

# Package ‘tseriesChaos’

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**Title** Analysis of Nonlinear Time Series

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**Depends** R (>= 2.2.0)

**Imports** deSolve

**Suggests** scatterplot3d

**LazyData** yes

**LazyLoad** yes

**Description** Routines for the analysis of nonlinear time series. This work is largely inspired by the TISEAN project, by Rainer Hegger, Holger Kantz and Thomas Schreiber:  
<<http://www.mpipks-dresden.mpg.de/~tisean/>>.

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C2	<i>Sample correlation integral</i>
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### Description

Sample correlation integral for the specified length scale

### Usage

`C2(series, m, d, t, eps)`

### Arguments

<code>series</code>	time series
<code>m</code>	embedding dimension
<code>d</code>	time delay
<code>t</code>	Theiler window
<code>eps</code>	length scale

### Details

Computes the sample correlation integral on the provided time series for the specified length scale, and considering a time window `t` (see references). It uses a naive algorithm: simply returns the fraction of points pairs nearer than `eps`. Normally, you would use `d2`, which takes roughly the same time, but computes the correlation sum for multiple length scales and embedding dimensions at once.

### Value

The sample correlation integral at `eps` length scale.

### Author(s)

Antonio, Fabio Di Narzo

**References**

Hegger, R., Kantz, H., Schreiber, T., Practical implementation of nonlinear time series methods: The TISEAN package; CHAOS 9, 413-435 (1999)

**See Also**

[d2](#)

---

d2

---

*Sample correlation integral (at multiple length scales)*


---

**Description**

Computes the sample correlation integral over a grid of neps length scales starting from eps.min, and for multiple embedding dimensions

**Usage**

```
d2(series, m, d, t, eps.min, neps=100)
```

**Arguments**

series	time series
m	max embedding dimension
d	time delay
t	Theiler window
eps.min	min length scale
neps	number of length scales to evaluate

**Details**

Computes the sample correlation integral over neps length scales starting from eps.min, for embedding dimension  $1, \dots, m$ , considering a t time window (see references). The slope of the linear segment in the log-log plot gives an estimate of the correlation dimension (see the example).

**Value**

Matrix. Column 1: length scales. Column  $i=2, \dots, m+1$ : sample correlation integral for embedding dimension  $i-1$ .

**Author(s)**

Antonio, Fabio Di Narzo

**References**

Hegger, R., Kantz, H., Schreiber, T., Practical implementation of nonlinear time series methods: The TISEAN package; CHAOS 9, 413-435 (1999)

**Examples**

```
d2(lorenz.ts, m=6, d=2, t=4, eps.min=2)
```

---

```
duffing.syst
```

```
Duffing oscillator
```

---

**Description**

Duffing oscillator system, to be used with [sim.cont](#)

**Details**

To be used with [sim.cont](#)

**Author(s)**

Antonio, Fabio Di Narzo

---

```
embedd
```

```
Embedding of a time series
```

---

**Description**

Embedding of a time series with provided time delay and embedding dimension parameters.

**Usage**

```
embedd(x, m, d, lags)
```

**Arguments**

x	time series
m	embedding dimension (if lags missed)
d	time delay (if lags missed)
lags	vector of lags (if m and d are missed)

**Details**

Embedding of a time series with provided delay and dimension parameters.

**Value**

Matrix with columns corresponding to lagged time series.

**Author(s)**

Antonio, Fabio Di Narzo. Multivariate time series patch by Jonathan Shore.

**Examples**

```
library(scatterplot3d)
x <- window(rossler.ts, start=90)
xyz <- embedd(x, m=3, d=8)
scatterplot3d(xyz, type="l")

## embedding multivariate time series
series <- cbind(seq(1,50),seq(101,150))
head(embedd(series, m=6, d=1))
```

---

false.nearest	<i>Method of false nearest neighbours</i>
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---

**Description**

Method of false nearest neighbours to help deciding the optimal embedding dimension

**Usage**

```
false.nearest(series, m, d, t, rt=10, eps=sd(series)/10)
```

**Arguments**

series	time series
m	maximum embedding dimension
d	delay parameter
t	Theiler window
rt	escape factor
eps	neighborhood diameter

**Details**

Method of false nearest neighbours to help deciding the optimal embedding dimension.

**Value**

Fraction of false neighbors (first row) and total number of neighbors (second row) for each specified embedding dimension (columns)

**Author(s)**

Antonio, Fabio Di Narzo

**References**

Hegger, R., Kantz, H., Schreiber, T., Practical implementation of nonlinear time series methods: The TISEAN package; CHAOS 9, 413-435 (1999)

Kennel M. B., Brown R. and Abarbanel H. D. I., Determining embedding dimension for phase-space reconstruction using a geometrical construction, Phys. Rev. A, Volume 45, 3403 (1992).

