

# Package ‘timeEL’

May 8, 2026

**Title** Time to Event Analysis via Empirical Likelihood Inference

**Version** 0.9.1

**Description** Computation of t-year survival probabilities and t-year risks with right censored survival data. The Kaplan-Meier estimator is used to provide estimates for data without competing risks and the Aalen-Johansen estimator is used when there are competing risks. Confidence intervals and p-values are obtained using either usual Wald-type inference or empirical likelihood inference, as described in Thomas and Grunkemeier (1975) <[doi:10.1080/01621459.1975.10480315](https://doi.org/10.1080/01621459.1975.10480315)> and Blanche (2020) <[doi:10.1007/s10985-018-09458-6](https://doi.org/10.1007/s10985-018-09458-6)>. Functions for both one-sample and two-sample inference are provided. Unlike Wald-type inference, empirical likelihood inference always leads to consistent conclusions, in terms of statistical significance, when comparing two risks (or survival probabilities) via either a ratio or a difference.

**License** GPL (>= 3)

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**RoxygenNote** 7.3.2

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AalenJohansen	<i>Risk estimate using the Aalen-Johansen method</i>
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### Description

Computes the Aalen-Johansen estimator to estimate an (absolute) risk with right-censored competing risks data, together with a confidence interval and (possibly) a p-value (for a one-sample hypothesis test). Computation of confidence intervals and p-values is based on either Empirical Likelihood (EL) inference or Wald-type inference. Both are non-parametric approaches, which are asymptotically equivalent. See Blanche (2020) for details. For the Wald-type approach, the asymptotic normal approximation is used on the cloglog scale. See e.g. equation 4.21 in Beyersmann et al (2011).

### Usage

```
AalenJohansen(
  time,
  cause,
  t,
  risk.H0 = NULL,
  level = 0.95,
  contr = list(tol = 1e-05, k = 3, Trace = FALSE, method = "both")
)
```

### Arguments

time	vector of times (possibly censored)
cause	vector of event types/causes. It should be coded 1 for main events, 2 for competing events and 0 for censored.
t	the time point of interest (e.g., 1 to compute a 1-year risk)

risk.H0	risk under the null hypothesis, if one would like to compute the corresponding p-value. Default is NULL, for which no p-value is computed.
level	confidence level for the confidence intervals. Default is 0.95.
contr	list of control parameters. tol=tolerance for numerical computation, default is 1e-5. method="EL", "Wald" or "both" indicates whether 95% CI and p-value should be computed based on Empirical Likelihood (EL) inference, Wald-type inference or both.

### Value

object of class 'AalenJohansen'

### Author(s)

Paul Blanche

### References

- Blanche, P. (2020). Confidence intervals for the cumulative incidence function via constrained NPMLE. *Lifetime Data Analysis*, 26(1), 45-64.
- Beyersmann, Allignol, & Schumacher (2011). *Competing risks and multistate models with R*. Springer Science & Business Media.

### Examples

```
x <- AalenJohansen(time=melanoma5$time, cause=melanoma5$status, t=4, level=0.95)
x
```

---

BMTplat

*Bone Marrow Transplant Registry*

---

### Description

The data contain observations of 408 patients treated with HLA-identical sibling bone marrow transplantation for myelodysplasia. The dataset is essentially a subset of the 'bmt' data of the 'timereg' package (minor changes were introduced to break the ties).

### Usage

BMTplat

### Format

A data frame with 408 rows and 3 variables:

**time** time to event since transplant (in months)

**status** event status, 1 is dead from treatment related causes, 2 is relapse, 0 is censored.

**group** platelet level: 1 if more than  $100 \times 10^9$  per L, 0 if less

**Source**

'timereg' package

**References**

Li, J., Le-Rademacher, J., & Zhang, M. J. (2014). Weighted comparison of two cumulative incidence functions with R-CIFsmry package. *Computer methods and programs in biomedicine*, 116(3), 205-214.

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BMTtcell

*Bone Marrow Transplant Registry*

---

**Description**

The data contain observations of 408 patients treated with HLA-identical sibling bone marrow transplantation for myelodysplasia. The dataset is essentially a subset of the 'bmt' data of the 'timereg' package (minor changes were introduced to break the ties).

