Package 'tripack'

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Title Triangulation of Irregularly Spaced Data

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Description A constrained two-dimensional Delaunay triangulation package providing both triangulation and generation of voronoi mosaics of irregular spaced data.
Please note that most of the functions are now also covered in package interp, which is a re-implementation from scratch under a free license based on a different triangulation algorithm.

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Contents

`add.constraint` *Add a constraint to an triangulaion object*

Description

This subroutine provides for creation of a constrained Delaunay triangulation which, in some sense, covers an arbitrary connected region R rather than the convex hull of the nodes. This is achieved simply by forcing the presence of certain adjacencies (triangulation arcs) corresponding to constraint curves. The union of triangles coincides with the convex hull of the nodes, but triangles in R can be distinguished from those outside of R. The only modification required to generalize the definition of the Delaunay triangulation is replacement of property 5 (refer to `tri.mesh` by the following:

5') If a node is contained in the interior of the circumcircle of a triangle, then every interior point of the triangle is separated from the node by a constraint arc.

In order to be explicit, we make the following definitions. A constraint region is the open interior of a simple closed positively oriented polygonal curve defined by an ordered sequence of three or more distinct nodes (constraint nodes) P(1),P(2),...,P(K), such that P(I) is adjacent to P(I+1) for I = 1,...,K with P(K+1) = P(1). Thus, the constraint region is on the left (and may have nonfinite area) as the sequence of constraint nodes is traversed in the specified order. The constraint regions must

not contain nodes and must not overlap. The region R is the convex hull of the nodes with constraint regions excluded.

Note that the terms boundary node and boundary arc are reserved for nodes and arcs on the boundary of the convex hull of the nodes.

The algorithm is as follows: given a triangulation which includes one or more sets of constraint nodes, the corresponding adjacencies (constraint arcs) are forced to be present (Fortran subroutine EDGE). Any additional new arcs required are chosen to be locally optimal (satisfy the modified circumcircle property).

Usage

```
add.constraint(tri.obj,cstx,csty,reverse=FALSE)
```

Arguments

`tri.obj`	object of class `"tri"`
`cstx`	vector containing x coordinates of the constraint curve.
`csty`	vector containing y coordinates of the constraint curve.
`reverse`	if `TRUE` the orientation of the constraint curve is reversed.

Value

An new object of class `"tri"`.

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`, `print.tri`, `plot.tri`, `summary.tri`, `triangles`, `convex.hull`.

Examples

```
# we will use the simple test data from TRIPACK:
data(tritest)
tritest.tr<-tri.mesh(tritest)
opar<-par(mfrow=c(2,2))
plot(tritest.tr)
# include all points in a big triangle:
tritest.tr<-add.constraint(tritest.tr,c(-0.1,2,-0.1),
                                      c(-3,0.5,3),reverse=TRUE)
# insert a small cube:
tritest.tr <- add.constraint(tritest.tr, c(0.4, 0.4,0.6, 0.6),
                                         c(0.6, 0.4,0.4, 0.6),
                                         reverse = FALSE)
par(opar)
```

`cells` *extract info about voronoi cells*

Description

This function returns some info about the cells of a voronoi mosaic, including the coordinates of the vertices and the cell area.

Usage

```
cells(voronoi.obj)
```

Arguments

`voronoi.obj`	object of class `voronoi`

Details

The function calculates the neighbourhood relations between the underlying triangulation and translates it into the neighbourhood relations between the voronoi cells.

Value

retruns a list of lists, one entry for each voronoi cell which contains

`cell`	cell index
`center`	cell 'center'
`neighbours`	neighbour cell indices
`nodes`	2 times `nnb` matrix with vertice coordinates
`area`	cell area

Note

outer cells have `area=NA`, currently also `nodes=NA` which is not really useful – to be done later

Author(s)

A. Gebhardt

See Also

`voronoi.mosaic`, `voronoi.area`

Examples

```
data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x,tritest$y)
tritest.cells <- cells(tritest.vm)
# higlight cell 12:
plot(tritest.vm)
polygon(t(tritest.cells[[12]]$nodes),col="green")
# put cell area into cell center:
text(tritest.cells[[12]]$center[1],
     tritest.cells[[12]]$center[2],
     tritest.cells[[12]]$area)
```

---

circles *plot circles*

Description

This function plots circles at given locations with given radii.

Usage

```
circles(x, y, r, ...)
```

Arguments

x	vector of x coordinates
y	vector of y coordinates
r	vactor of radii
...	additional graphic parameters will be passed through

Note

This function needs a previous plot where it adds the circles.

