

# Package ‘tehtuner’

May 8, 2026

**Title** Fit and Tune Models to Detect Treatment Effect Heterogeneity

**Version** 0.3.0

**Description** Implements methods to fit Virtual Twins models (Foster et al. (2011) <[doi:10.1002/sim.4322](https://doi.org/10.1002/sim.4322)>) for identifying subgroups with differential effects in the context of clinical trials while controlling the probability of falsely detecting a differential effect when the conditional average treatment effect is uniform across the study population using parameter selection methods proposed in Wolf et al. (2022) <[doi:10.1177/17407745221095855](https://doi.org/10.1177/17407745221095855)>.

**License** GPL (>= 3)

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**Imports** party, glmnet, Rdpack, rpart, stringr, SuperLearner, randomForestSRC, earth, foreach

**RdMacros** Rdpack

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**URL** <https://github.com/jackmwolf/tehtuner>

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---

get\_mnpp

*Get the MNPP for the Step 2 model*

---

### Description

Find the lowest penalty parameter so that the Step 2 model fit for the estimated CATE from Step 1 is constant for all subjects.

### Usage

```
get_mnpp(z, data, step2, Trtr, Y, threshold)
```

**Arguments**

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
step2	a character string specifying the Step 2 model. Supports "lasso", "rtree", "classtree", or "ctree".
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
threshold	for "step2 = 'classtree'" only. The value against which to test if the estimated individual treatment effect from Step 1 is higher (TRUE) or lower (FALSE).

---

get\_mnpp.classtree      *Get the MNPP for a Classification Tree*

---

**Description**

Finds the lowest complexity parameter for a null regression tree fit

**Usage**

```
get_mnpp.classtree(z, data, Trt, Y, threshold)
```

**Arguments**

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
threshold	for "step2 = 'classtree'" only. The value against which to test if the estimated individual treatment effect from Step 1 is higher (TRUE) or lower (FALSE).

**Value**

the MNPP

---

get\_mnpp.ctree      *Get the MNPP for a Conditional Inference Tree*

---

### Description

Finds the lowest test statistic for a null conditional inference tree

### Usage

```
get_mnpp.ctree(z, data, Trt, Y)
```

### Arguments

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.

### Value

the MNPP

---

get\_mnpp.lasso      *Get the MNPP for a Model fit via Lasso*

---

### Description

Finds the lowest penalty parameter for a null lasso model.

### Usage

```
get_mnpp.lasso(z, data, Trt, Y)
```

### Arguments

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.

---

get_mnpp.rtree	<i>Get the MNPP for a Regression Tree</i>
----------------	---

---

**Description**

Finds the lowest complexity parameter for a null regression tree fit

**Usage**

```
get_mnpp.rtree(z, data, Trt, Y)
```

**Arguments**

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.

**Value**

the MNPP

---

get_theta_null	<i>Permute a dataset under the null hypothesis and get the MNPP</i>
----------------	---

---

**Description**

Permute a dataset under the null hypothesis and get the MNPP

**Usage**

```
get_theta_null(data, Trt, Y, zbar, step1, step2, threshold, ...)
```

**Arguments**

data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
zbar	the estimated marginal treatment effect
step1	character strings specifying the Step 1 model. Supports either "lasso", "mars", "randomforest", or "superlearner".

step2	a character string specifying the Step 2 model. Supports "lasso", "rtree", "classtree", or "ctree".
threshold	for "step2 = 'classtree'" only. The value against which to test if the estimated individual treatment effect from Step 1 is higher (TRUE) or lower (FALSE).
...	additional arguments to the Step 1 model call.