**Usage**

BMTtcell

**Format**

A data frame with 408 rows and 3 variables:

**time** time to event since transplant (in months)

**status** event status, 1 is dead from treatment related causes, 2 is relapse , 0 is censored.

**group** presence of T-cell depletion: 1 if present, 0 otherwise

**Source**

'timereg' package

**References**

Li, J., Le-Rademacher, J., & Zhang, M. J. (2014). Weighted comparison of two cumulative incidence functions with R-CIFsmry package. *Computer methods and programs in biomedicine*, 116(3), 205-214.

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Freireich	<i>Acute Leukemia data from Freireich et al (1963)</i>
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**Description**

In this study there were 21 pairs of subjects, and within each pair one subject received 6-mercaptopurine (6-MP) and one got placebo. The data are right censored. See also Gehan (1965) and Thomas & Grunkemeier (1975) who used the data as an illustrative example (ignoring the pairing).

**Usage**

Freireich

**Format**

A data frame with 42 rows and 3 variables:

**time** time in remission (in weeks)

**status** event status, 1 is relapse, 0 is censored

**group** treatment group: 0 (placebo) or 1 (6-MP)

**Source**

Data listed in Section 5 in Thomas & Grunkemeier (1975) and Section 11 in Gehan (1965)

**References**

Freireich et al (1963) *Blood* 21(6):699-716

Gehan (1965) *Biometrika* 52:203-223

Thomas & Grunkemeier (1975) *JASA* 70(352): 865-871

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KaplanMeier	<i>Risk and survival probability estimates using the Kaplan-Meier method</i>
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**Description**

Computes the Kaplan-Meier estimator to estimate a risk or, equivalently, a survival probability, with right-censored data, together with a confidence interval and (possibly) a p-value (for a one-sample hypothesis test). Computation of confidence intervals and p-values is based on either Empirical Likelihood (EL) inference or Wald-type inference. Both are non-parametric approaches, which are asymptotically equivalent. See Thomas & Grunkemeier (1975) for details about the Empirical Likelihood method. For the Wald-type approach, the asymptotic normal approximation is used on the cloglog scale. See e.g. equation 4.16 in Beyersmann et al (2011).

**Usage**

```
KaplanMeier(
  time,
  status,
  t,
  risk.H0 = NULL,
  level = 0.95,
  contr = list(tol = 1e-05, k = 3, Trace = FALSE, method = "both")
)
```

**Arguments**

time	vector of times (possibly censored)
status	vector of usual survival status indicators (0 for censored observations, 1 for events)
t	the time point of interest (e.g. 1 to compute a 1-year risk or survival probability)
risk.H0	risk under the null hypothesis, if one would like to compute the corresponding p-value. Default is NULL, for which no p-value is computed.
level	confidence level for the confidence intervals. Default is 0.95.
contr	list of control parameters. tol=tolerance for numerical computation, default is 1e-5. method="EL", "Wald" or "both" indicates whether 95% CI and p-value should be computed based on Empirical Likelihood (EL) inference, Wald-type inference or both.

**Value**

object of class 'KaplanMeier'

**Author(s)**

Paul Blanche

**References**

Thomas & Grunkemeier (1975). Confidence interval estimation of survival probabilities for censored data. *Journal of the American Statistical Association*, 70(352), 865-871.

Beyersmann, Allignol, & Schumacher (2011). *Competing risks and multistate models* with R. Springer Science & Business Media.

**Examples**

```
# This example reproduces some results presented in Table 1 of Thomas and Grunkemeier (1975)
ResKM.1.95 <- KaplanMeier(time=Freireich$time[Freireich$group==1],
  status=Freireich$status[Freireich$group==1],
  t=10, level=0.95, contr=list(tol=1e-4))
ResKM.1.95
```

---

melanoma5                      *Melanoma competing risks data*

---

**Description**

These competing risks data relate to survival of patients after operation for malignant melanoma collected at Odense University Hospital between 1962 and 1977. The data are a subsample of the 'melanoma' data of the 'timereg' package (patients who had a tumor thickness of less than 5 cm).