**Examples**

```
(fn.out <- false.nearest(rossler.ts, m=6, d=8, t=180, eps=1, rt=3))
plot(fn.out)
```

---

lorenz.syst

*Lorenz system*

---

**Description**

Lorenz system, to be used with [sim.cont](#)

**Details**

To be used with [sim.cont](#)

**Author(s)**

Antonio, Fabio Di Narzo

---

lorenz.ts

*Lorenz simulated time series, without noise*

---

**Description**

Lorenz simulated time series, without noise. Of each state of the system, we observe the euclidean norm.

**Details**

Lorenz simulated time series, without noise, obtained with the call: `lorenz.ts <- sim.cont(lorenz.syst, 0, 100, 0.05, start.x=c(5,5,5), parms=c(10, 28, -8/3), obs.fun = function(x) sqrt(sum(x^2)))`

**Author(s)**

Antonio, Fabio Di Narzo

---

Lyapunov exponent      *Tools to evaluate the maximal Lyapunov exponent of a dynamic system*

---

**Description**

Tools to evaluate the maximal Lyapunov exponent of a dynamic system from a univariate time series

**Usage**

```
lyap_k(series, m, d, t, k=1, ref, s, eps)
lyap(dsts, start, end)
```

**Arguments**

series	time series
m	embedding dimension
d	time delay
k	number of considered neighbours
eps	radius where to find nearest neighbours
s	iterations along which follow the neighbours of each point
ref	number of points to take into account
t	Theiler window
dsts	Should be the output of a call to lyap_k (see the example)
start	Starting time of the linear bite of dsts
end	Ending time of the linear bite of dsts

**Details**

The function lyap\_k estimates the largest Lyapunov exponent of a given scalar time series using the algorithm of Kantz.

The function lyap computes the regression coefficients of a user specified segment of the sequence given as input.

**Value**

lyap\_k gives the logarithm of the stretching factor in time.

lyap gives the regression coefficients of the specified input sequence.

**Author(s)**

Antonio, Fabio Di Narzo

## References

Hegger, R., Kantz, H., Schreiber, T., Practical implementation of nonlinear time series methods: The TISEAN package; CHAOS 9, 413-435 (1999)

M. T. Rosenstein, J. J. Collins, C. J. De Luca, A practical method for calculating largest Lyapunov exponents from small data sets, Physica D 65, 117 (1993)

## See Also

`mutual`, `false.nearest` for the choice of optimal embedding parameters. `embedd` to perform embedding.

## Examples

```
output <-lyap_k(lorenz.ts, m=3, d=2, s=200, t=40, ref=1700, k=2, eps=4)
plot(output)
lyap(output, 0.73, 2.47)
```

---

<code>mutual</code>	<i>Average Mutual Information</i>
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---

## Description

Estimates the average mutual information index (ami) of a given time series for a specified number of lags

## Usage

```
mutual(series, partitions = 16, lag.max = 20, plot=TRUE, ...)
```

## Arguments

<code>series</code>	time series
<code>partitions</code>	number of bins
<code>lag.max</code>	largest lag
<code>plot</code>	logical. If 'TRUE' (the default) the ami is plotted
<code>...</code>	further arguments to be passed to the plot method

## Details

Estimates the mutual information index for a specified number of lags. The joint probability distribution function is estimated with a simple bi-dimensional density histogram.

## Value

An object of class "ami", which is a vector containing the estimated mutual information index for each lag between 0 and `lag.max`.

**Author(s)**

Antonio, Fabio Di Narzo

**References**

Hegger, R., Kantz, H., Schreiber, T., Practical implementation of nonlinear time series methods: The TISEAN package; CHAOS 9, 413-435 (1999)

**Examples**

```
mutual(lorenz.ts)
```

---

plot.ami

*Plotting average mutual information index*

---

**Description**

Plotting method for objects inheriting from class "ami".

**Usage**

```
## S3 method for class 'ami'  
plot(x, main = NULL, ...)
```

**Arguments**

x                    "ami" object  
main, ...            additional graphical arguments

**Details**

Plots the ami for each lag in x.

**Author(s)**

Antonio, Fabio Di Narzo

**See Also**

[mutual](#)

---

plot.d2                      *Plotting sample correlation integrals*

---

**Description**

Plotting method for objects inheriting from class "d2".

**Usage**

```
## S3 method for class 'd2'  
plot(x, ...)
```

**Arguments**

x                      "d2" object  
...                    additional graphical arguments

**Details**

Plots the sample correlation integrals in x in log-log scale, as a line for each considered embedding dimension.

**Author(s)**

Antonio, Fabio Di Narzo

**See Also**

[d2](#)

---

plot.false.nearest            *Plotting false nearest neighbours results*

---

**Description**

Plotting method for objects inheriting from class "false.nearest".

**Usage**

```
## S3 method for class 'false.nearest'  
plot(x, ...)
```

**Arguments**

x                      "false.nearest" object  
...                    additional graphical arguments

**Details**

Plots the results of [false.nearest](#).