**Value**

the MNPP for the permuted data set

---

get_vt1	<i>Get the appropriate Step 1 estimation function associated with a method</i>
---------	--

---

**Description**

Get the appropriate Step 1 estimation function associated with a method

**Usage**

```
get_vt1(step1)
```

**Arguments**

step1	character strings specifying the Step 1 model. Supports either "lasso", "mars", "randomforest", or "superlearner".
-------	--

**Value**

a function that estimates the CATE through Step 1 of Virtual Twins

---

get_vt2	<i>Get the appropriate Step 2 estimation function associated with a method</i>
---------	--

---

**Description**

Get the appropriate Step 2 estimation function associated with a method

**Usage**

```
get_vt2(step2)
```

**Arguments**

step2	a character string specifying the Step 2 model. Supports "lasso", "rtree", "classtree", or "ctree".
-------	---

**Value**

a function that fits a model for the CATE through Step 2 of Virtual Twins

---

permut	<i>Generate a dataset with permuted treatment indicators</i>
--------	--

---

**Description**

Sets the marginal treatment effect to zero and then permute all treatment indicators.

**Usage**

```
permut(data, Trt, Y, zbar)
```

**Arguments**

data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
zbar	the estimated marginal treatment effect

**Value**

a permuted dataset of the same size as data

---

print.tunevt	<i>Print an object of class tunevt</i>
--------------	--

---

**Description**

Prints a Virtual Twins model for the conditional average treatment effect with a tuned Step 2 model.

**Usage**

```
## S3 method for class 'tunevt'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

**Arguments**

x	an object of class tunevt
digits	the number of significant digits to use when printing.
...	further arguments passed to or from other methods.

**Value**

An object of class "tunevt".

An object of class "tunevt" is a list containing at least the following components:

call	the matched call
vtmod	the model estimated by the given step2 procedure fit with the permuted tuning parameter for the estimated CATEs from the step1 model. See <a href="#">vt2_lasso</a> , <a href="#">vt2_rtree</a> , or <a href="#">vt2_ctree</a> for specifics.
mnpp	the MNPP for the estimated CATEs from Step 1.
theta_null	a vector of the MNPPs from each permutation under the null hypothesis.
pvalue	the probability of observing a MNPP as or more extreme as the observed MNPP under the null hypothesis of no effect heterogeneity.
z	if keepz = TRUE, the estimated CATEs from the step1 model.

---

tehtuner_example	<i>Simulated example data</i>
------------------	-------------------------------

---

**Description**

Simulated data from a clinical trial with heterogeneous treatment effects where the CATE was a function of V1 and V9.

**Usage**

```
tehtuner_example
```

**Format**

A data frame with 1000 rows and 12 columns:

**Trt** Binary treatment indicator

**Y** Continuous response

**V1,V2,V3,V4,V5,V6,V7,V8** Continuous covariates

**V9,V10** Binary covariates

---

test\_null\_theta\_ctree *Test if a Value Gives a Null Conditional Inference Tree*

---

### Description

Fits a conditional inference tree with minimal test statistic `theta` and tests if the tree has more than one terminal node.

### Usage

```
test_null_theta_ctree(theta, z, data, Trt, Y)
```

### Arguments

<code>theta</code>	a positive double
<code>z</code>	a numeric vector of estimated CATEs from Step 1
<code>data</code>	a data frame containing a response, binary treatment indicators, and covariates.
<code>Trt</code>	a string specifying the name of the column of data contains the treatment indicators.
<code>Y</code>	a string specifying the name of the column of data contains the response.

### Value

a boolean. True if `theta` is large enough to give a null conditional inference tree. False otherwise.

---

tunevt *Fit a tuned Virtual Twins model*

---

### Description

`tunevt` fits a Virtual Twins model to estimate factors and subgroups associated with differential treatment effects while controlling the Type I error rate of falsely detecting at least one heterogeneous effect when the treatment effect is uniform across the study population.

### Usage

```
tunevt(
  data,
  Y = "Y",
  Trt = "Trt",
  step1 = "randomforest",
  step2 = "rtree",
  alpha0,
  p_reps,
```

