthogonal loading matrix for the B-mode, clr transformed. Available only if <code>coda.transform="ilr"</code> , otherwise NULL
<code>C</code>	Orthogonal loading matrix for the C-mode
<code>Xhat</code>	(Robustly) reconstructed array
<code>const</code>	Optional constraints (same as the input parameter)
<code>iter</code>	Number of iterations
<code>rd</code>	Residual distances
<code>sd</code>	Score distances
<code>flag</code>	The observations whose residual distance <code>rd</code> is larger than <code>cutoff.rd</code> or score distance <code>sd</code> is larger than <code>cutoff.sd</code> , can be considered outliers and receive a flag equal to zero. The regular observations receive a flag 1
<code>robust</code>	The paramater <code>robust</code> , whether robust method is used or not
<code>coda.transform</code>	Which coda transformation is used, can be <code>coda.transform=c("none", "ilr", "clr")</code> .

Author(s)

Valentin Todorov <valentin.todorov@chello.at> and Maria Anna Di Palma <madipalma@unior.it>
and Michele Gallo <mgallo@unior.it>

References

- Harshman, R.A. (1970). Foundations of Parafac procedure: models and conditions for an "explanatory" multi-mode factor analysis. *UCLA Working Papers in Phonetics*, 16: 1–84.
- Engelen, S., Frosch, S. and Jorgensen, B.M. (2009). A fully robust PARAFAC method analyzing fluorescence data. *Journal of Chemometrics*, 23(3): 124–131.
- Kroonenberg, P.M. (1983). Three-mode principal component analysis: Theory and applications (Vol. 2), DSWO press.
- Rousseeuw, P.J. and Driessen, K.V. (1999). A fast algorithm for the minimum covariance determinant estimator. *Technometrics*, 41(3): 212–223.
- Egozcue J.J., Pawlowsky-Glahn V., Mateu-Figueras G. and Barcel'o-Vidal, C. (2003). Isometric logratio transformations for compositional data analysis. *Mathematical Geology*, 35(3): 279-300

Examples

```
#####
##
## Example with the UNIDO Manufacturing value added data

data(va3way)
dim(va3way)

## Treat quickly and dirty the zeros in the data set (if any)
va3way[va3way==0] <- 0.001

##
res <- Parafac(va3way)
res
print(res$fit)
print(res$A)

## Distance-distance plot
plot(res, which="dd", main="Distance-distance plot")

data(ulabor)
res <- Parafac(ulabor, robust=TRUE, coda.transform="ilr")
res

## Plot Orthonormalized A-mode component plot
plot(res, which="comp", mode="A", main="Component plot, A-mode")

## Plot Orthonormalized B-mode component plot
plot(res, which="comp", mode="B", main="Component plot, B-mode")

## Plot Orthonormalized C-mode component plot
plot(res, which="comp", mode="C", main="Component plot, C-mode")
```

permute	<i>Permutation of a matricized array</i>
---------	--

Description

Permutes the matricized ($n \times m \times p$) array X to the matricized array Y of order ($m \times p \times n$).

Usage

```
permute(X, n, m, p)
```

Arguments

X	Matrix (or data.frame coerced to a matrix) containing the matricized array
n	Number of A-mode entities of the array X
m	Number of B-mode entities of the array X
p	Number of C-mode entities of the array X

Value

Y	Matrix containing the permuted matricized array
-----	---

References

H.A.L. Kiers (2000). Towards a standardized notation and terminology in multiway analysis. *Journal of Chemometrics* 14:105–122.

Examples

```
X <- array(1:24, c(4,3,2))
dim(X)

## matricize the array
Xa <- unfold(X) # matricized X with the A-mode entities in its rows
dim(Xa)
Xa

## matricized X with the B-mode entities in its rows
Xb <- permute(Xa, 4, 3, 2)
dim(Xb)
Xb

## matricized X with the C-mode entities in its rows
Xc <- permute(Xb, 3, 2, 4)
dim(Xc)
Xc
```

plot.tucker3 *Plot a parafac or a tucker3 object*

Description

Different plots for the results of Parafac or Tucker3 analysis, stored in a Parafac or a tucker3 object, see Details.