**Author(s)**

Antonio, Fabio Di Narzo

**See Also**

[false.nearest](#)

---

print.d2

*Printing sample correlation integrals*

---

**Description**

Printing method for objects inheriting from class `"d2"`.

**Usage**

```
## S3 method for class 'd2'  
print(x, ...)
```

**Arguments**

x	"d2" object
...	additional arguments to 'print'

**Details**

Simply calls [plot.d2](#).

**Author(s)**

Antonio, Fabio Di Narzo

**See Also**

[plot.d2](#), [d2](#)

---

`print.false.nearest`     *Printing false nearest neighbours results*

---

**Description**

Printing method for objects inheriting from class `"false.nearest"`.

**Usage**

```
## S3 method for class 'false.nearest'  
print(x, ...)
```

**Arguments**

<code>x</code>	<code>"false.nearest"</code> object
<code>...</code>	additional arguments to <code>'print'</code>

**Details**

Prints the table of results of `false.nearest`.

**Author(s)**

Antonio, Fabio Di Narzo

**See Also**

`plot.false.nearest`, `false.nearest`

---

`recurr`     *Recurrence plot*

---

**Description**

Recurrence plot

**Usage**

```
recurr(series, m, d, start.time=start(series), end.time=end(series), ...)
```

**Arguments**

series	time series
m	embedding dimension
d	time delay
start.time	starting time window (in time units)
end.time	ending time window (in time units)
...	further parameters to be passed to filled.contour

**Details**

Produces the recurrence plot, as proposed by Eckmann et al. (1987). White is maximum distance, black is minimum.

**warning**

Be aware that number of distances to store goes as  $n^2$ , where  $n = \text{length}(\text{window}(\text{series}, \text{start}=\text{start.time}, \text{end}=\text{end.time}))$ !

**Author(s)**

Antonio, Fabio Di Narzo

**References**

Eckmann J.P., Oliffson Kamphorst S. and Ruelle D., Recurrence plots of dynamical systems, Europhys. Lett., volume 4, 973 (1987)

**Examples**

```
recurr(lorenz.ts, m=3, d=2, start.time=15, end.time=20)
```

---

rossler.syst

*Roessler system of equations*

---

**Description**

Roessler system of equations

**Details**

To be used with [sim.cont.](#)

**Author(s)**

Antonio, Fabio Di Narzo

---

rossler.ts	<i>Roessler simulated time series, without noise</i>
------------	--

---

**Description**

Roessler simulated time series, without noise. Of each state of the system, we observe the first component.

**Details**

Roessler simulated time series, without noise, obtained with the call:

```
rossler.ts <- sim.cont(rossler.syst, start=0, end=650, dt=0.1, start.x=c(0,0,0), parms=c(0.15, 0.2, 10))
```

**Author(s)**

Antonio, Fabio Di Narzo

---

sim.cont	<i>Simulates a continuous dynamic system</i>
----------	--

---

**Description**

Simulates a dynamic system of provided ODEs

**Usage**

```
sim.cont(syst, start.time, end.time, dt, start.x, parms=NULL, obs.fun=function(x) x[1])
```

**Arguments**

syst	ODE system
start.time	starting time
end.time	ending time
dt	time between observations
start.x	initial conditions
parms	parameters for the system
obs.fun	observed function of the state

**Details**

Simulates a dynamic system of provided ODEs. Uses `lsoda` in `odesolve` for numerical integration of the system.

**Value**

The time series of the observed function of the system's state

**Author(s)**

Antonio, Fabio Di Narzo

**See Also**

[lorenz.syst](#), [rossler.syst](#), [duffing.syst](#)

**Examples**

```
rossler.ts <- sim.cont(rossler.syst, start=0, end=650, dt=0.1,
                      start.x=c(0,0,0), parms=c(0.15, 0.2, 10))
```

---

 stplot

*Space-time separation plot*


---

**Description**

Space-time separation plot

**Usage**

```
stplot(series, m, d, idt=1, mdt)
```

**Arguments**

series	time series
m	embedding dimension
d	time delay
idt	observation steps in each iteration
mdt	number of iterations

**Details**

Produces the space-time separation plot, as introduced by Provenzale et al. (1992), which can be used to decide the Theiler time window  $t$ , which is required in many other algorithms in this package.

It plots the probability that two points in the reconstructed phase-space have distance smaller than epsilon in function of epsilon and of the time  $t$  between the points, as iso-lines at levels 10%, 20%, ..., 100%.

**Value**

lines of constant probability at 10%, 20%, ..., 100%.

**Author(s)**

Antonio, Fabio Di Narzo

**References**

Kantz H., Schreiber T., Nonlinear time series analysis. Cambridge University Press, (1997)

Provenzale A., Smith L. A., Vio R. and Murante G., Distinguishing between low-dimensional dynamics and randomness in measured time series. Physica D., volume 58, 31 (1992)

**See Also**

[false.nearest, d2, lyap\\_k](#)

**Examples**

```
stplot(rossler.ts, m=3, d=8, idt=1, mdt=250)
```

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