```

    threshold = NA,
    keepz = FALSE,
    parallel = FALSE,
    ...
  )

```

### Arguments

<code>data</code>	a data frame containing a response, binary treatment indicators, and covariates.
<code>Y</code>	a string specifying the name of the column of data contains the response.
<code>Trt</code>	a string specifying the name of the column of data contains the treatment indicators.
<code>step1</code>	character strings specifying the Step 1 model. Supports either "lasso", "mars", "randomforest", or "superlearner".
<code>step2</code>	a character string specifying the Step 2 model. Supports "lasso", "rtree", "classtree", or "ctree".
<code>alpha0</code>	the nominal Type I error rate.
<code>p_reps</code>	the number of permutations to run.
<code>threshold</code>	for "step2 = 'classtree'" only. The value against which to test if the estimated individual treatment effect from Step 1 is higher (TRUE) or lower (FALSE).
<code>keepz</code>	logical. Should the estimated CATE from Step 1 be returned?
<code>parallel</code>	Should the loop over replications be parallelized? If FALSE, then no, if TRUE, then yes. Note that running in parallel requires a <i>parallel backend</i> that must be registered before performing the computation. See the <a href="#">foreach</a> documentation for more details.
<code>...</code>	additional arguments to the Step 1 model call.

### Details

Virtual Twins is a two-step approach to detecting differential treatment effects. Subjects' conditional average treatment effects (CATEs) are first estimated in Step 1 using a flexible model. Then, a simple and interpretable model is fit in Step 2 to model either (1) the expected value of these estimated CATEs if step2 is equal to "lasso", "rtree", or "ctree" or (2) the probability that the CATE is greater than a specified threshold if step2 is equal to "classtree".

The Step 2 model is dependent on some tuning parameter. This parameter is selected to control the Type I error rate by permuting the data under the null hypothesis of a constant treatment effect and identifying the minimal null penalty parameter (MNPP), which is the smallest penalty parameter that yields a Step 2 model with no covariate effects. The  $1-\alpha_0$  quantile of the distribution of is then used to fit the Step 2 model on the original data.

### Value

An object of class "tunevt".

An object of class "tunevt" is a list containing at least the following components:

<code>call</code>	the matched call
-------------------	------------------

vtmod	the model estimated by the given step2 procedure fit with the permuted tuning parameter for the estimated CATEs from the step1 model. See <a href="#">vt2_lasso</a> , <a href="#">vt2_rtree</a> , or <a href="#">vt2_ctree</a> for specifics.
mnpp	the MNPP for the estimated CATEs from Step 1.
theta_null	a vector of the MNPPs from each permutation under the null hypothesis.
pvalue	the probability of observing a MNPP as or more extreme as the observed MNPP under the null hypothesis of no effect heterogeneity.
z	if keepz = TRUE, the estimated CATEs from the step1 model.

## References

- Foster JC, Taylor JM, Ruberg SJ (2011). “Subgroup identification from randomized clinical trial data.” *Statistics in Medicine*, **30**(24), 2867–2880. ISSN 02776715, [doi:10.1002/sim.4322](#).
- Wolf JM, Koopmeiners JS, Vock DM (2022). “A permutation procedure to detect heterogeneous treatment effects in randomized clinical trials while controlling the type I error rate.” *Clinical Trials*, **19**(5), 512-521. ISSN 1740-7745, [doi:10.1177/17407745221095855](#), Publisher: SAGE Publications.
- Deng C, Wolf JM, Vock DM, Carroll DM, Hatsukami DK, Leng N, Koopmeiners JS (2023). “Practical guidance on modeling choices for the virtual twins method.” *Journal of Biopharmaceutical Statistics*. [doi:10.1080/10543406.2023.2170404](#).

## Examples

```
data(tehtuner_example)
# Low p_reps for example use only
tunevt(
  tehtuner_example, step1 = "lasso", step2 = "rtree",
  alpha0 = 0.2, p_reps = 5
)
```

---

tune\_theta

*Estimate the penalty parameter for Step 2 of Virtual Twins*

---

## Description

Permutes data under the null hypothesis of a constant treatment effect and calculates the MNPP on each permuted data set. The 1 - alpha quantile of the distribution is taken.

## Usage