Usage

```
## S3 method for class 'tucker3'
plot(x, which = c("dd", "comp", "allcomp", "jbplot",
  "tjplot", "all"), ask = (which == "all" && dev.interactive(TRUE)), id.n, ...)
## S3 method for class 'parafac'
plot(x, which = c("dd", "comp", "percomp", "allcomp",
  "all"), ask = (which == "all" && dev.interactive(TRUE)), id.n, ...)
```

Arguments

x	A tucker3 object
which	Which plot to select (see Details). Default is dd, distance-distance plot.
ask	Generates all plots in interactive mode
id.n	Number of items to highlight
...	Other parameters to be passed to the lower level functions.

Details

Different plots for a tucker3 or parafac object will be produced. Use the parameter which to select which plot to produce:

dd Distance-distance plot
 comp Paired components plot
 percomp Per-component plot - only for Parafac
 allcomp All components plot
 jbplot Joint biplot - only for Tucker3
 tjplot Trajectory plot - only for Tucker3

Author(s)

Valentin Todorov <valentin.todorov@chello.at> and Maria Anna Di Palma <madipalma@unior.it>
 and Michele Gallo <mgallo@unior.it>

References

Kiers, H.A. (2000).Some procedures for displaying results from three-way methods. *Journal of Chemometrics*. 14(3): 151-170.

Kroonenberg, P.M. (1983).Three-mode principal component analysis: Theory and applications (Vol. 2), DSWO press.

Examples

```
#####
##
## Example with the UNIDO Manufacturing value added data

data(va3way)
dim(va3way)

## Treat quickly and dirty the zeros in the data set (if any)
va3way[va3way==0] <- 0.001

##
res <- Tucker3(va3way)
res
print(res$fit)
print(res$A)

## Print the core matrix
print(res$GA)

## Distance-distance plot
plot(res, which="dd", main="Distance-distance plot")

## Paired component plot, mode A
plot(res, which="comp", main="Paired component plot (mode A)")

## Paired component plot, mode B
plot(res, which="comp", mode="B", main="Paired component plot (mode B)")

## Joint biplot
plot(res, which="jbplot", main="Joint biplot")

## Trajectory
plot(res, which="tjplot", choices=c(1:4), arrows=FALSE, main="Trajectory biplot")
```

Description

The primary assessment tool for analyzing student satisfaction is an annual questionnaire organized into five categories: degree program, course characteristics, teaching, equipment, and overall satisfaction. Each questionnaire comprises 18 standardized questions rated on a ten-point Likert scale (1 = "Strongly Disagree" to 10 = "Strongly Agree"). The original microdata were aggregated by 10 faculties and six academic years. Thus, we have a threeway array with dimensions $10 \times 18 \times 6$.

Usage

```
data(satisfaction)
```

Format

A three-way array with dimension $10 \times 18 \times 6$. The first dimension refers to the 10 faculties. The second dimension refers to 18 standardized questions rated on a ten-point Likert scale (1 = "Strongly Disagree" to 10 = "Strongly Agree"). The third dimension refers to six consecutive academic years (2012–2017).

Source

Italian universities are mandated by Law No. 370/99 to evaluate teaching quality through student opinion surveys. The National Agency for the Evaluation of Universities and Research (ANVUR), established in 2006, supervises the periodic assessment of academic quality. Following Presidential Decree 76/2010, ANVUR standardized methodologies for evaluating institutions and degree programs, with a strong focus on student involvement. The University of Florence provided microdata, which were later aggregated into data for 10 faculties, 18 questions and 6 academic years.

Simonacci V, Gallo M (2017) Statistical tools for student evaluation of academic educational quality. *Quality & Quantity* 51(2):565–579

References

Gallo M, Simonacci V, Todorov V (2021) A compositional three-way approach for student satisfaction analysis. In: Filzmoser P, Hron K, Martín-Fernández JA, Palarea-Albaladejo J (eds) *Advances in Compositional Data Analysis*, Springer, Cham, pp 143–162

Todorov, V., Simonacci, V., Gallo, M., and Di Palma, M. (2025). Robust tools for three-way component analysis of compositional data: The R package *rrcov3way*. *Behaviormetrika*. In press.