Author(s)

A. Gebhardt

See Also

lines, points

Examples

```
x<-rnorm(10)
y<-rnorm(10)
r<-runif(10,0,0.5)
plot(x,y, xlim=c(-3,3), ylim=c(-3,3), pch="+")
circles(x,y,r)
```

circtest *circtest / sample data*

Description

Sample data for the link{circumcircle} function.

circtest2 are points sampled from a circle with some jitter added, i.e. they represent the most complicated case for the link{circumcircle} function.

circum *Determine the circumcircle of a triangle*

Description

This function returns the circumcircle of a triangle.

Usage

```
circum(x, y)
```

Arguments

x	Vector of three elements, giving the x coordinatres of the triangle nodes.
y	Vector of three elements, giving the y coordinatres of the triangle nodes.

Details

This is an interface to the Fortran function CIRCUM found in TRIPACK.

Value

x	'x' coordinate of center
y	'y' coordinate of center
radius	circumcircle radius
signed.area	signed area of riangle (positive iff nodes are numbered counter clock wise)
aspect.ratio	ratio "radius of inscribed circle"/"radius of circumcircle", varies between 0 and 0.5 0 means collinear points, 0.5 equilateral trangle.

Note

This function is mainly intended to be used by circumcircle.

Author(s)

Fortran code: R. J. Renka, R code: A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

circumcircle

Examples

```
circum(c(0,1,0),c(0,0,1))
```

---

circumcircle *Determine the circumcircle of a set of points*

Description

This function returns the (smallest) circumcircle of a set of n points

Usage

```
circumcircle(x, y = NULL, num.touch=2, plot = FALSE, debug = FALSE)
```

Arguments

x	vector containing x coordinates of the data. If y is missing x should contain two elements $x and $y.
y	vector containing y coordinates of the data.
num.touch	How often should the resulting circle touch the convex hull of the given points? default: 2 possible values: 2 or 3 Note: The circumcircle of a triangle is usually defined to touch at 3 points, this function searches by default the minimum circle, which may be only touching at 2 points. Set parameter num.touch accordingly if you dont want the default behaviour!
plot	Logical, produce a simple plot of the result. default: FALSE
debug	Logical, more plots, only needed for debugging. default: FALSE

Details

This is a (naive implemented) algorithm which determines the smallest circumcircle of n points:

First step: Take the convex hull.

Second step: Determine two points on the convex hull with maximum distance for the diameter of the set.

Third step: Check if the circumcircle of these two points already contains all other points (of the convex hull and hence all other points).

If not or if 3 or more touching points are desired (`num.touch=3`), search a point with minimum enclosing circumcircle among the remaining points of the convex hull.

If such a point cannot be found (e.g. for `data(circtest2)`), search the remaining triangle combinations of points from the convex hull until an enclosing circle with minimum radius is found.

The last search uses an upper and lower bound for the desired miniumum radius:

Any enclosing rectangle and its circumcircle gives an upper bound (the axis-parallel rectangle is used).

Half the diameter of the set from step 1 is a lower bound.

Value

`x`	'x' coordinate of circumcircle center
`y`	'y' coordinate of circumcircle center
`radius`	radius of circumcircle

Author(s)

Albrecht Gebhardt

See Also

`convex.hull`

Examples

```
data(circtest)
# smallest circle:
circumcircle(circtest,num.touch=2,plot=TRUE)

# smallest circle with maximum touching points (3):
circumcircle(circtest,num.touch=3,plot=TRUE)

# some stress test for this function,
data(circtest2)
# circtest2 was generated by:
# 100 random points almost one a circle:
# alpha <- runif(100,0,2*pi)
# x <- cos(alpha)
# y <- sin(alpha)
# circtest2<-list(x=cos(alpha)+runif(100,0,0.1),
```

```
#                 y=sin(alpha)+runif(100,0,0.1))
#
circumcircle(circtest2,plot=TRUE)
```

---

convex.hull *Return the convex hull of a triangulation object*

Description

Given a triangulation `tri.obj` of n points in the plane, this subroutine returns two vectors containing the coordinates of the nodes on the boundary of the convex hull.

Usage

```
convex.hull(tri.obj, plot.it=FALSE, add=FALSE,...)
```

Arguments

`tri.obj`	object of class `"tri"`
`plot.it`	logical, if `TRUE` the convex hull of `tri.obj` will be plotted.
`add`	logical. if `TRUE` (and `plot.it=TRUE`), add to a current plot.
`...`	additional plot arguments

Value

`x`	x coordinates of boundary nodes.
`y`	y coordinates of boundary nodes.