```
tune_theta(
  data,
  Trt,
  Y,
  zbar,
```

```

    step1,
    step2,
    threshold,
    alpha0,
    p_reps,
    parallel,
    ...
)

```

### Arguments

data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
zbar	the estimated marginal treatment effect
step1	character strings specifying the Step 1 model. Supports either "lasso", "mars", "randomforest", or "superlearner".
step2	a character string specifying the Step 2 model. Supports "lasso", "rtree", "classtree", or "ctree".
threshold	for "step2 = 'classtree'" only. The value against which to test if the estimated individual treatment effect from Step 1 is higher (TRUE) or lower (FALSE).
alpha0	the nominal Type I error rate.
p_reps	the number of permutations to run.
parallel	Should the loop over replications be parallelized? If FALSE, then no, if TRUE, then yes. Note that running in parallel requires a <i>parallel backend</i> that must be registered before performing the computation. See the <a href="#">foreach</a> documentation for more details.
...	additional arguments to the Step 1 model call.

### Value

the estimated penalty parameter

---

validate_alpha0	<i>Check if alpha0 is a valid input to tunevt</i>
-----------------	---

---

### Description

Check if alpha0 is a valid input to tunevt

### Usage

```
validate_alpha0(data, alpha0)
```

**Arguments**

data a data frame containing a response, binary treatment indicators, and covariates.  
 alpha0 the nominal Type I error rate.

**Value**

TRUE if alpha0 is a valid input. Errors otherwise.

---

validate\_p\_reps *Check if p\_reps is a valid input to tunevt*

---

**Description**

Check if p\_reps is a valid input to tunevt

**Usage**

```
validate_p_reps(data, p_reps)
```

**Arguments**

data a data frame containing a response, binary treatment indicators, and covariates.  
 p\_reps the number of permutations to run.

**Value**

TRUE if p\_reps is a valid input. Errors otherwise.

---

validate\_Trtr *Check if Trtr is a valid input to tunevt*

---

**Description**

Check if Trtr is a valid input to tunevt

**Usage**

```
validate_Trtr(data, Trtr)
```

**Arguments**

data a data frame containing a response, binary treatment indicators, and covariates.  
 Trtr a string specifying the name of the column of data contains the treatment indicators.

**Value**

TRUE if Trtr is a valid input. Errors otherwise.

---

validate_Y	<i>Check if Y is a valid input to tunevt</i>
------------	--

---

**Description**

Check if Y is a valid input to tunevt

**Usage**

```
validate_Y(data, Y)
```

**Arguments**

data	a data frame containing a response, binary treatment indicators, and covariates.
Y	a string specifying the name of the column of data contains the response.

**Value**

TRUE if Y is a valid input. Errors otherwise.

---

vt1_lasso	<i>Estimate the CATE Using the Lasso for Step 1 of Virtual Twins</i>
-----------	--

---

**Description**

Estimate the CATE Using the Lasso for Step 1 of Virtual Twins

**Usage**

```
vt1_lasso(data, Trt, Y, ...)
```

**Arguments**

data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
...	additional arguments to <code>cv.glmnet</code>

**Value**

Estimated CATEs for each subject in data.

**See Also**

Other VT Step 1 functions: [vt1\\_mars\(\)](#), [vt1\\_rf\(\)](#), [vt1\\_super\(\)](#)

---

vt1_mars	<i>Estimate the CATE Using MARS for Step 1 of Virtual Twins</i>
----------	---

---

**Description**

Estimate the CATE Using MARS for Step 1 of Virtual Twins

**Usage**

```
vt1_mars(data, Trt, Y, ...)
```

**Arguments**

data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
...	additional arguments to earth

**Value**

Estimated CATEs for each subject in data.

**See Also**

Other VT Step 1 functions: [vt1\\_lasso\(\)](#), [vt1\\_rf\(\)](#), [vt1\\_super\(\)](#)

---

vt1_rf	<i>Estimate the CATE Using a Random Forest for Step 1 of Virtual Twins</i>
--------	--

---

**Description**

Estimate the CATE Using a Random Forest for Step 1 of Virtual Twins

**Usage**