Examples

```
data(satisfaction)

t3 <- Tucker3(satisfaction, P=2, Q=2, R=1, coda.transform="clr")
t3
t3$A
t3$B
t3$C
t3$G
plot(t3)
plot(t3, which="jbplot", xlim=c(-1, 1))
```

`toArray`*Matrix to array conversion*

Description

Restore an array from its matricization with all the frontal slices of the array next to each other (mode="A")

Usage

```
toArray(x, n, m, r, mode = c("A", "B", "C"))
```

Arguments

<code>x</code>	Matrix (or data.frame coerced to a matrix) containing the elements of the frontal slices of an array
<code>n</code>	number of A-mode elements
<code>m</code>	number of B-mode elements
<code>r</code>	number of C-mode elements
<code>mode</code>	in which mode is the matricized array

Value

Three way array

Author(s)

Valentin Todorov <valentin.todorov@chello.at> and Maria Anna Di Palma <madipalma@unior.it> and Michele Gallo <mgallo@unior.it>

References

H.A.L. Kiers (2000). Towards a standardized notation and terminology in multiway analysis. *Journal of Chemometrics*, 14: 105–122.

Examples

```
data(elind)
di <- dim(elind)
toArray(unfold(elind), di[1], di[2], di[3])
```

Tucker3 *Robust Tucker3 estimator for compositional data*

Description

Compute a robust Tucker3 model for compositional data

Usage

```
Tucker3(X, P = 2, Q = 2, R = 2,
  center = FALSE, center.mode = c("A", "B", "C", "AB", "AC", "BC", "ABC"),
  scale = FALSE, scale.mode = c("B", "A", "C"),
  conv = 1e-06, start="svd",
  robust = FALSE, coda.transform=c("none", "ilr", "clr"),
  ncomp.rpca = 0, alpha = 0.75, robiter=100, crit=0.975, trace = FALSE)
```

Arguments

X	3-way array of data
P	Number of A-mode components
Q	Number of B-mode components
R	Number of C-mode components
center	Whether to center the data
center.mode	If scaling the data, on which mode to do this
scale	Whether to scale the data
scale.mode	If centering the data, on which mode to do this
conv	Convergence criterion, defaults to 1e-6
start	Initial values for the A, B and C components. Can be "svd" for starting point of the algorithm from SVD's, "random" for random starting point (orthonormalized component matrices), or a list containing user specified components.
robust	Whether to apply a robust estimation
coda.transform	If the data are a composition, use an <i>ilr</i> or <i>clr</i> transformation. Default is non-compositional data, i.e. coda.transform="none"
ncomp.rpca	Number of components for robust PCA
alpha	Measures the fraction of outliers the algorithm should resist. Allowed values are between 0.5 and 1 and the default is 0.75
robiter	Maximal number of iterations for robust estimation
crit	Cut-off for identifying outliers, default crit=0.975
trace	Logical, provide trace output

Details

The function can compute four versions of the Tucker3 model:

1. Classical Tucker3,
2. Tucker3 for compositional data,
3. Robust Tucker3 and
4. Robust Tucker3 for compositional data.

This is controlled through the parameters `robust=TRUE` and `coda.transform="ilr"`.

Value

An object of class "tucker3" which is basically a list with components:

<code>fit</code>	Fit value
<code>fp</code>	Fit percentage
<code>A</code>	Orthogonal loading matrix for the A-mode
<code>B</code>	Orthogonal loading matrix for the B-mode
<code>Bclr</code>	Orthogonal loading matrix for the B-mode, clr transformed. Available only if <code>coda.transform="ilr"</code> , otherwise NULL
<code>C</code>	Orthogonal loading matrix for the C-mode
<code>GA</code>	Core matrix, which describes the relation between A, B and C, unfolded in A-form. The largest squared elements of the core matrix indicate the most important factors in the model of X.
<code>iter</code>	Number of iterations
<code>rd</code>	Residual distances
<code>sd</code>	Score distances
<code>flag</code>	The observations whose residual distance RD is larger than <code>cutoff.RD</code> can be considered as outliers and receive a flag equal to zero. The regular observations receive a flag 1
<code>robust</code>	The parameter <code>robust</code> , whether robust method is used or not
<code>coda.transform</code>	The input parameter <code>coda.transform</code> , what transformation for compositional data was used
<code>La</code>	Diagonal matrix containing the <i>intrinsic eigenvalues</i> for A-mode
<code>Lb</code>	Diagonal matrix containing the <i>intrinsic eigenvalues</i> for B-mode
<code>Lc</code>	Diagonal matrix containing the <i>intrinsic eigenvalues</i> for C-mode