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`, `print.tri`, `plot.tri`, `summary.tri`, `triangles`, `add.constraint`.

Examples

```
# rather simple example from TRIPACK:
data(tritest)
tr<-tri.mesh(tritest$x,tritest$y)
convex.hull(tr,plot.it=TRUE)
# random points:
rand.tr<-tri.mesh(runif(10),runif(10))
plot(rand.tr)
rand.ch<-convex.hull(rand.tr, plot.it=TRUE, add=TRUE, col="red")
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-17 & quakes[,1]>=-19.0 &
                     quakes[,2]<=182.0 & quakes[,2]>=180.0),]
quakes.tri<-tri.mesh(quakes.part$lon, quakes.part$lat, duplicate="remove")
plot(quakes.tri)
convex.hull(quakes.tri, plot.it=TRUE, add=TRUE, col="red")
```

`identify.tri` *Identify points in a triangulation plot*

Description

Identify points in a plot of `"x"` with its coordinates. The plot of `"x"` must be generated with `plot.tri`.

Usage

```
## S3 method for class 'tri'
identify(x,...)
```

Arguments

`x`	object of class `"tri"`
`...`	additional paramters for `identify`

Value

an integer vector containing the indexes of the identified points.

Author(s)

A. Gebhardt

See Also

`tri`, `print.tri`, `plot.tri`, `summary.tri`

Examples

```
data(tritest)
tritest.tr<-tri.mesh(tritest$x,tritest$y)
plot(tritest.tr)
identify.tri(tritest.tr)
```

`in.convex.hull` *Determines if points are in the convex hull of a triangulation object*

Description

Given a triangulation `tri.obj` of n points in the plane, this subroutine returns a logical vector indicating if the points (x_i, y_i) are contained within the convex hull of `tri.obj`.

Usage

```
in.convex.hull(tri.obj, x, y)
```

Arguments

`tri.obj`	object of class `"tri"`
`x`	vector of x-coordinates of points to locate
`y`	vector of y-coordinates of points to locate

Value

Logical vector.

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`, `print.tri`, `plot.tri`, `summary.tri`, `triangles`, `add.constraint`, `convex.hull`.

Examples

```
# example from TRIPACK:
data(tritest)
tr<-tri.mesh(tritest$x,tritest$y)
in.convex.hull(tr,0.5,0.5)
in.convex.hull(tr,c(0.5,-1,1),c(0.5,1,1))
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-10.78 & quakes[,1]>=-19.4 &
                     quakes[,2]<=182.29 & quakes[,2]>=165.77),]
q.tri<-tri.mesh(quakes.part$lon, quakes.part$lat, duplicate="remove")
in.convex.hull(q.tri,quakes$lon[990:1000],quakes$lat[990:1000])
```

`left` *Determines whether given points are left of a directed edge.*

Description

This function returns a logical vector indicating which elements of the given points P0 are left of the directed edge P1->P2.

Usage

```
left(x0, y0, x1, y1, x2, y2)
```

Arguments

`x0`	Numeric vector, 'x' coordinates of points P0 to check
`y0`	Numeric vector, 'y' coordinates of points P0 to check, same length as 'x'.
`x1`	'x' coordinate of point P1
`y1`	'y' coordinate of point P1
`x2`	'x' coordinate of point P2
`y2`	'y' coordinate of point P2

Value

Logical vector.

Note

This is an interface to the Fortran function VLEFT, wich is modeled after TRIPACKs LEFT function but accepts more than one point P0.

Author(s)

A. Gebhardt

See Also

in.convex.hull

Examples

```
left(c(0,0,1,1),c(0,1,0,1),0,0,1,1)
```

---

neighbours *List of neighbours from a triangulation object*

Description

Extract a list of neighbours from a triangulation object

Usage

```
neighbours(tri.obj)
```

Arguments

tri.obj	object of class "tri"

Value

nested list of neighbours per point

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

tri, print.tri, plot.tri, summary.tri, triangles

Examples

```
data(tritest)
tritest.tr<-tri.mesh(tritest$x,tritest$y)
tritest.nb<-neighbours(tritest.tr)
```

`on.convex.hull` *Determines if points are on the convex hull of a triangulation object*

Description

Given a triangulation `tri.obj` of n points in the plane, this subroutine returns a logical vector indicating if the points (x_i, y_i) lay on the convex hull of `tri.obj`.

Usage

```
on.convex.hull(tri.obj, x, y)
```

Arguments

`tri.obj`	object of class `"tri"`
`x`	vector of x-coordinates of points to locate
`y`	vector of y-coordinates of points to locate

Value

Logical vector.