```
vt1_rf(data, Trt, Y, ...)
```

**Arguments**

data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
...	additional arguments to rfsrc

**Value**

Estimated CATEs for each subject in data.

**See Also**

Other VT Step 1 functions: [vt1\\_lasso\(\)](#), [vt1\\_mars\(\)](#), [vt1\\_super\(\)](#)

---

 vt1\_super

---

*Estimate the CATE Using Super Learner for Step 1 of Virtual Twins*


---

**Description**

Estimate the CATE Using Super Learner for Step 1 of Virtual Twins

**Usage**

```
vt1_super(data, Trt, Y, SL.library, ...)
```

**Arguments**

<code>data</code>	a data frame containing a response, binary treatment indicators, and covariates.
<code>Trt</code>	a string specifying the name of the column of data contains the treatment indicators.
<code>Y</code>	a string specifying the name of the column of data contains the response.
<code>SL.library</code>	Either a character vector of prediction algorithms or a list containing character vector. See SuperLearner for more details.
<code>...</code>	additional arguments to SuperLearner

**Value**

Estimated CATEs for each subject in data.

**See Also**

Other VT Step 1 functions: [vt1\\_lasso\(\)](#), [vt1\\_mars\(\)](#), [vt1\\_rf\(\)](#)

---

vt2_classtree	<i>Estimate the CATE using a classification tree for Step 2</i>
---------------	---

---

**Description**

Estimate the CATE using a classification tree for Step 2

**Usage**

```
vt2_classtree(z, data, Trt, Y, theta, threshold)
```

**Arguments**

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
theta	tree complexity parameter (cp)
threshold	for "step2 = 'classtree'" only. The value against which to test if the estimated individual treatment effect from Step 1 is higher (TRUE) or lower (FALSE).

**Value**

an object of class `rpart`. See [rpart.object](#).

**See Also**

Other VT Step 2 functions: [vt2\\_ctree\(\)](#), [vt2\\_lasso\(\)](#), [vt2\\_rtree\(\)](#)

---

vt2_ctree	<i>Estimate the CATE using a conditional inference tree for Step 2</i>
-----------	--

---

**Description**

Estimate the CATE using a conditional inference tree for Step 2

**Usage**

```
vt2_ctree(z, data, Trt, Y, theta)
```

**Arguments**

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
theta	the value of the test statistic that must be exceeded in order to implement a split (mincriterion)

**Value**

An object of class `BinaryTree-class`. See [BinaryTree-class](#).

**See Also**

Other VT Step 2 functions: [vt2\\_classtree\(\)](#), [vt2\\_lasso\(\)](#), [vt2\\_rtree\(\)](#)

---

 vt2\_lasso

*Estimate the CATE using the Lasso for Step 2*


---

**Description**

Estimate the CATE using the Lasso for Step 2

**Usage**

```
vt2_lasso(z, data, Trt, Y, theta)
```

**Arguments**

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
theta	lasso penalty parameter ( $\lambda$ )

**Value**

a list of length 3 containing the following elements:

mod	an object of class <code>glmnet</code> . See <a href="#">glmnet</a> .
coefficients	coefficients associated with the penalty parameter $\theta$ .
fitted.values	predicted values associated with the penalty parameter $\theta$ .

**See Also**

Other VT Step 2 functions: [vt2\\_classtree\(\)](#), [vt2\\_ctree\(\)](#), [vt2\\_rtree\(\)](#)

---

vt2\_rtree

*Estimate the CATE using a regression tree for Step 2*

---

**Description**

Estimate the CATE using a regression tree for Step 2

**Usage**

```
vt2_rtree(z, data, Trt, Y, theta)
```

**Arguments**

z	a numeric vector of estimated CATEs from Step 1
data	a data frame containing a response, binary treatment indicators, and covariates.
Trt	a string specifying the name of the column of data contains the treatment indicators.
Y	a string specifying the name of the column of data contains the response.
theta	tree complexity parameter (cp)

**Value**

an object of class `rpart`. See [rpart.object](#).

**See Also**

Other VT Step 2 functions: [vt2\\_classtree\(\)](#), [vt2\\_ctree\(\)](#), [vt2\\_lasso\(\)](#)

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