**Usage**

```
melanoma5
```

**Format**

A data frame with 173 rows and 2 variables:

**time** time to event (in years)

**status** event status, 1 is death due to malignant melanoma, 2 is death due to another cause and 0 is censored

**Source**

'timereg' package

**References**

Andersen PK, Skovgaard LT (2010) Regression with linear predictors. Springer, Berlin

Drzewiecki K, Andersen PK (1982) Survival with malignant melanoma: a regression analysis of prognostic factors. *Cancer* 49:2414–2419

---

`print.AalenJohansen`      *Print function for object of class 'AalenJohansen'*

---

**Description**

Print function for object of class 'AalenJohansen'

**Usage**

```
## S3 method for class 'AalenJohansen'  
print(x, digits = 4, method = NULL, ...)
```

**Arguments**

<code>x</code>	an object of class 'AalenJohansen'
<code>digits</code>	number of digits to print the results
<code>method</code>	either "EL", "Wald" or "both", depending on whether we want to print the results obtained when using empirical likelihood inference (EL), Wald-type inference (Wald) or both. Default is 'NULL', which means that 'method' inherits the value of the corresponding control parameter used when creating the object 'x'.
<code>...</code>	Not used

**Value**

no return value, called for printing only.

**Author(s)**

Paul Blanche

**Examples**

```
x <- AalenJohansen(time=melanoma5$time, cause=melanoma5$status, t=4, level=0.95)
print(x, digits=3, method="EL")
```

---

`print.KaplanMeier`      *Print function for object of class 'KaplanMeier'*

---

**Description**

Print function for object of class 'KaplanMeier'

**Usage**

```
## S3 method for class 'KaplanMeier'
print(x, digits = 4, type = "risk", method = NULL, ...)
```

**Arguments**

<code>x</code>	an object of class 'KaplanMeier'
<code>digits</code>	number of digits to print the results
<code>type</code>	either "surv" or "risk" (the default), depending on whether we want to print the results in terms of a survival probability or a risk (i.e., one minus the survival probability).
<code>method</code>	either "EL", "Wald" or "both", depending on whether we want to print the results obtained when using empirical likelihood inference (EL), Wald-type inference (Wald) or both. Default is 'NULL', which means that 'method' inherits the value of the corresponding control parameter used when creating the object 'x'.
<code>...</code>	Not used

**Value**

no return value, called for printing only.

**Author(s)**

Paul Blanche

**Examples**

```
# This example reproduces some results presented in Table 1 of Thomas and Grunkemeier (1975)
ResKM.1.95 <- KaplanMeier(time=Freireich$time[Freireich$group==1],
                        status=Freireich$status[Freireich$group==1],
                        t=10, level=0.95, contr=list(tol=1e-4))
print(ResKM.1.95, digits=3, type="surv", method="EL") # EL results for survival
print(ResKM.1.95, digits=3, type="risk", method="Wald") # Wald results for risk
```

---

```
print.TwoSampleAalenJohansen
```

*Print function for object of class 'TwoSampleAalenJohansen'*

---

**Description**

Print function for object of class 'TwoSampleAalenJohansen'

**Usage**

```
## S3 method for class 'TwoSampleAalenJohansen'
print(x, digits = 4, what = "both", method = NULL, absRisk = TRUE, ...)
```

**Arguments**

x	an object of class 'TwoSampleAalenJohansen'
digits	number of digits to print the results
what	either "RR", "Diff" or "both" (default), depending on whether we want to print the results for the risk ratio (RR), the risk difference (Diff) or both.
method	either "EL", "Wald" or "both", depending on whether we want to print the results obtained when using empirical likelihood inference (EL), Wald-type inference (Wald) or both. Default is 'NULL', which means that 'method' inherits the value of the corresponding control parameter used when creating the object 'x'.
absRisk	Default is TRUE and this should not be changed.
...	Not used

**Value**

no return value, called for printing only.