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`, `print.tri`, `plot.tri`, `summary.tri`, `triangles`, `add.constraint`, `convex.hull`, `in.convex.hull`.

Examples

```
# example from TRIPACK:
data(tritest)
tr<-tri.mesh(tritest$x,tritest$y)
on.convex.hull(tr,0.5,0.5)
on.convex.hull(tr,c(0.5,-1,1),c(0.5,1,1))
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-10.78 & quakes[,1]>=-19.4 &
                     quakes[,2]<=182.29 & quakes[,2]>=165.77),]
q.tri<-tri.mesh(quakes.part$lon, quakes.part$lat, duplicate="remove")
on.convex.hull(q.tri,quakes.part$lon[1:20],quakes.part$lat[1:20])
```

`outer.convhull` *Version of outer which operates only in a convex hull*

Description

This version of `outer` evaluates `FUN` only on that part of the grid $cxxcy$ that is enclosed within the convex hull of the points (`px`,`py`).

This can be useful for spatial estimation if no extrapolation is wanted.

Usage

```
outer.convhull(cx,cy,px,py,FUN,duplicate="remove",...)
```

Arguments

`cx`	x cordinates of grid
`cy`	y cordinates of grid
`px`	vector of x coordinates of points
`py`	vector of y coordinates of points
`FUN`	function to be evaluated over the grid
`duplicate`	indicates what to do with duplicate (px_i, py_i) points, default `"remove"`.
`...`	additional arguments for `FUN`

Value

Matrix with values of `FUN` (`NA`s if outside the convex hull).

Author(s)

A. Gebhardt

See Also

`in.convex.hull`

Examples

```
x<-runif(20)
y<-runif(20)
z<-runif(20)
z.lm<-lm(z~x+y)
f.pred<-function(x,y)
  {predict(z.lm,data.frame(x=as.vector(x),y=as.vector(y)))}
xg<-seq(0,1,0.05)
yg<-seq(0,1,0.05)
image(xg,yg,outer.convhull(xg,yg,x,y,f.pred))
points(x,y)
```

plot.tri *Plot a triangulation object*

Description

plots the triangulation "x"

Usage

```
## S3 method for class 'tri'
plot(x, add=FALSE,xlim=range(x$x),ylim=range(x$y),
  do.points=TRUE, do.labels = FALSE, isometric=FALSE,...)
```

Arguments

x	object of class "tri"
add	logical, if TRUE, add to a current plot.
do.points	logical, indicates if points should be plotted.
do.labels	logical, indicates if points should be labelled
xlim, ylim	x/y ranges for plot
isometric	generate an isometric plot (default FALSE)
...	additional plot parameters

Value

None

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

tri, print.tri, summary.tri

Examples

```
# random points
plot(tri.mesh(rpois(100,lambda=20),rpois(100,lambda=20),duplicate="remove"))
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-10.78 & quakes[,1]>=-19.4 &
                     quakes[,2]<=182.29 & quakes[,2]>=165.77),]
quakes.tri<-tri.mesh(quakes.part$lon, quakes.part$lat, duplicate="remove")
plot(quakes.tri)
# use the whole quakes data set
# (will not work with standard memory settings, hence commented out)
#plot(tri.mesh(quakes$lon, quakes$lat, duplicate="remove"), do.points=F)
```

`plot.voronoi` *Plot a voronoi object*

Description

Plots the mosaic `"x"`.

Dashed lines are used for outer tiles of the mosaic.

Usage

```
## S3 method for class 'voronoi'
plot(x,add=FALSE,
                            xlim=c(min(x$tri$x)-
                              0.1*diff(range(x$tri$x)),
                              max(x$tri$x)+
                              0.1*diff(range(x$tri$x))),
                            ylim=c(min(x$tri$y)-
                              0.1*diff(range(x$tri$y)),
                              max(x$tri$y)+
                              0.1*diff(range(x$tri$y))),
                            all=FALSE,
                            do.points=TRUE,
                            main="Voronoi mosaic",
                            sub=deparse(substitute(x)),
                            isometric=FALSE,
                            ...)
```

Arguments

`x`	object of class `"voronoi"`
`add`	logical, if `TRUE`, add to a current plot.
`xlim`	x plot ranges, by default modified to hide dummy points outside of the plot
`ylim`	y plot ranges, by default modified to hide dummy points outside of the plot

all	show all (including dummy points in the plot
do.points	logical, indicates if points should be plotted.
main	plot title
sub	plot subtitle
isometric	generate an isometric plot (default FALSE)
...	additional plot parameters