Author(s)

Valentin Todorov <valentin.todorov@chello.at> and Maria Anna Di Palma <madipalma@unior.it> and Michele Gallo <mgallo@unior.it>

References

Tucker, L.R. (1966). Some mathematical notes on three-mode factor analysis. *Psychometrika*, 31: 279–311.

Egozcue J.J., Pawlowsky-Glahn, V., Mateu-Figueras G. and Barcel' o-Vidal, C. (2003). Isometric logratio transformations for compositional data analysis. *Mathematical Geology*, 35(3): 279–300.

Examples

```
#####
##
## Example with the UNIDO Manufacturing value added data

data(va3way)
dim(va3way)

## Treat quickly and dirty the zeros in the data set (if any)
va3way[va3way==0] <- 0.001

##
res <- Tucker3(va3way)
res
print(res$fit)
print(res$A)

## Print the core matrix
print(res$GA)

## Distance-distance plot
plot(res, which="dd", main="Distance-distance plot")

## Paired component plot, mode A
plot(res, which="comp", main="Paired component plot (mode A)")

## Paired component plot, mode B
plot(res, which="comp", mode="B", main="Paired component plot (mode B)")

## Joint biplot
plot(res, which="jbplot", main="Joint biplot")

## Trajectory
plot(res, which="tjplot", choices=c(1:4), arrows=FALSE, main="Trajectory biplot")
```

Description

The dataset contains the undeclared labor in thousands work units. The data originate from Italy and are recorded at a regional level over a certain time horizon for five macroeconomic activities defined according to NACE Rev. 1.1 classification.

Usage

```
data("ulabor")
```

Format

A three-way array with dimension 22x5x5. The first dimension refers to 22 regions in Italy. The second dimension refers to the 5 economic activities. The third dimension refers to the years in the period 2001-2009.

Source

ISTAT (2011). Note metodologiche, la misura dell'occupazione non regolare nelle stime di contabilità nazionale [online]. Roma.

References

ISTAT (2011). Note metodologiche, la misura dell'occupazione non regolare nelle stime di contabilità nazionale [online]. Roma.

Di Palma M.A., Filzmoser P., Gallo M. and Hron, K. (2016). A robust CP model for compositional data, submitted.

Examples

```
data(ulabor)
dim(ulabor)
str(ulabor)

## Plot robust and non-robust DD-plots of the ilr-transformed data
usr <- par(mfrow=c(1,2))
res1 <- Parafac(ulabor, robust=TRUE, coda.transform="ilr")
res2 <- Parafac(ulabor, coda.transform="ilr")
plot(res1)
plot(res2)
par(usr)

## Not run:

## Plot Orthonormalized A-mode component plot
res <- Parafac(ulabor, robust=TRUE, coda.transform="ilr")
plot(res, which="comp", mode="A", main="Component plot, A-mode")

## Plot Orthonormalized B-mode component plot
plot(res, which="comp", mode="B", main="Component plot, B-mode")
```

```
## Plot Orthonormalized B-mode component plot
plot(res, which="comp", mode="C", main="Component plot, C-mode")

## Per component plot
## adapted for the example and only for robust, ilr transformed model
##
##
res <- Parafac(ulabor, robust=TRUE, coda.transform="ilr")

plot(res, which="percomp")          # component 1
plot(res, which="percomp", comp=2) # component 2

## End(Not run)
```

unfold

Matrix unfolding

Description

Conducts matricizations of a three-way array into matrices according to the selected mode.