**Author(s)**

Paul Blanche

**Examples**

```
## A simple example for Wald-type inference, using simulated data.
## It illustrates the possible inconsistency of Wald-type inference, in
## terms of statistical significance, when inference is based on the risk
## ratio and on the risk difference. This inconsistency cannot exist
## using an empirical likelihood approach.

ResSimA100 <- TwoSampleAalenJohansen(time=SimA100$time,
                                     cause=SimA100$status,
                                     group=SimA100$group,
                                     t=1,
                                     contr=list(method="Wald"))

print(ResSimA100, digits=3, what="Diff")
print(ResSimA100, digits=3, what="RR")

## Same example data, but now analyzed with an empirical likelihood approach. It
## takes approx 20 seconds to run.

ResSimA100 <- TwoSampleAalenJohansen(time=SimA100$time,
                                     cause=SimA100$status,
                                     group=SimA100$group,
                                     t=1)

print(ResSimA100, digits=3, what="Diff", method="EL")
```

---

```
print.TwoSampleKaplanMeier
```

*Print function for object of class 'TwoSampleKaplanMeier'*

---

**Description**

Print function for object of class 'TwoSampleKaplanMeier'

**Usage**

```
## S3 method for class 'TwoSampleKaplanMeier'
print(x, digits = 4, what = "all", method = NULL, ...)
```

**Arguments**

<code>x</code>	an object of class 'TwoSampleKaplanMeier'
<code>digits</code>	number of digits to print the results

what	either "SR", "RR", "Diff" or "all" (default), depending on whether we want to print the results for the survival ratio (SR), the risk ratio (RR), the risk difference (Diff) or all of them.
method	either "EL", "Wald" or "both", depending on whether we want to print the results obtained when using empirical likelihood inference (EL), Wald-type inference (Wald) or both. Default is 'NULL', which means that 'method' inherits the value of the corresponding control parameter used when creating the object 'x'.
...	Not used

**Value**

no return value, called for printing only.

**Author(s)**

Paul Blanche

**Examples**

```
# This example reproduces some results presented in Table 4 of Thomas and Grunkemeier (1975)
Res2SKM95 <- TwoSampleKaplanMeier(time=Freireich$time,
                                status=Freireich$status,
                                group=Freireich$group,
                                t=10)
print(Res2SKM95, digits=3, what="SR", method="EL")
```

---

SimA100

*Simulated competing risks data*

---

**Description**

The data were simulated as described in Blanche & Eriksson (2023), using scenario A with sample size  $n=100$ .

**Usage**

```
SimA100
```

**Format**

A data frame with 100 rows and 3 variables:

**time** time to event

**status** event status, 1 is main event, 2 is competing event, 0 is censored.

**group** group (1 or 0)

**Source**

Simulated data

**References**

Blanche & Eriksson (2023). Empirical likelihood comparison of absolute risks.

---

TwoSampleAalenJohansen

*Risk difference and ratio using the Aalen-Johansen method*

---

**Description**

Computes an (absolute) risk difference or ratio with right-censored competing risks data, together with a confidence interval and a p-value (to test for a difference between the two risks). Pointwise estimates are computed via the Aalen-Johansen estimator. Computation of confidence intervals and p-values are based on either Empirical Likelihood (EL) inference or Wald-type inference. Both are non-parametric approaches, which are asymptotically equivalent. For the Wald-type approach, the asymptotic normal approximation is used on the log scale for the risk ratio. No transformation is used for the risk difference. See Blanche & Eriksson (2023) for details.

**Usage**

```
TwoSampleAalenJohansen(
  time,
  cause,
  group,
  t,
  RR.H0 = 1,
  Diff.H0 = 0,
  level = 0.95,
  contr = list(tol = 1e-05, algo = 2, k = 3, Trace = FALSE, method = "both")
)
```

**Arguments**

time	vector of times (possibly censored)
cause	vector of event types/causes. It should be coded 1 for main events, 2 for competing events and 0 for censored.
group	vector of binary group indicator. The reference group should be coded 0, the other 1.
t	the time point of interest (e.g. 1 to compute a 1-year risk ratio)
RR.H0	the risk ratio under the null hypothesis, to compute a p-value. Default is 1.
Diff.H0	the risk difference under the null hypothesis, to compute a p-value. Default is 0.
level	confidence level for the confidence intervals. Default is 0.95.