Value

None

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

voronoi, print.voronoi, summary.voronoi

Examples

```
# plot a random mosaic
plot(voronoi.mosaic(runif(100),runif(100),duplicate="remove"))
# use isometric=TRUE and all=TRUE to see the complete mosaic
# including extreme outlier points:
plot(voronoi.mosaic(runif(100),runif(100),duplicate="remove"),
     all=TRUE, isometric=TRUE)
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-17 & quakes[,1]>=-19.0 &
                     quakes[,2]<=182.0 & quakes[,2]>=180.0),]
quakes.vm<-voronoi.mosaic(quakes.part$lon, quakes.part$lat,
                          duplicate="remove")
plot(quakes.vm, isometric=TRUE)
# use the whole quakes data set
# (will not work with standard memory settings, hence commented out here)
#plot(voronoi.mosaic(quakes$lon, quakes$lat, duplicate="remove"), isometric=TRUE)
```

`plot.voronoi.polygons` *plots an voronoi.polygons object*

Description

plots an `voronoi.polygons` object

Usage

```
## S3 method for class 'voronoi.polygons'
plot(x, which, color=TRUE, ...)
```

Arguments

`x`	object of class `voronoi.polygons`
`which`	index vector selecting which polygons to plot
`color`	logical, determines if plot should be colored, default: `TRUE`
`...`	additional plot arguments

Author(s)

A. Gebhardt

See Also

`voronoi.polygons`

Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==>  Define data, use random,
##--     or do  help(data=index)  for the standard data sets.
data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x,tritest$y)
tritest.vp <- voronoi.polygons(tritest.vm)
plot(tritest.vp)
plot(tritest.vp,which=c(1,3,5))
```

print.summary.tri *Print a summary of a triangulation object*

Description

Prints some information about `tri.obj`

Usage

```
## S3 method for class 'summary.tri'
print(x, ...)
```

Arguments

`x`	object of class `"summary.tri"`, generated by `summary.tri`.
`...`	additional paramters for `print`

Value

None

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`,`tri.mesh`, `print.tri`, `plot.tri`, `summary.tri`.

print.summary.voronoi *Print a summary of a voronoi object*

Description

Prints some information about `x`

Usage

```
## S3 method for class 'summary.voronoi'
print(x, ...)
```

Arguments

x	object of class "summary.voronoi", generated by summary.voronoi.
...	additional paramters for print

Value

None

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

voronoi,voronoi.mosaic, print.voronoi, plot.voronoi, summary.voronoi.

---

print.tri *Print a triangulation object*

Description

prints a adjacency list of "x"

Usage

```
## S3 method for class 'tri'
print(x,...)
```

Arguments

x	object of class "tri"
...	additional paramters for print

Value

None

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`, `plot.tri`, `summary.tri`

`print.voronoi` *Print a voronoi object*

Description

prints a summary of `"x"`

Usage

```
## S3 method for class 'voronoi'
print(x,...)
```

Arguments

`x`	object of class `"voronoi"`
`...`	additional paramters for `print`

Value

None

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`voronoi`, `plot.voronoi`, `summary.voronoi`

summary.tri *Return a summary of a triangulation object*

Description

Returns some information (number of nodes, triangles, arcs, boundary nodes and constraints) about `object`.

Usage

```
## S3 method for class 'tri'
summary(object,...)
```

Arguments

`object`	object of class `"tri"`
`...`	additional paramters for `summary`

Value

An objekt of class `"summary.tri"`, to be printed by `print.summary.tri`.

It contains the number of nodes (`n`), of arcs (`na`), of boundary nodes (`nb`), of triangles (`nt`) and constraints (`nc`).

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`, `print.tri`, `plot.tri`, `print.summary.tri`.

summary.voronoi *Return a summary of a voronoi object*

Description

Returns some information about object

Usage