Usage

```
unfold(x, mode=c("A", "B", "C"))
```

Arguments

x	Array to be unfolded
mode	the selected mode for unfolding

Value

A matrix representing the input array, according to the selected mode:

- Mode=A: B-mode entities are nested within C-mode entities (all the frontal slices of the array next to each other) item Mode=B: C-mode entities nested within A-mode entities (all the horizontal slices of the array next to each other) item Mode C: A-mode entities nested within B-mode entities (all the lateral slices of the array next to each other)

Author(s)

Valentin Todorov <valentin.todorov@chello.at>

References

H.A.L. Kiers (2000). Towards a standardized notation and terminology in multiway analysis. *Journal of Chemometrics* 14:105–122.

Examples

```
(X <- array(1:24, c(4,3,2)))
dim(X)

## matricize the array

## matricized X with the A-mode entities in its rows
## all the frontal slices of the array next to each other
##
(Xa <- unfold(X))
dim(Xa)

## matricized X with the B-mode entities in its rows
## all the horizontal slices of the array next to each other
##
(Xb <- unfold(X, mode="B"))
dim(Xb)

## matricized X with the C-mode entities in its rows
## all the lateral slices of the array next to each other
##
(Xc <- unfold(X, mode="C"))
dim(Xc)
```

va3way

Manufacturing value added by technology intensity for several years

Description

A three-way array containing manufacturing value added by technology intensity for 55 countries in the period 2000–2010. UNIDO maintains a unique database containing key industrial statistics indicators for more than 160 countries in the world in the period 1963-2011: INDSTAT 2, available at <https://stat.unido.org>. The data are organized according to the International Standard Industrial Classification of all economic activities (ISIC) Revision 3 at 2-digit level. The present data set was created by aggregating the 23 2-digit divisions into five groups according to technology intensity, using the UNIDO derived classification (Upadhyaya, 2011). Then 55 countries were selected which have relatively complete data in the period 2000–2010.

Usage

```
data(va3way)
```

Format

A three-way array with dimension 55x5x11. The first dimension refers to 55 countries. The second dimension refers to the five categories of technology intensity described above. The third dimension refers to the years in the period 2000–2010.

Details

Note that the values in the second mode (sectors) sum up to a constant - the total manufacturing value added of a country in a given year and thus the data set has a compositional character.

Source

<https://stat.unido.org>

References

Upahdyaya S (2011). Derived classifications for industrial performance indicators. In *Int. Statistical Inst.: Proc. 58th World Statistical Congress, 2011, Dublin (Session STS022)*.

Upahdyaya S, Todorov V (2008). UNIDO Data Quality. UNIDO Staff Working Paper, Vienna.

Examples

```
data(va3way)
ct <- 2
x <- va3way[ct,]/1000000
plot(colnames(x), x[1,], ylim=c(min(x), max(x)), type="n", ylab="Manufacturing Value
  Added in million USD", xlab="Years")
for(i in 1:nrow(x))
  lines(colnames(x), x[i,], col=i)
legend("topleft", legend=rownames(x), col=1:nrow(x), lwd=1)
title(paste("Country: ", rownames(va3way[,1])[ct]))

## Treat quickly and dirty the zeros in the data set (if any)
## in order to be able to perform ilr transformation:

va3way[va3way==0] <- 0.001

res <- Tucker3(va3way)

##
## Not yet a print function
##
print(res$fit)
print(res$A)

## Print the core matrix
print(res$GA)

## Distance-distance plot
plot(res, which="dd", main="Distance-distance plot")

## Paired component plot, mode A
plot(res, which="comp", main="Paired component plot (mode A)")

## Paired component plot, mode B
plot(res, which="comp", mode="B", main="Paired component plot (mode B)")
```

```
## Joint biplot
plot(res, which="jbplot", main="Joint biplot")

## Trajectory
plot(res, which="tjplot", main="Trajectory biplot")
```

waterquality

Water quality data in Wyoming, USA

Description

Water quality data for three years of seasonal compositional groundwater chemistry data for 14 wells at a study site in Wyoming, USA. Routine water quality monitoring typically involves measurement of J parameters and constituents measured at I number of static locations at K sets of seasonal occurrences.