`contr` list of control parameters. `tol`=tolerance for numerical computation, default is  $1e-5$ . `method`="EL", "Wald" or "both" indicates whether 95% CI and the p-value should be computed based on Empirical Likelihood (EL) inference, Wald-type inference or both. `algo`=2 (default) or 1, depending on which computational method should be used to maximize the empirical likelihood (method 1 or 2, as described in Blanche & Eriksson (2023))

### Value

an object of class 'TwoSampleAalenJohansen'

### Author(s)

Paul Blanche

### References

Blanche & Eriksson (2023). Empirical likelihood comparison of absolute risks.

### Examples

```
## A simple example for Wald-type inference, using simulated data.
## It illustrates the possible inconsistency of Wald-type inference, in
## terms of statistical significance, when inference is based on the risk
## ratio and on the risk difference. This inconsistency cannot exist
## using an empirical likelihood approach.
```

```
ResSimA100 <- TwoSampleAalenJohansen(time=SimA100$time,
                                     cause=SimA100$status,
                                     group=SimA100$group,
                                     t=1,
                                     contr=list(method="Wald"))
```

```
ResSimA100
```

```
## Same example data, but now analyzed with an empirical likelihood approach. It
## takes approx 20 seconds to run.
```

```
ResSimA100 <- TwoSampleAalenJohansen(time=SimA100$time,
                                     cause=SimA100$status,
                                     group=SimA100$group,
                                     t=1)
```

```
ResSimA100
```

---

TwoSampleKaplanMeier *Risk difference and risk ratio using the Kaplan-Meier method*

---

### Description

Computes a risk difference, risk ratio or survival ratio with right-censored data, together with a confidence interval and a p-value (to test for a difference between two groups). Pointwise estimates are computed via the Kaplan-Meier estimator. Computation of confidence intervals and p-values are based on either Empirical Likelihood (EL) inference or Wald-type inference. Both are non-parametric approaches, which are asymptotically equivalent. See Thomas & Grunkemeier (1975) for details about the Empirical Likelihood method. For the Wald-type approach, the asymptotic normal approximation is used on the log scale for the risk ratio or survival ratio. No transformation is used for the risk or survival difference.

### Usage

```
TwoSampleKaplanMeier(
  time,
  status,
  group,
  t,
  SR.H0 = 1,
  RR.H0 = 1,
  Diff.H0 = 0,
  level = 0.95,
  contr = list(tol = 1e-05, algo = 2, k = 3, Trace = FALSE, method = "both")
)
```

### Arguments

time	vector of times (possibly censored)
status	vector of usual survival status indicators (0 for censored observations, 1 otherwise)
group	vector of binary group indicator. The reference group should be coded 0, the other 1.
t	the time point of interest (e.g. 1 to compute 1-year risk ratio)
SR.H0	the survival ratio under the null hypothesis, to compute a p-value. Default is 1.
RR.H0	the risk ratio under the null hypothesis, to compute a p-value. Default is 1.
Diff.H0	the risk difference under the null hypothesis, to compute a p-value. Default is 0.
level	confidence level for the confidence intervals. Default is 0.95.
contr	list of control parameters. tol=tolerance for numerical computation, default is 1e-5. method="EL", "Wald" or "both" indicates whether 95% CI and the p-value should be computed based on Empirical Likelihood inference, Wald-type inference or both. algo=2 is currently the only option that is implemented.

**Value**

an object of class 'TwoSampleKaplanMeier'

**Author(s)**

Paul Blanche

**References**

Thomas & Grunkemeier (1975). Confidence interval estimation of survival probabilities for censored data. *Journal of the American Statistical Association*, 70(352), 865-871.

**Examples**

```
# This example reproduces some results presented in Table 4 of Thomas and Grunkemeier (1975)
Res2SKM95 <- TwoSampleKaplanMeier(time=Freireich$time,
                                  status=Freireich$status,
                                  group=Freireich$group,
                                  t=10)

Res2SKM95
```

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