```
## S3 method for class 'voronoi'
summary(object,...)
```

Arguments

object	object of class "voronoi"
...	additional parameters for summary

Value

Object of class "summary.voronoi".

It contains the number of nodes (nn) and dummy nodes (nd).

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

voronoi,voronoi.mosaic, print.voronoi, plot.voronoi, print.summary.voronoi.

tri *A triangulation object*

Description

R object that represents the triangulation of a set of 2D points, generated by `tri.mesh` or `add.constraint`.

Arguments

`n`	Number of nodes
`x`	x coordinates of the triangulation nodes
`y`	y coordinates of the triangulation nodes
`tlist`	Set of nodal indexes which, along with `tlptr`, `tlend`, and `tlnew`, define the triangulation as a set of n adjacency lists – counterclockwise-ordered sequences of neighboring nodes such that the first and last neighbors of a boundary node are boundary nodes (the first neighbor of an interior node is arbitrary). In order to distinguish between interior and boundary nodes, the last neighbor of each boundary node is represented by the negative of its index.
`tlptr`	Set of pointers in one-to-one correspondence with the elements of `tlist`. `tlist[tlptr[i]]` indexes the node which follows `tlist[i]` in cyclical counterclockwise order (the first neighbor follows the last neighbor).
`tlend`	Set of pointers to adjacency lists. `tlend[k]` points to the last neighbor of node k for $k = 1, ..., n$. Thus, `tlist[tlend[k]]`<0 if and only if k is a boundary node.
`tlnew`	Pointer to the first empty location in `tlist` and `tlptr` (list length plus one).
`nc`	number of constraints
`lc`	starting indices of constraints in `x` and `y`
`call`	call, which generated this object

Note

The elements `tlist`, `tlptr`, `tlend` and `tlnew` are mainly intended for internal use in the appropriate Fortran routines.

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri.mesh`, `print.tri`, `plot.tri`, `summary.tri`

`tri.dellens` *Compute the Delaunay segment lengths*

Description

Return a vector of Delaunay segment lengths for the voronoi object. The Delaunay triangles connected to sites contained in `exceptions` vector are ignored (unless `inverse` is TRUE, when only those Delaunay triangles are accepted).

The `exceptions` vector is provided so that sites at the border of a region can be removed, as these tend to bias the distribution of Delaunay segment lengths. `exceptions` can be created by `voronoi.findrejectsites`.

Usage

```
tri.dellens(voronoi.obj, exceptions = NULL, inverse = FALSE)
```

Arguments

`voronoi.obj`	object of class `"voronoi"`
`exceptions`	a numerical vector
`inverse`	Logical

Value

A vector of Delaunay segment lengths.

Author(s)

S. J. Eglen

See Also

`voronoi.findrejectsites`, `voronoi.mosaic`,

Examples

```
data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x,tritest$y)

tritest.vm.rejects <- voronoi.findrejectsites(tritest.vm, 0,1, 0, 1)
trilens.all <- tri.dellens(tritest.vm)
trilens.acc <- tri.dellens(tritest.vm, tritest.vm.rejects)
trilens.rej <- tri.dellens(tritest.vm, tritest.vm.rejects, inverse=TRUE)

par(mfrow=c(3,1))
dotchart(trilens.all, main="all Delaunay segment lengths")
dotchart(trilens.acc, main="excluding border sites")
dotchart(trilens.rej, main="only border sites")
```

`tri.find` *Locate a point in a triangulation*

Description

This subroutine locates a point P=(x,y) relative to a triangulation created by `tri.mesh`. If P is contained in a triangle, the three vertex indexes are returned. Otherwise, the indexes of the rightmost and leftmost visible boundary nodes are returned.

Usage

```
tri.find(tri.obj,x,y)
```

Arguments

`tri.obj`	an triangulation object
`x`	x-coordinate of the point
`y`	y-coordinate of the point

Value

A list with elements `i1`,`i2`,`i3` containing nodal indexes, in counterclockwise order, of the vertices of a triangle containing P=(x,y), or, if P is not contained in the convex hull of the nodes, `i1` indexes the rightmost visible boundary node, `i2` indexes the leftmost visible boundary node, and `i3` = 0. Rightmost and leftmost are defined from the perspective of P, and a pair of points are visible from each other if and only if the line segment joining them intersects no triangulation arc. If P and all of the nodes lie on a common line, then `i1=i2=i3` = 0 on output.

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`, `print.tri`, `plot.tri`, `summary.tri`, `triangles`, `convex.hull`

Examples

```
data(tritest)
tritest.tr<-tri.mesh(tritest$x,tritest$y)
plot(tritest.tr)
pnt<-list(x=0.3,y=0.4)
triangle.with.pnt<-tri.find(tritest.tr,pnt$x,pnt$y)
attach(triangle.with.pnt)
lines(tritest$x[c(i1,i2,i3,i1)],tritest$y[c(i1,i2,i3,i1)],col="red")
points(pnt$x,pnt$y)
```

`tri.mesh` *Create a delaunay triangulation*

Description

This subroutine creates a Delaunay triangulation of a set of N arbitrarily distributed points in the plane referred to as nodes. The Delaunay triangulation is defined as a set of triangles with the following five properties:

1) The triangle vertices are nodes.

2) No triangle contains a node other than its vertices.

3) The interiors of the triangles are pairwise disjoint.

4) The union of triangles is the convex hull of the set of nodes (the smallest convex set which contains the nodes).

5) The interior of the circumcircle of each triangle contains no node.

The first four properties define a triangulation, and the last property results in a triangulation which is as close as possible to equiangular in a certain sense and which is uniquely defined unless four or more nodes lie on a common circle. This property makes the triangulation well-suited for solving closest point problems and for triangle-based interpolation.

The triangulation can be generalized to a constrained Delaunay triangulation by a call to `add.constraint`. This allows for user-specified boundaries defining a nonconvex and/or multiply connected region.

The operation count for constructing the triangulation is close to O(N) if the nodes are presorted on X or Y components. Also, since the algorithm proceeds by adding nodes incrementally, the triangulation may be updated with the addition (or deletion) of a node very efficiently. The adjacency information representing the triangulation is stored as a linked list requiring approximately 13N storage locations.

Usage