Usage

```
data("waterquality")
```

Format

A three-way array with dimension 14x12x10. The first dimension refers to 14 wells at a study site in Wyoming, USA. The second dimension refers to the ten most reactive and indicative dissolved constituents at the site: B, Ba, Ca, Cl, K, Mg, Na, Si, Sr, and SO₄. In addition, the concentration of water in each sample was calculated. The third dimension refers to the time of collection - ten occasions.

References

Engle, M.A., Gallo, M., Schroeder, K.T., Geboy, N.J., Zupancic, J.W., (2014). Three-way compositional analysis of water quality monitoring data. *Environmental and Ecological Statistics*, 21(3):565-581.

Examples

```
data(waterquality)
dim(waterquality)           # [1] 14 12 10
dim(waterquality[,1])      # [1] 14 12
rownames(waterquality[,1]) # the 14 wells
colnames(waterquality[,1]) # the 12 chemical compositions
dim(waterquality[1,])      # [1] 14 10
colnames(waterquality[1,]) # the ten occasions

(res <- Tucker3(waterquality, robust=FALSE, coda.transform="ilr"))

## Distance-distance plot
```

```
plot(res, which="dd", main="Distance-distance plot")
## Paired component plot, mode A
plot(res, which="comp", main="Paired component plot (mode A)")

## Paired component plot, mode B
plot(res, which="comp", mode="B", main="Paired component plot (mode B)")

## Joint biplot
plot(res, which="jbplot", main="Joint biplot")

## Trajectory
plot(res, which="tjplot", main="Trajectory biplot")
```

Index

* **Multivariate**

- Parafac, [29](#)
- plot.tucker3, [33](#)
- Tucker3, [37](#)

* **Robust**

- Parafac, [29](#)
- plot.tucker3, [33](#)
- Tucker3, [37](#)

* **algebra**

- do3Postprocess, [15](#)
- do3Scale, [18](#)
- permute, [32](#)
- toArray, [36](#)
- unfold, [41](#)

* **array**

- do3Postprocess, [15](#)
- do3Scale, [18](#)
- permute, [32](#)
- toArray, [36](#)
- unfold, [41](#)

* **datasets**

- amino, [2](#)
- Arno, [4](#)
- dorrit, [19](#)
- elind, [21](#)
- girls, [22](#)
- Kiers2001, [24](#)
- Kojima, [25](#)
- satisfaction, [34](#)
- ulabor, [39](#)
- va3way, [42](#)
- waterquality, [44](#)

* **multivariate**

- do3Postprocess, [15](#)
- do3Scale, [18](#)
- permute, [32](#)
- toArray, [36](#)
- unfold, [41](#)

amino, [2](#)

Arno, [4](#)

congruence, [5](#)
coordinates (do3Postprocess), [15](#)
cp_als, [6](#)
cp_atld, [9](#)
cp_gen, [11](#)
cp_int2, [13](#)

do3Postprocess, [15](#)
do3Rotate, [17](#)
do3Scale, [18](#)
dorrit, [19](#)

elind, [21](#)

girls, [22](#)

is.orthogonal (do3Postprocess), [15](#)
is.orthonormal (do3Postprocess), [15](#)

Kiers2001, [24](#)
Kojima, [25](#)
krp, [27](#)

mtrace, [28](#)

Parafac, [29](#)
permute, [32](#)
plot.parafac (plot.tucker3), [33](#)
plot.tucker3, [33](#)
print.parafac (Parafac), [29](#)
print.tucker3 (Tucker3), [37](#)

reflect (do3Postprocess), [15](#)
reorder (do3Postprocess), [15](#)

satisfaction, [34](#)

tall2wide (do3Postprocess), [15](#)
tallArray (do3Postprocess), [15](#)
toArray, [36](#)

Tucker3, [37](#)

ulabor, [39](#)

unfold, [41](#)

va3way, [42](#)

waterquality, [44](#)

weights (do3Postprocess), [15](#)

wideArray (do3Postprocess), [15](#)