```
tri.mesh(x, y = NULL, duplicate = "error",
         jitter = 10^-12, jitter.iter = 6, jitter.random = FALSE)
```

Arguments

x	vector containing x coordinates of the data. If y is missing x should contain two elements $x and $y.
y	vector containing y coordinates of the data.
duplicate	flag indicating how to handle duplicate elements. Possible values are: "error" – default, "strip" – remove all duplicate points, "remove" – leave one point of duplicate points.
jitter	Jitter of amount of diff(range(XX))*jitter (XX=x or y) will be added to coordinates if collinear points are detected. Afterwards interpolation will be tried once again. Note that the jitter is not generated randomly unless jitter.random is set to TRUE. This ensures reproducable results. interp of package akima uses the same jitter mechanism. That means you can plot the triangulation on top of the interpolation and see the same triangulation as used for interpolation, see examples for interp.
jitter.iter	number of iterations to retry with jitter, amount will be increased in each iteration by iter^1.5
jitter.random	logical, see jitter, defaults to FALSE

Value

An object of class "tri"

Note

There is re-implementation of this function available in package interp under the same name with the same arguments. But the return value is of a different class. So returned objects from this function can not be used by functions of same name in package interp. But code written to use functions from this package can be reused with the new package unless a constrained triangulation is wanted. This is the only thing missing in the new implementation.

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

tri, print.tri, plot.tri, summary.tri, triangles, convex.hull, neighbours, add.constraint.

Examples

```
data(tritest)
tritest.tr<-tri.mesh(tritest$x,tritest$y)
tritest.tr
```

`triangles` *Extract a list of triangles from a triangulation object*

Description

This function extracts a triangulation data structure from an triangulation object created by `tri.mesh`.

The vertices in the returned matrix (let's denote it with `retval`) are ordered counterclockwise with the first vertex taken to be the one with smallest index. Thus, `retval[i,"node2"]` and `retval[i,"node3"]` are larger than `retval[i,"node3"]` and index adjacent neighbors of node `retval[i,"node1"]`. The columns `trx` and `arcx`, x=1,2,3 index the triangle and arc, respectively, which are opposite (not shared by) node `nodex`, with `trix`= 0 if `arcx` indexes a boundary arc. Vertex indexes range from 1 to N, triangle indexes from 0 to NT, and, if included, arc indexes from 1 to NA = NT+N-1. The triangles are ordered on first (smallest) vertex indexes, except that the sets of constraint triangles (triangles contained in the closure of a constraint region) follow the non-constraint triangles.

Usage

```
triangles(tri.obj)
```

Arguments

`tri.obj`	object of class `"tri"`

Value

A matrix with columns `node1`,`node2`,`node3`, representing the vertex nodal indexes, `tr1`,`tr2`,`tr3`, representing neighboring triangle indexes and `arc1`,`arc2`,`arc3` reresenting arc indexes.

Each row represents one triangle.

Author(s)

A. Gebhardt

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

See Also

`tri`, `print.tri`, `plot.tri`, `summary.tri`, `triangles`

Examples

```
# use a slighlty modified version of data(tritest)
data(tritest2)
tritest2.tr<-tri.mesh(tritest2$x,tritest2$y)
triangles(tritest2.tr)
```

`tripack-internal` *Internal functions*

Description

Internal tripack functions

Details

These functions are not intended to be called by the user.

`tritest` *tritest / sample data*

Description

A very simply set set of points to test the tripack functions, taken from the FORTRAN original. `tritest2` is a slight modification by adding `runif(,-0.1,0.1)` random numbers to the coordinates.

References

R. J. Renka (1996). Algorithm 751: TRIPACK: a constrained two-dimensional Delaunay triangulation package. ACM Transactions on Mathematical Software. **22**, 1-8.

voronoi *Voronoi object*

Description

An voronoi object is created with voronoi.mosaic

Arguments

x, y	x and y coordinates of nodes of the voronoi mosaic. Each node is a circumcircle center of some triangle from the Delaunay triangulation.
node	logical vector, indicating real nodes of the voronoi mosaic. These nodes are the centers of circumcircles of triangles with positive area of the delaunay triangulation. If node[i]=FALSE, (c[i],x[i]) belongs to a triangle with area 0.
n1, n2, n3	indices of neighbour nodes. Negative indices indicate dummy points as neighbours.
tri	triangulation object, see tri.
area	area of triangle i. area[i]=-1 indicates a removed triangle with area 0 at the border of the triangulation.
ratio	aspect ratio (inscribed radius/circumradius) of triangle i.
radius	circumradius of triangle i.
dummy.x, dummy.y	x and y coordinates of dummy points. They are used for plotting of unbounded tiles.

Author(s)

A. Gebhardt

See Also

voronoi.mosaic,plot.voronoi

voronoi.area *Calculate area of Voronoi polygons*

Description

Computes the area of each Voronoi polygon. For some sites at the edge of the region, the Voronoi polygon is not bounded, and so the area of those sites cannot be calculated, and hence will be NA.

Usage

```
voronoi.area(voronoi.obj)
```

Arguments

voronoi.obj	object of class "voronoi"

Value

A vector of polygon areas.

Author(s)

S. J. Eglen

See Also

voronoi,

Examples

```
data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x,tritest$y)
tritest.vm.areas <- voronoi.area(tritest.vm)
plot(tritest.vm)
text(tritest$x, tritest$y, tritest.vm.areas)
```

---

voronoi.findrejectsites

Find the Voronoi sites at the border of the region (to be rejected).

Description

Find the sites in the Voronoi tesselation that lie at the edge of the region. A site is at the edge if any of the vertices of its Voronoi polygon lie outside the rectangle with corners (xmin,ymin) and (xmax,ymax).

Usage

```
voronoi.findrejectsites(voronoi.obj, xmin, xmax, ymin, ymax)
```

Arguments

voronoi.obj	object of class "voronoi"
xmin	minimum x-coordinate of sites in the region
xmax	maximum x-coordinate of sites in the region
ymin	minimum y-coordinate of sites in the region
ymax	maximum y-coordinate of sites in the region

Value

A logical vector of the same length as the number of sites. If the site is a reject, the corresponding element of the vector is set to TRUE.

Author(s)

S. J. Eglen

See Also

tri.dellens

`voronoi.mosaic` *Create a Voronoi mosaic*

Description

This function creates a Voronoi mosaic.

It creates first a Delaunay triangulation, determines the circumcircle centers of its triangles, and connects these points according to the neighbourhood relations between the triangles.

Usage

```
voronoi.mosaic(x,y=NULL,duplicate="error")
```

Arguments

x	vector containing x coordinates of the data. If y is missing x should contain two elements $x and $y.
y	vector containing y coordinates of the data.
duplicate	flag indicating how to handle duplicate elements. Possible values are: "error" – default, "strip" – remove all duplicate points, "remove" – leave one point of duplicate points.

Value

An object of class voronoi.

Author(s)

A. Gebhardt

See Also

voronoi,voronoi.mosaic, print.voronoi, plot.voronoi

Examples

```
# example from TRIPACK:
data(tritest)
tritest.vm<-voronoi.mosaic(tritest$x,tritest$y)
tritest.vm
# use a part of the quakes data set:
data(quakes)
quakes.part<-quakes[(quakes[,1]<=-17 & quakes[,1]>=-19.0 &
                     quakes[,2]<=182.0 & quakes[,2]>=180.0),]
quakes.vm<-voronoi.mosaic(quakes.part$lon, quakes.part$lat, duplicate="remove")
quakes.vm
```

---

voronoi.polygons *extract polygons from a voronoi mosaic*

Description

This functions extracts polygons from a `voronoi.mosaic` object.

Usage

```
voronoi.polygons(voronoi.obj)
```

Arguments

`voronoi.obj`	object of class `voronoi.mosaic`

Value

Returns an object of class `voronoi.polygons` with unamed list elements for each polygon. These list elements are matrices with columns `x` and `y`.

Author(s)

Denis White

See Also

`plot.voronoi.polygons`,`voronoi.mosaic`

Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==>  Define data, use random,
##--     or do  help(data=index)  for the standard data sets.

data(tritest)
tritest.vm <- voronoi.mosaic(tritest$x,tritest$y)
tritest.vp <- voronoi.polygons(tritest.vm)
tritest.vp
```

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